

Synchrotron and magnetic fields with GALPROP

Elena Orlando & Andy Strong, MPE Garching

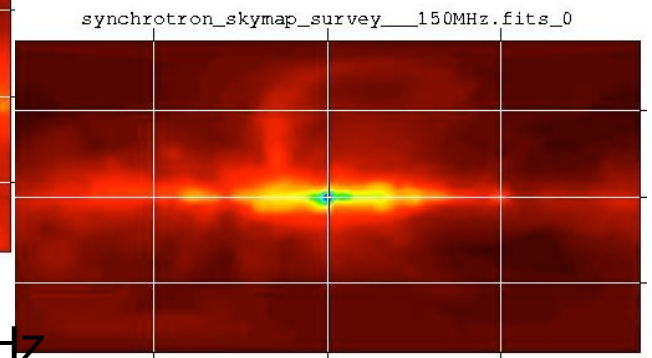
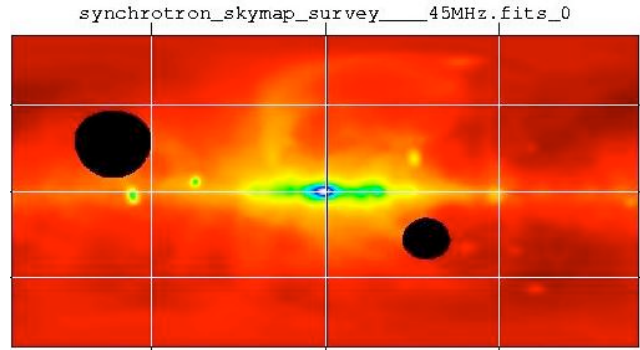
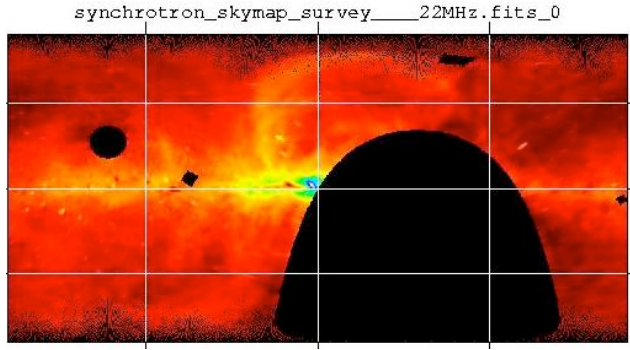
UHECR and Magnetic field Workshop,
Ringberg, 11-14 Feb 2009

Aim

- Testing existing models of B
- Improving the models

Procedure

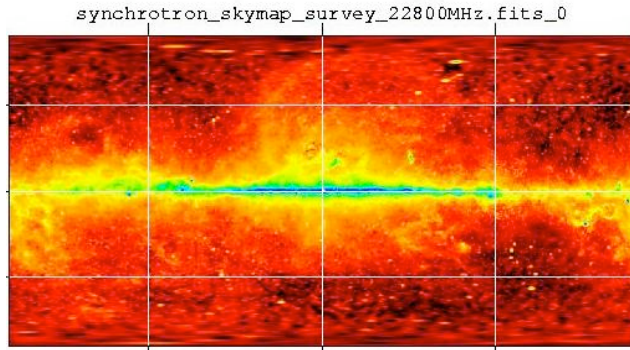
- Used CR sources distribution, and the electron spectrum that fits the FERMI intermediate latitude spectrum (see Strong's talk).
- 3D model of the regular field and random field component implemented in GALPROP
- Adjusting the value of total magnetic field to fit the synchrotron spectrum at the 408 MHz map
- Comparing synchrotron latitude and longitude profiles with the available radio surveys.



22 MHz

45 MHz

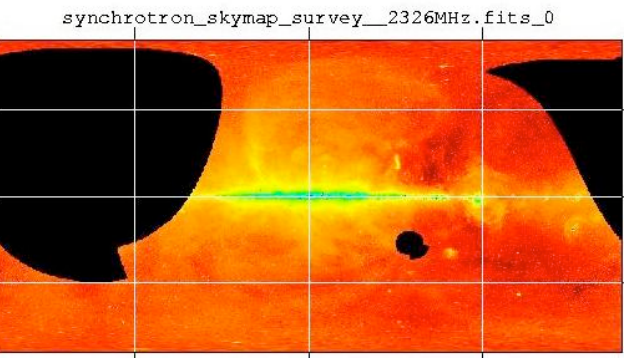
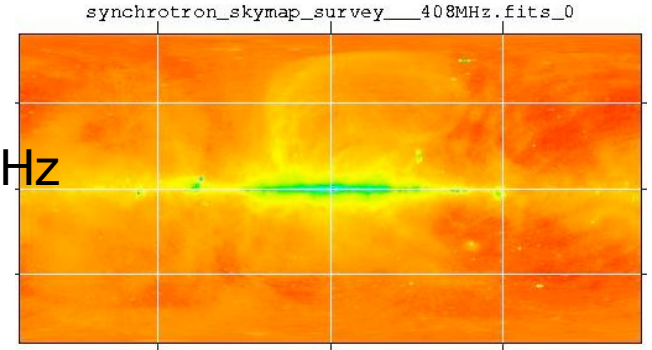
150 MHz



23 GHz

Continuum
sky surveys

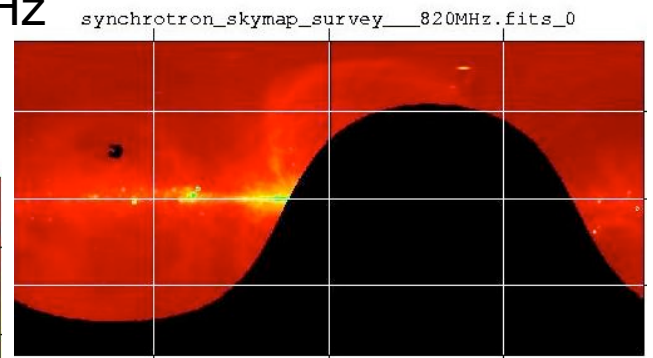
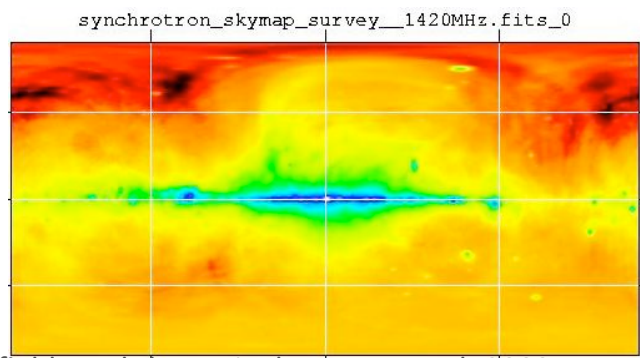
408 MHz



2.3 GHz

820 MHz

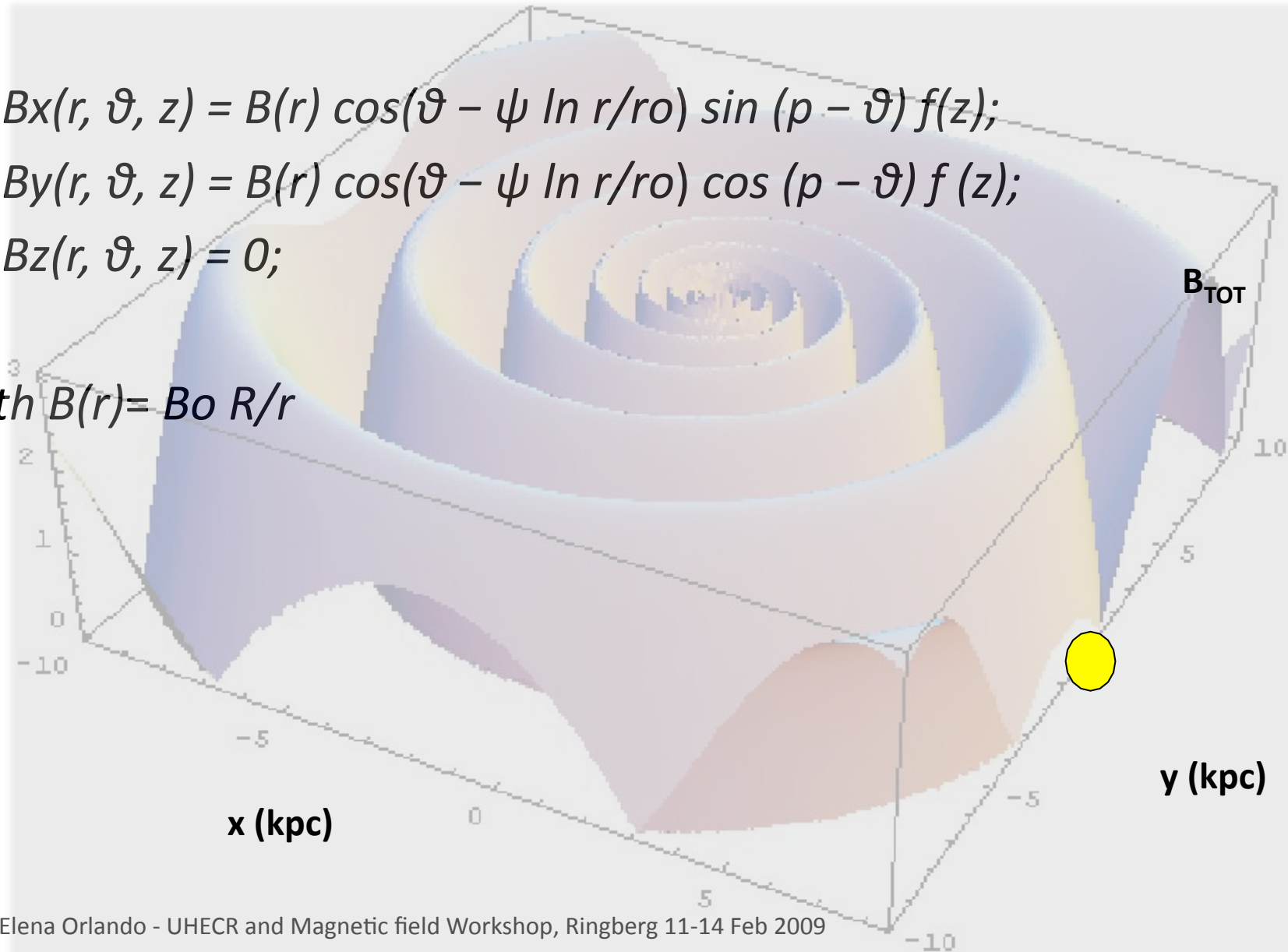
1.4 GHz



Spiral Magnetic field

- $B_x(r, \vartheta, z) = B(r) \cos(\vartheta - \psi \ln r/r_0) \sin(p - \vartheta) f(z);$
- $B_y(r, \vartheta, z) = B(r) \cos(\vartheta - \psi \ln r/r_0) \cos(p - \vartheta) f(z);$
- $B_z(r, \vartheta, z) = 0;$

with $B(r) = B_0 R/r$



Tinyakov & Tkachev (2002) model

$$B(r) = B_0 R/r \quad \text{for } r > 4\text{kpc};$$

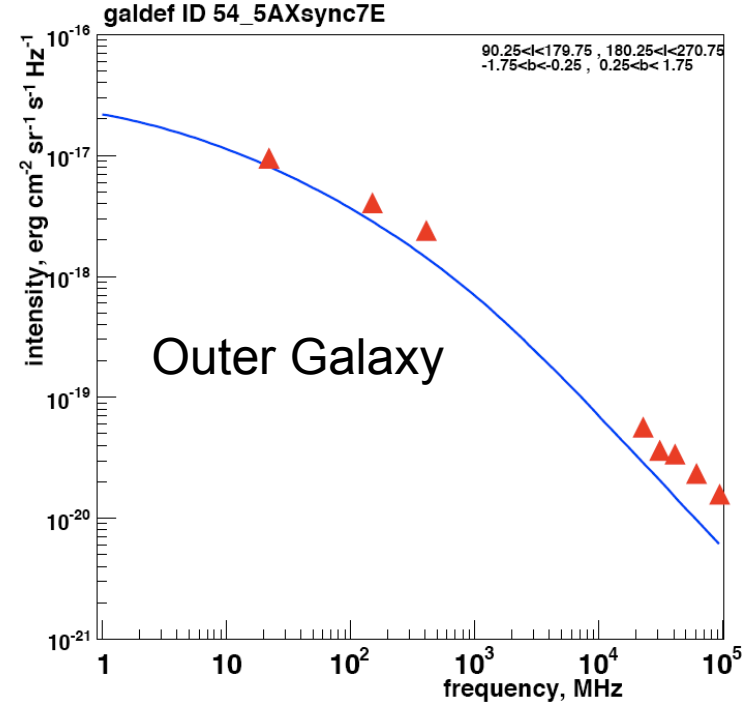
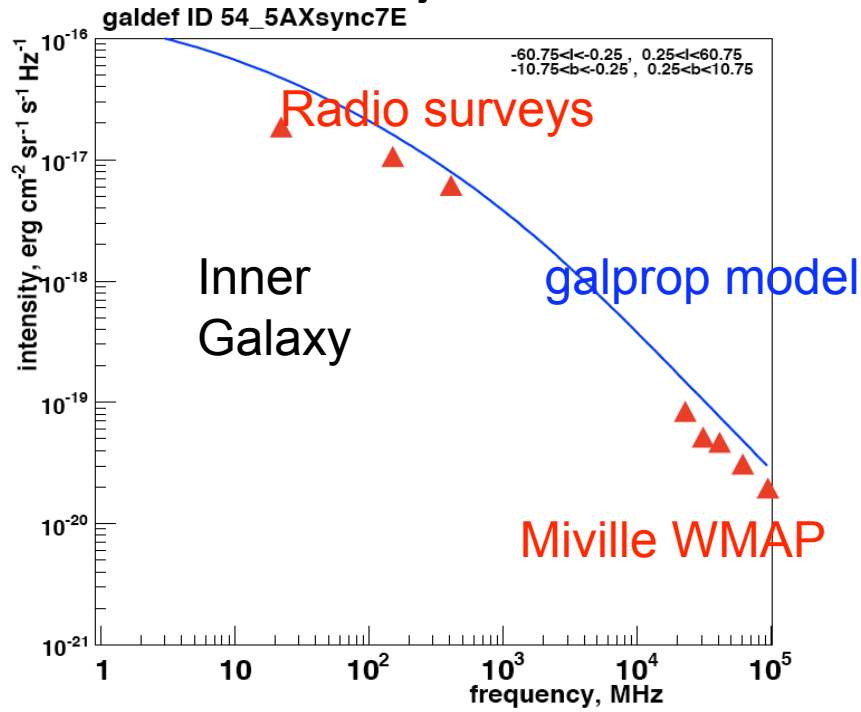
$$B(r) = \text{const} \quad \text{for } r \leq 4\text{kpc};$$

$$B_0 = 8\mu\text{G}; \quad p = -8^\circ; \quad r_0 = 10; \quad B(\text{local}) = 3.3\mu\text{G}$$

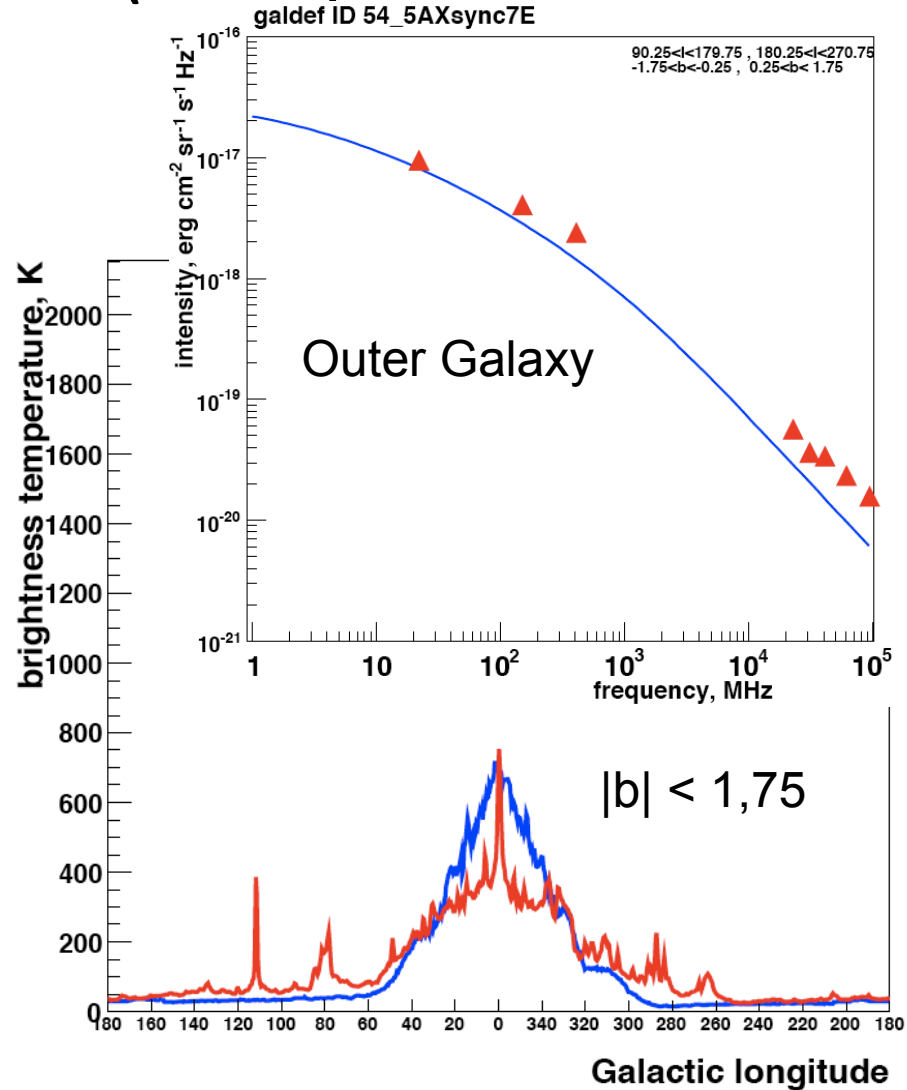
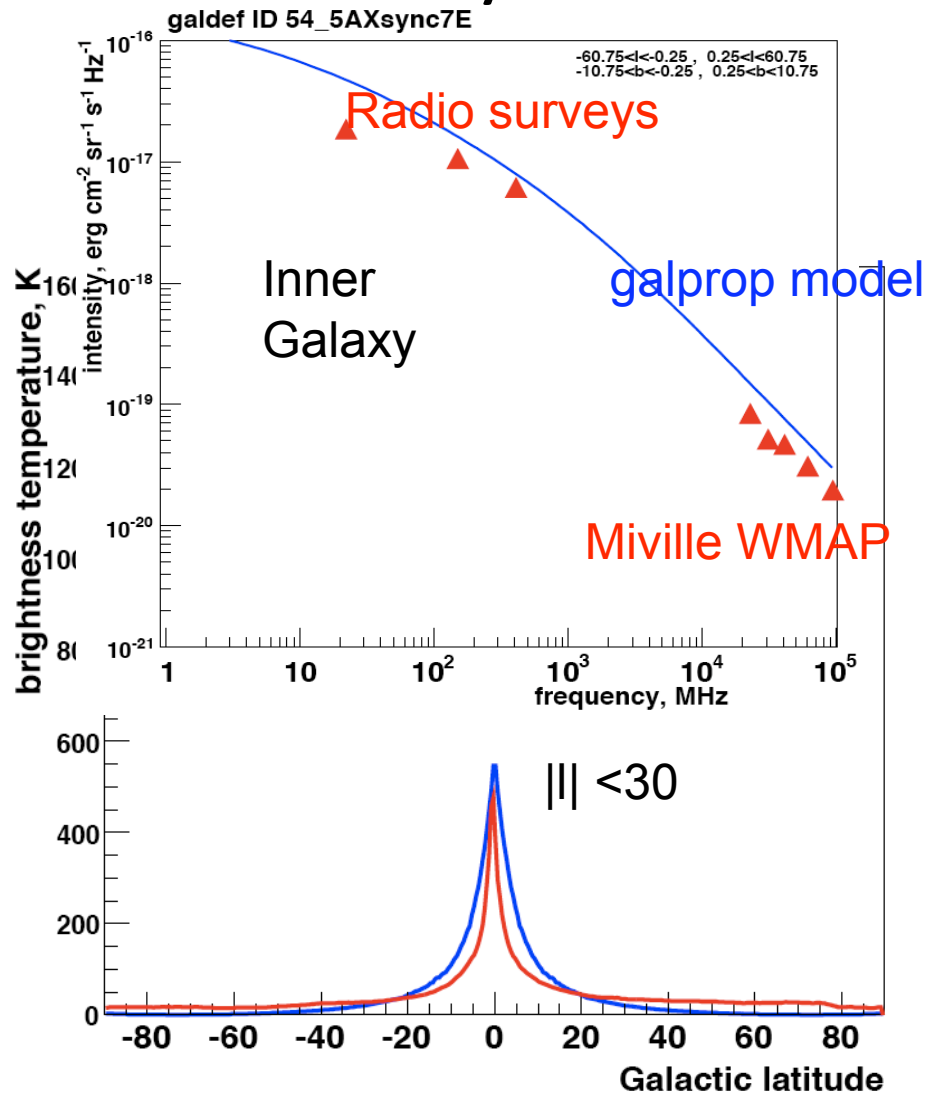
- $f(z) = \text{sign}(z) \exp(-|z|/h)$ with $h = 1.5\text{kpc}$
- no info on B random in TT(2002), hence we took 3 formulations:
 - 1) const. everywhere
 - 2) const in $z=0$, but decreasing with $f(z)$
 - 3) following the spiral structure, with a scale factor

B random/B regular = 0.57 (Miville-Deschenes et al. 2008)

Tinyakov & Tkachev (2002) results



Tinyakov & Tkachev (2002) results



**TINYAKOV & TKACHEV (2002) MODEL DOES NOT MATCH
LATITUDE AND LONGITUDE PROFILES**

Model 2 (new)

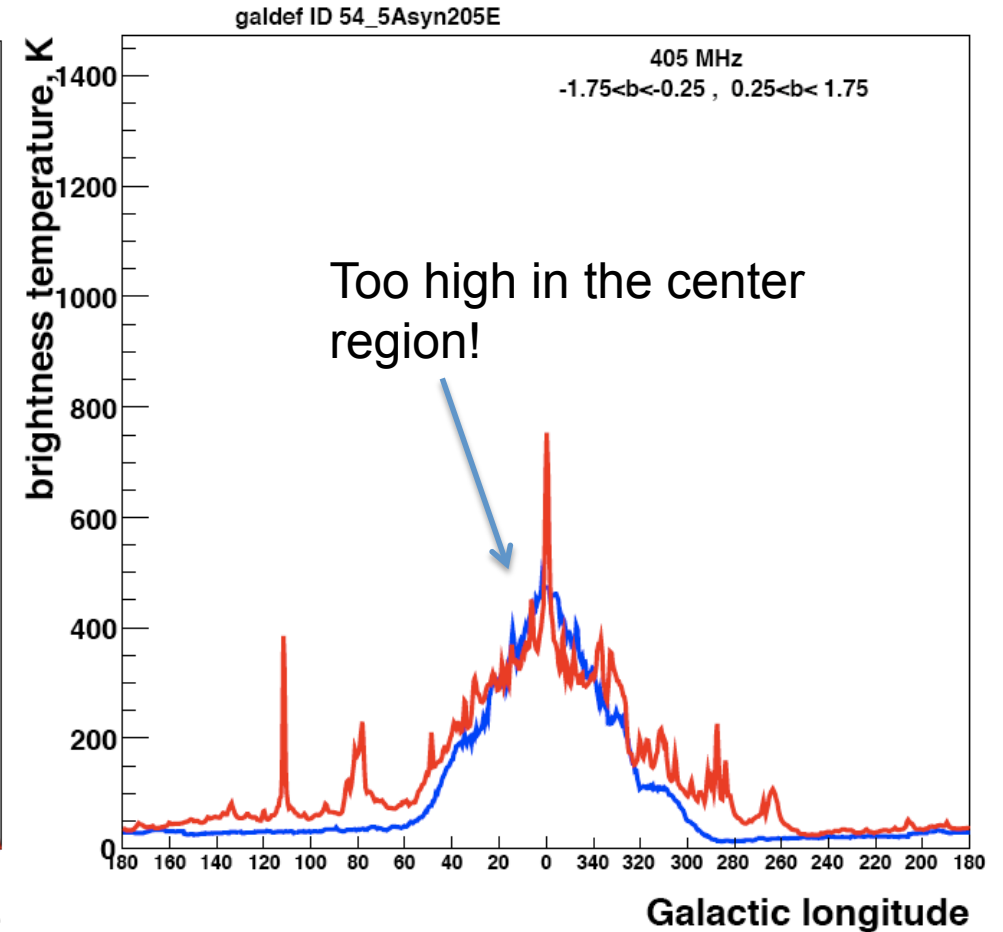
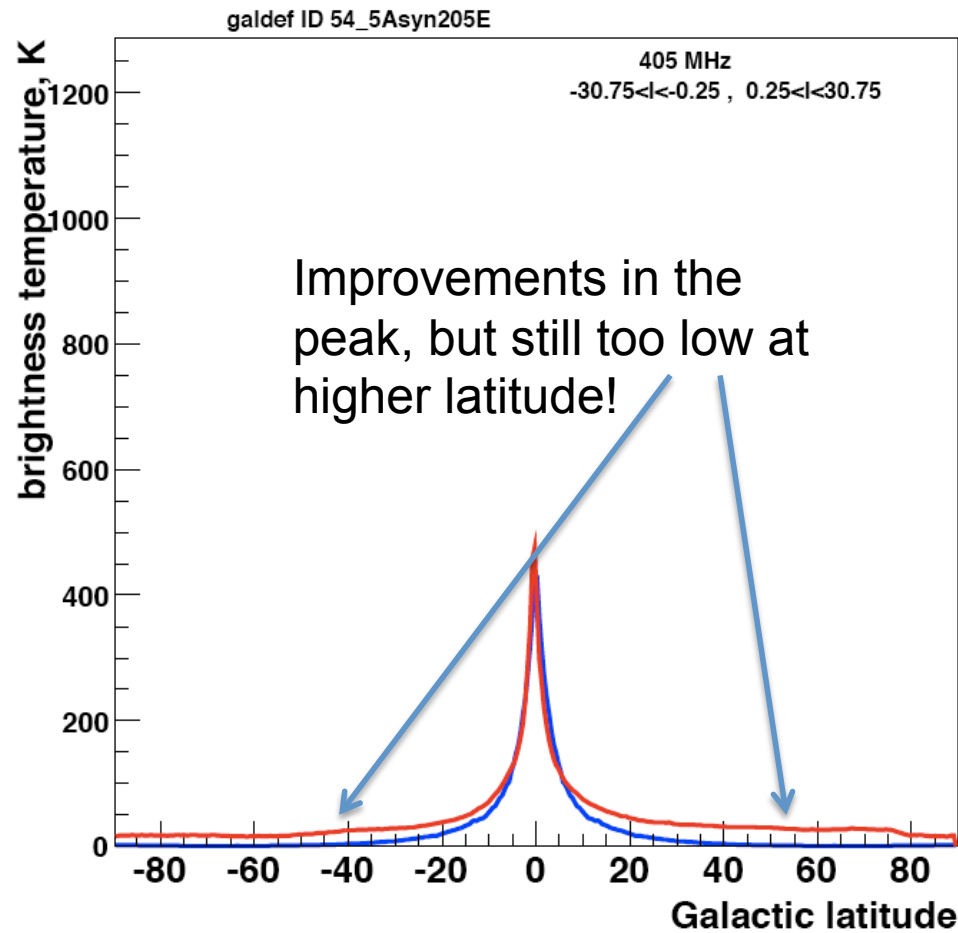
$$B(r) = B_0 R/r \quad \text{for } r > 5 \text{ kpc};$$

$$B(r) = \text{const} \quad \text{for } r \leq 5 \text{ kpc};$$

$$B_0 = 8\mu\text{G}; \quad p = -8.5^\circ; \quad r_0 = 10; \quad B(\text{local}) = 3.3\mu\text{G}$$

- $f(z) = \text{sign}(z) \exp(-|z|/h)$ with $h = 1 \text{ kpc}$
- B random 3 formulations:
 - 1) const. everywhere (no improvements)
 - 2) const in $z=0$, but decreasing with $f(z)$ (improved)
 - 3) following the spiral structure, with a scale factor (improved)

Model 2 results



Model 3 (+toroidal as in Sun et al. 2008)

$B(r)=B_0=8 \mu\text{G}$; $p = -8.5^\circ$; $r_0 = 10$; $B_{reg}(local)=3.7 \mu\text{G}$ and $B_{ran}(local)=2 \mu\text{G}$

- $f(z) = \text{sign}(z) \exp(-|z|/h)$ with $h = 1 \text{ kpc}$

Random following the spiral structure, with a scale factor

+ HALO TOROIDAL FIELD (Sun et al. 2008)

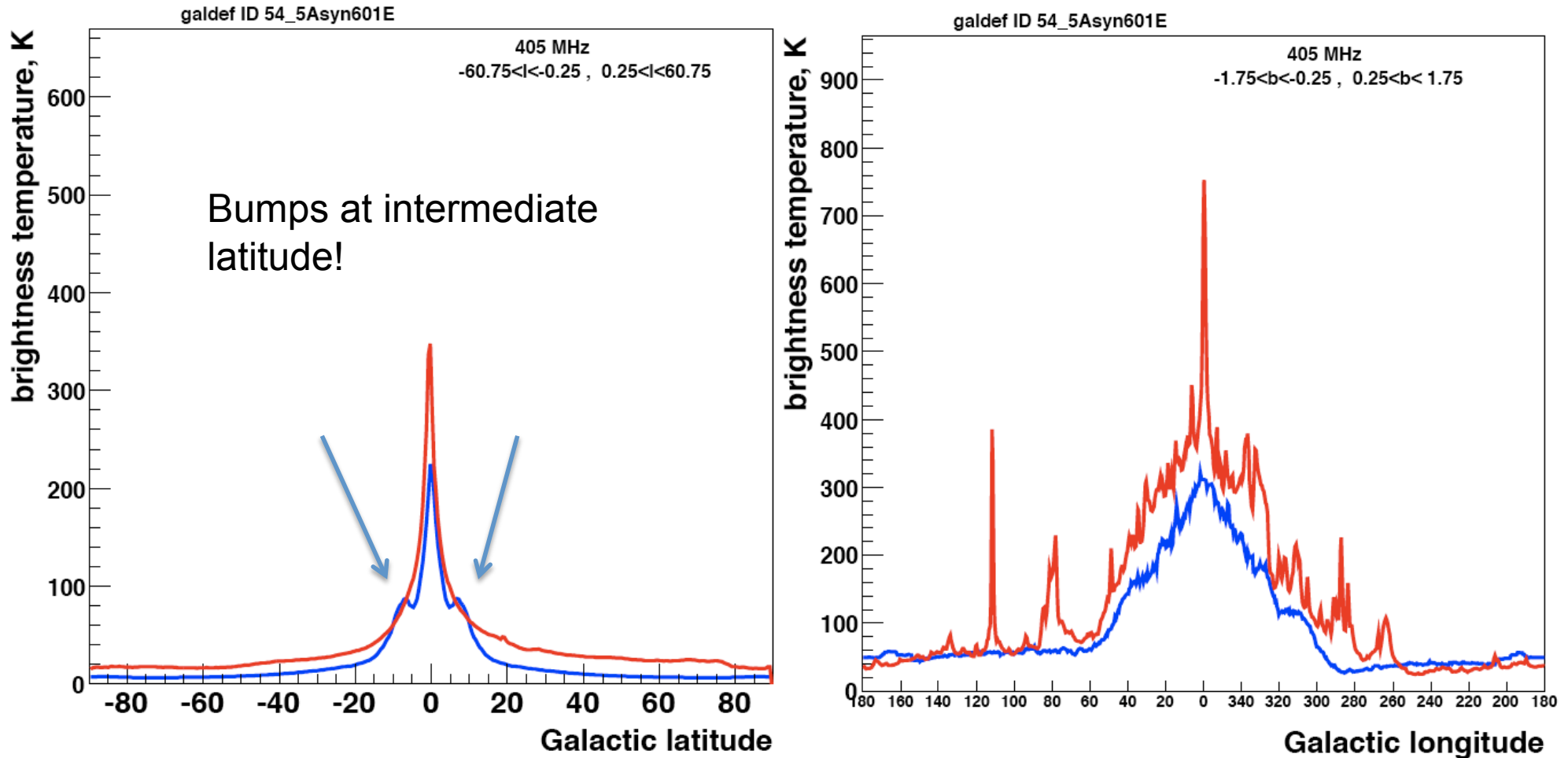
$$B_x = BT \cos(\varphi)$$

$$B_y = -BT \sin(\varphi)$$

$$B_T = B_0^H \frac{1}{1 + \left(\frac{|z| - z_0^H}{z_1^H}\right)^2} \frac{R}{R_0^H} \exp\left(-\frac{R - R_0^H}{R_0^H}\right)$$

$z_{Ho} = 1.5 \text{ kpc}$,
 $z_{H1} = 0.2 \text{ kpc}$ for $|z| < z_{Ho}$
 $z_{H1} = 0.4 \text{ kpc}$ otherwise,
 $B_{Ho} = 10 \mu\text{G}$ (Prouza & smida 2003)
 $B_{Ho} = 2 \mu\text{G}$ (Sun et al. 2008)
and $R_{Ho} = 4 \text{ kpc}$.

Model 3 (toroidal as in Sun et al. 2008) results



If $BHo = 10 \mu\text{G}$, showed in the plots, (Prouza & Smida 2003) the bumps are not in agreement with the data, but If $BHo = 2 \mu\text{G}$ (Sun et al. 2008), the contribution of this model to the synchrotron and hence the bumps are not significant.

Dipole field: Prouza & Smida (2003)

$$B_x = -\frac{3K}{2r^3} \sin 2\beta \sin \theta$$

$$B_y = -\frac{3K}{2r^3} \sin 2\beta \cos \theta$$

$$B_z = -\frac{K}{r^3} (3 \cos^2 \beta - 1)$$

$0 < \beta < \pi$ from north to south pole

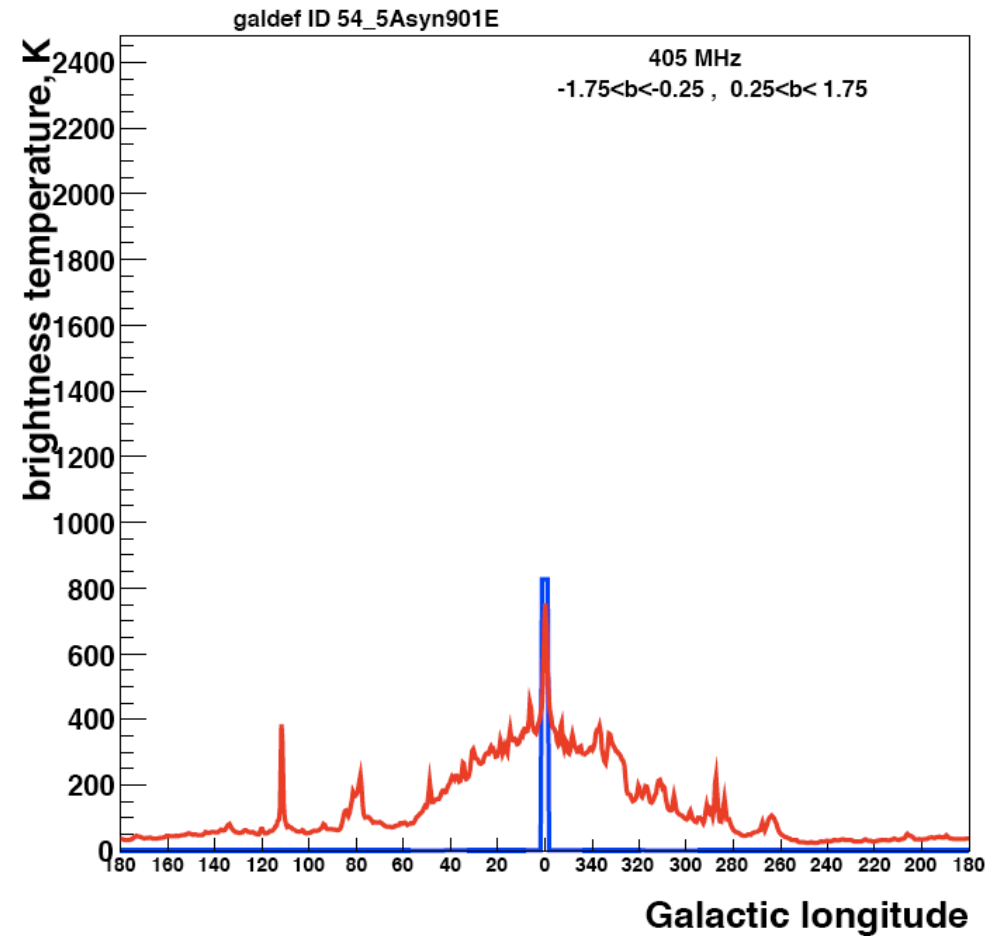
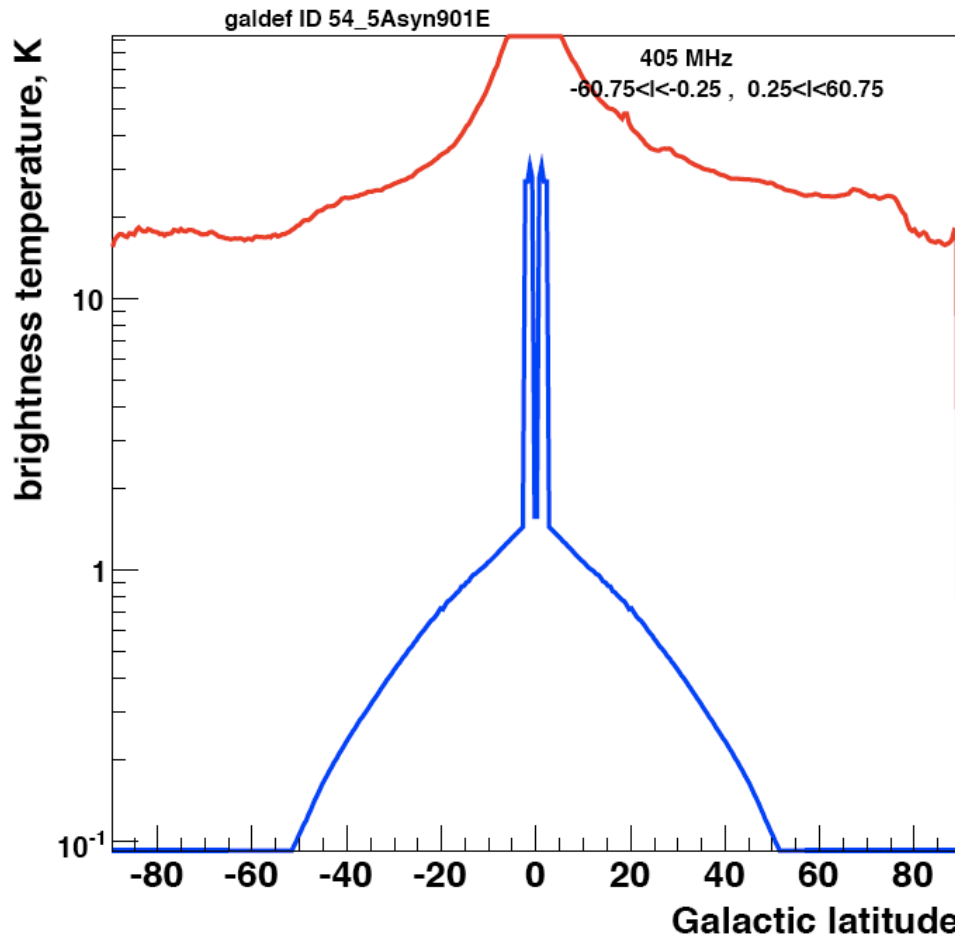
- cylinder (height 300 pc, diameter 100 pc) with constant strength = 2 mG

$K = 10^5 \text{ G pc}^3$ for outer regions ($R > 5 \text{ kpc}$),

$K = 200 \text{ G pc}^3$ for central region ($R < 2 \text{ kpc}$)

10^{-6} G constant for $2 \text{ kpc} < R < 5 \text{ kpc}$

Dipole field: Prouza & Smida (2003)



No significant contribution of a dipole field out from the Galactic center.
However it is possible to constrain the maximum B value in the central
region < 2 mG!

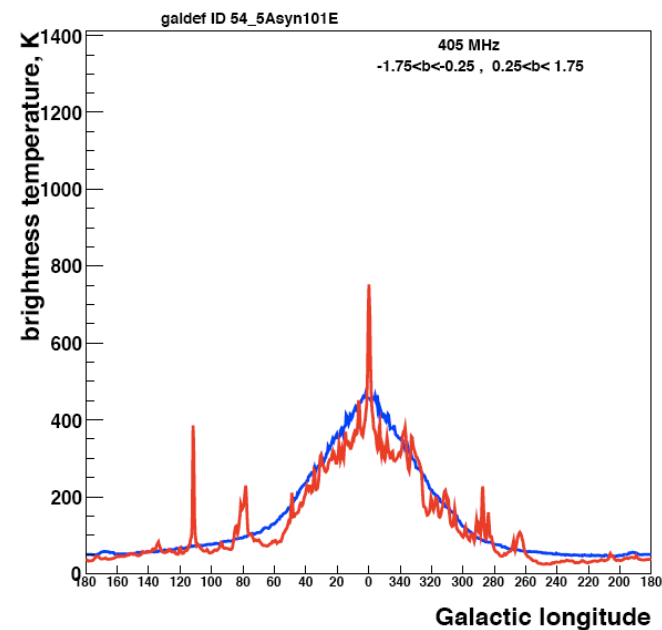
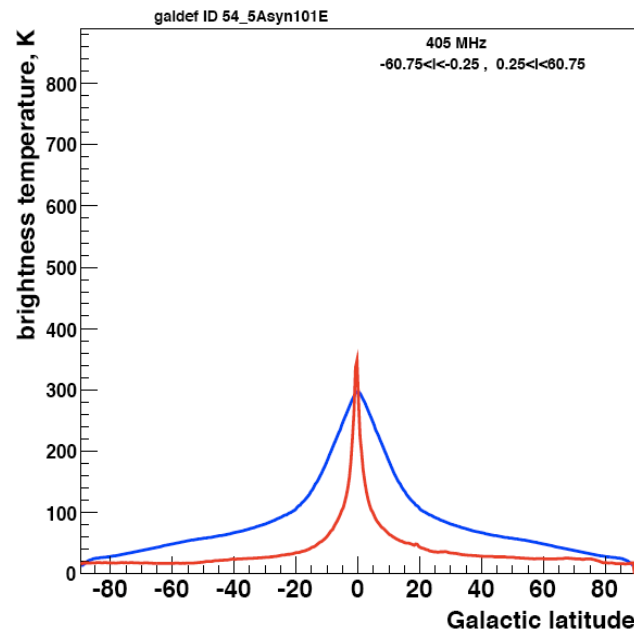
Miville-Deschenes et al. 2008

$B(r) = B_0 = \text{const}$ everywhere

$B_0 = 8 \mu\text{G}$; $p = -8.5^\circ$; $r_0 = 11$; $B_{\text{reg}}(\text{local}) = 1,2 \mu\text{G}$; $B_{\text{ran}}(\text{local}) = 0,7 \mu\text{G}$

- $f(z) = \cos \chi$; with $\chi(z) = \chi_0 \tanh(z/z_H)$ and $z_H = 1 \text{ kpc}$ and $\chi_0 = 8^\circ$

We took many models of random magnetic field, but no much difference



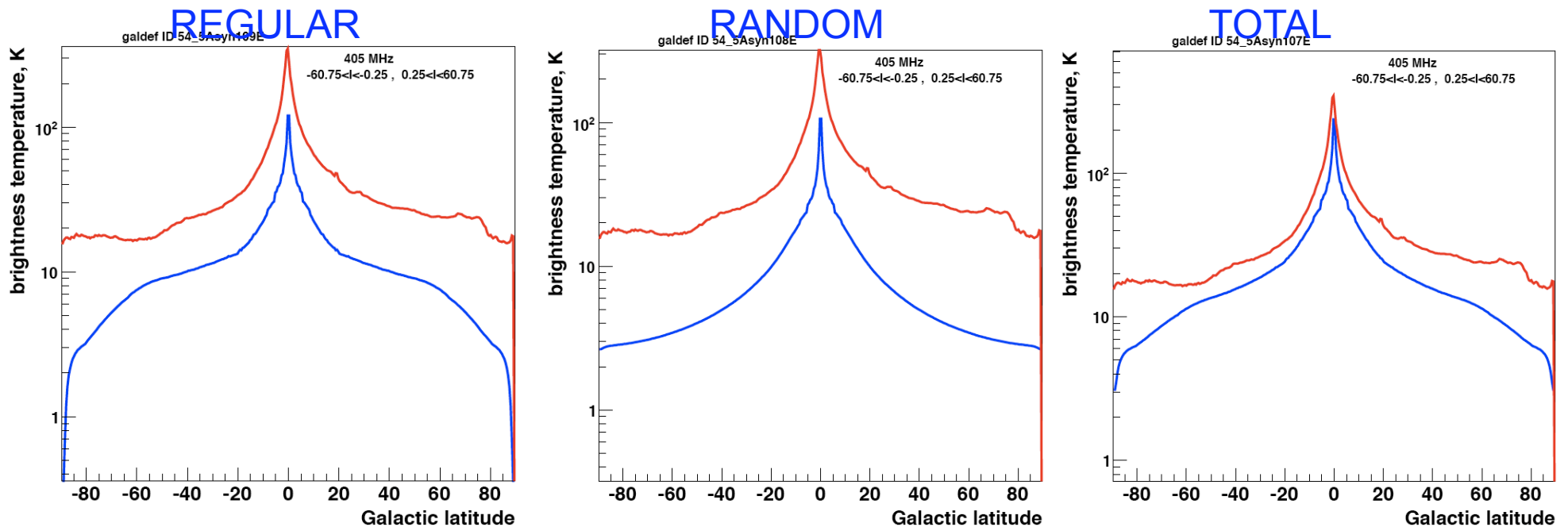
IT DOES NOT AGREE WITH DATA OUT OF THE PLANE

Model 4

$B(r) = B_0 = \text{const}$ everywhere

$B_0 = 9 \mu\text{G}$; $p = -8.5^\circ$; $r_0 = 11$; $B_{\text{reg}}(\text{local}) = 1,4 \mu\text{G}$; $B_{\text{ran}}(\text{local}) = 5 \mu\text{G}$

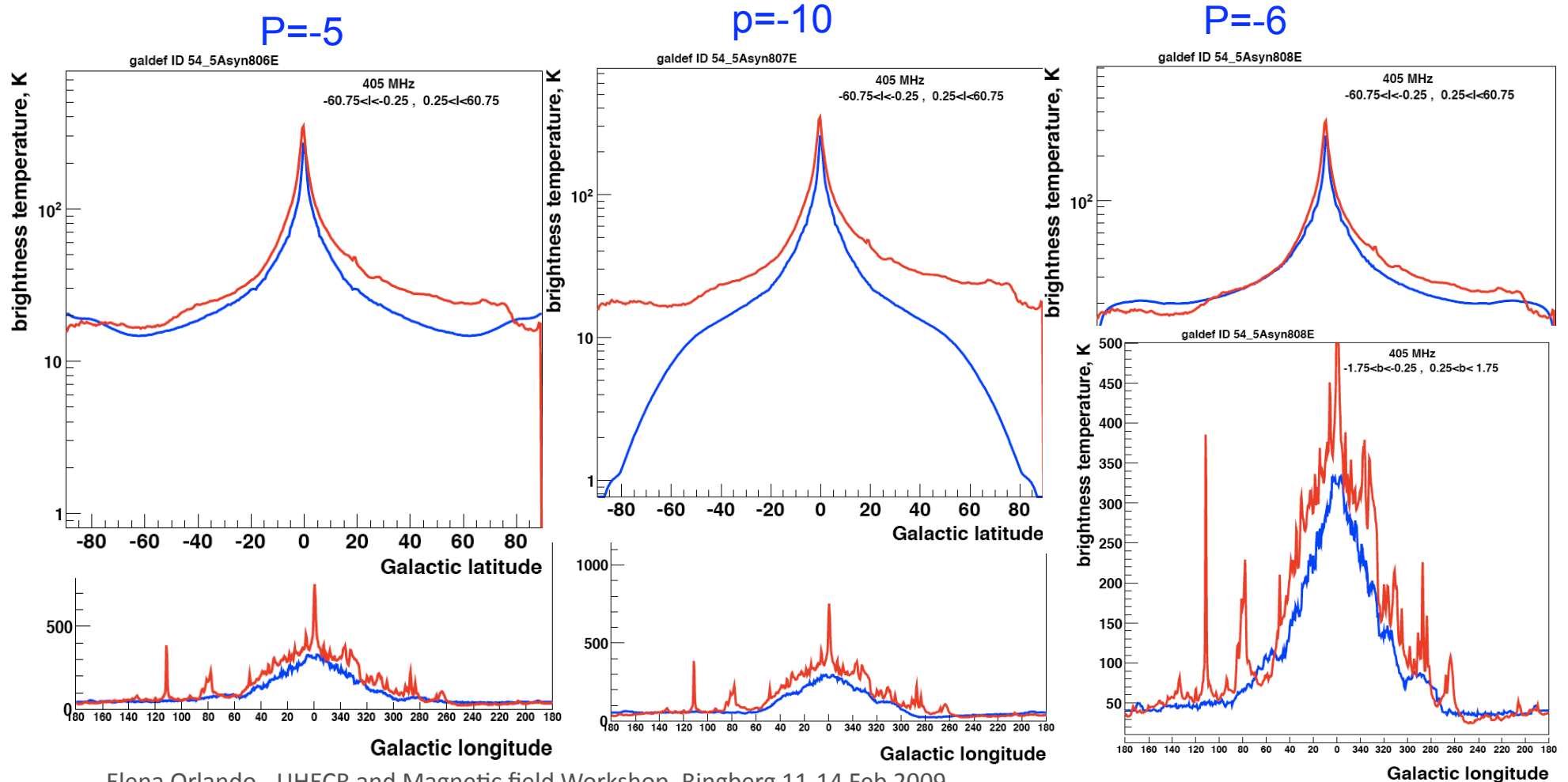
- $f(z) = \cos \chi$; with $\chi(z) = \chi_0 \tanh(z/z_H)$ and $z_H = 0,1 \text{ kpc}$ and $\chi_0 = 65^\circ$
- Random field constant in $z=0$, but decreasing with $f(z)$



Model 5

$$B(r) = B_0 = 10 \mu\text{G}; r_0 = 11;$$

- $f(z) = \cos \chi$; with $\chi(z) = \chi_0 \tanh(z/z_H)$ and $z_H = 0,2 \text{ kpc}$ and $\chi_0 = 65^\circ$
- Random field scaling with the regular

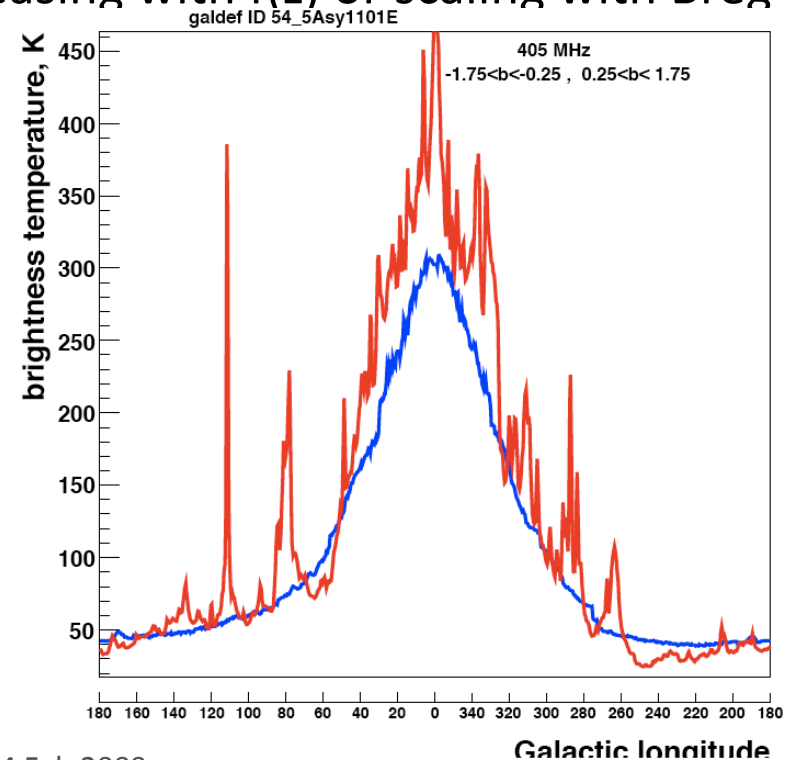
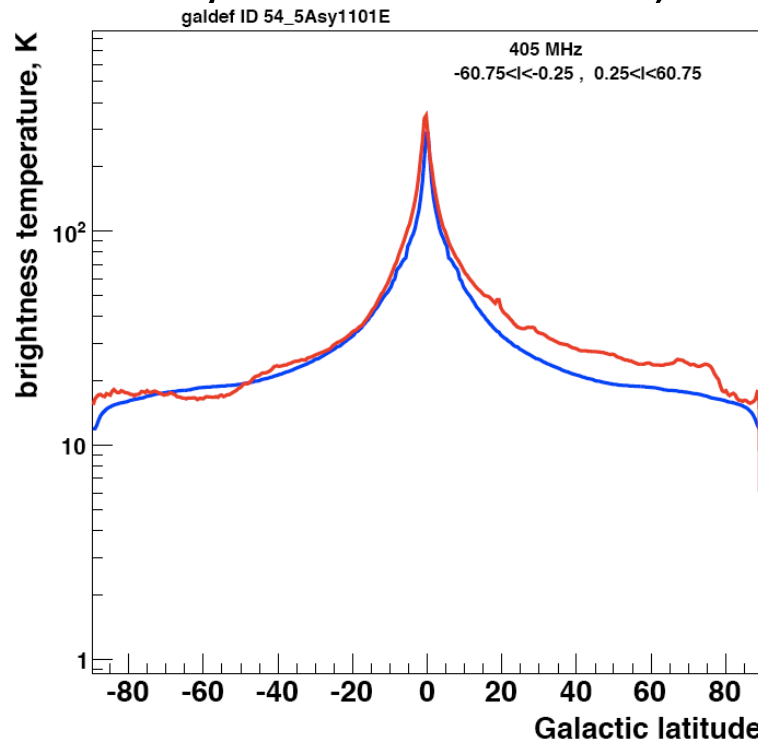


Best Galprop Model

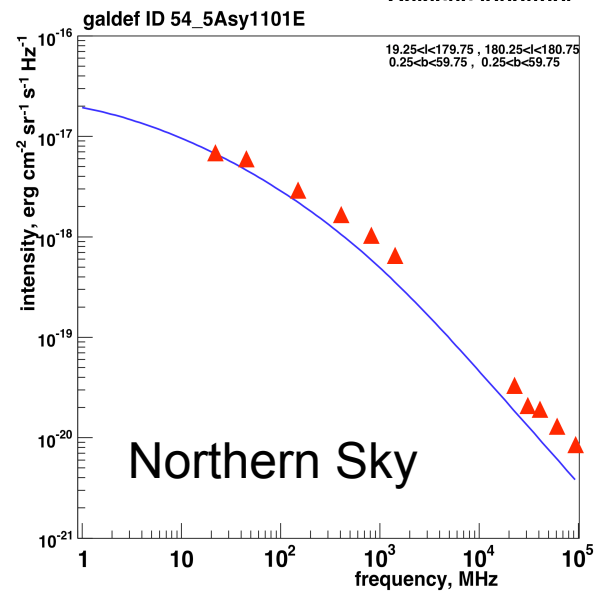
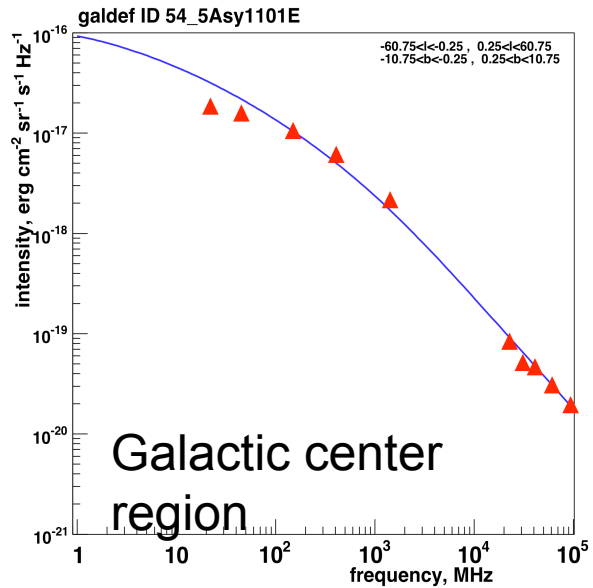
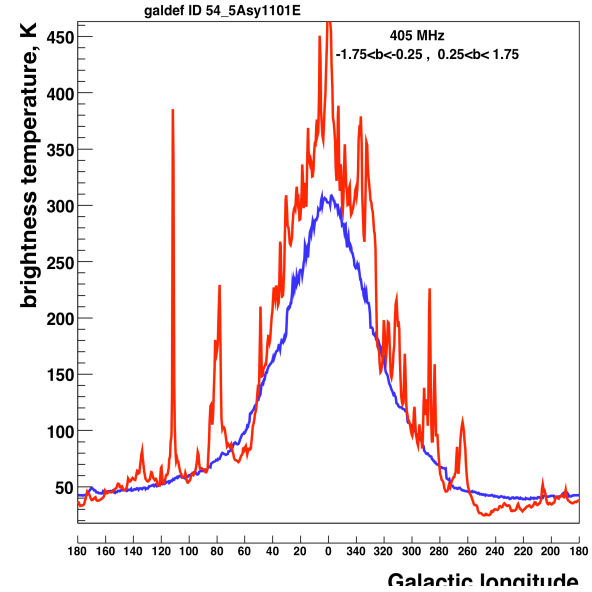
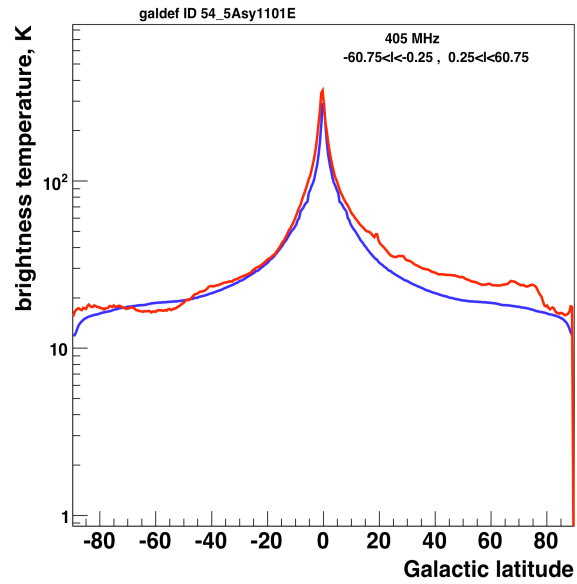
$B(r) = B_0 = \text{const}$ everywhere

$B_0 = 9 \mu\text{G}$; $\rho = -8.5^\circ$; $r_0 = 12,3$; $B_{\text{reg}}(\text{local}) = 6,2 \mu\text{G}$; $B_{\text{ran}}(\text{local}) \sim 4-5 \mu\text{G}$

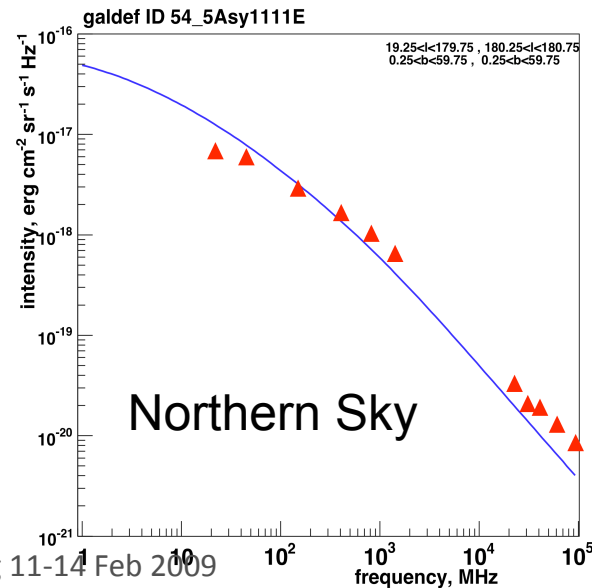
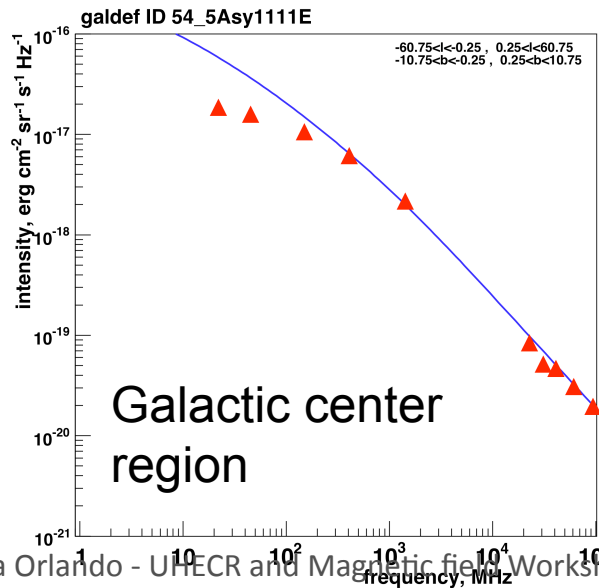
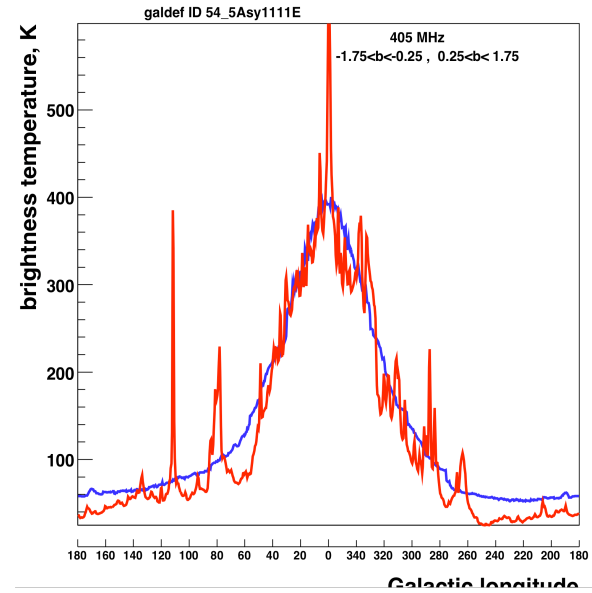
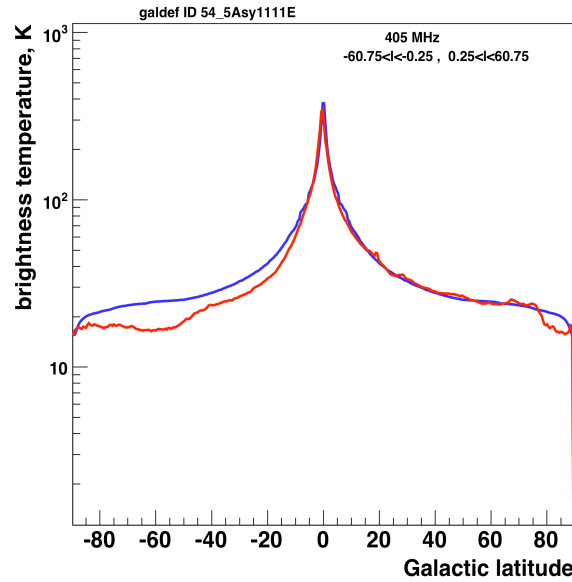
- $f(z) = \cos \chi$; with $\chi(z) = \chi_0 \tanh(z/z_H)$ and $z_H = 0,2 \text{ kpc}$ and $\chi_0 = 65^\circ$
- Random field constant in $z=0$, but decreasing with $f(z)$ or scaling with B_{reg}



Best Galprop model no secondaries

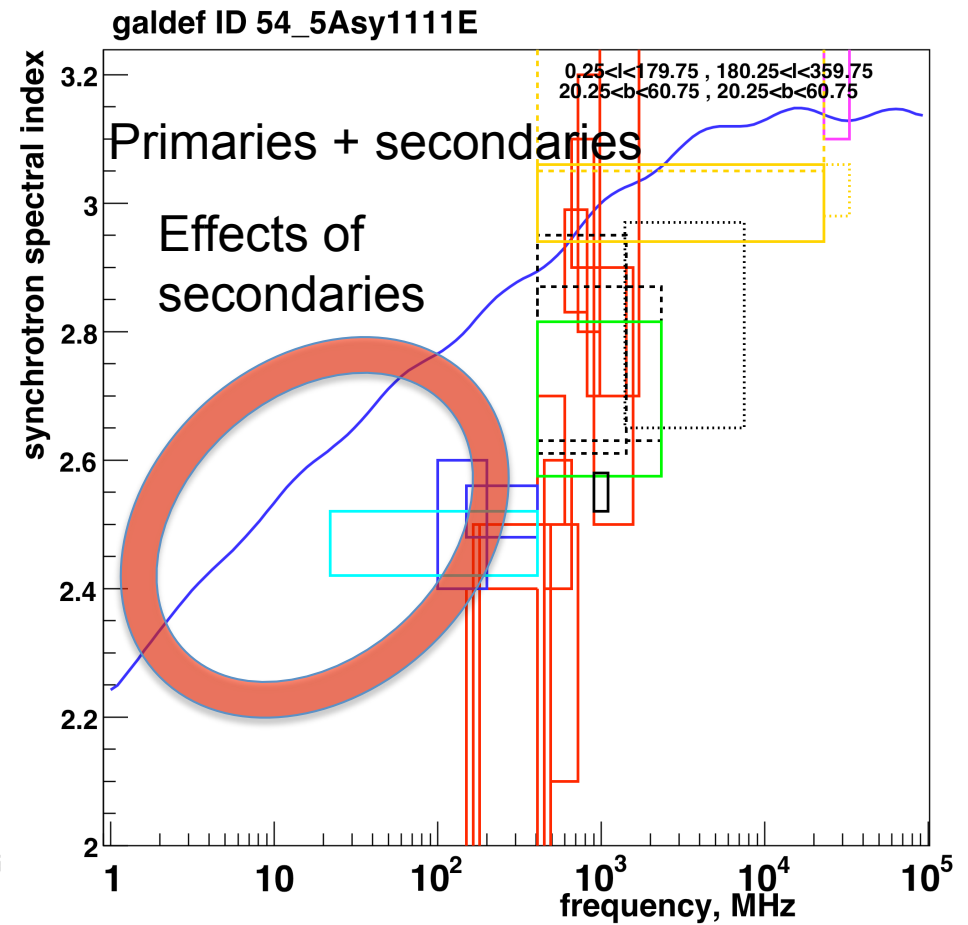
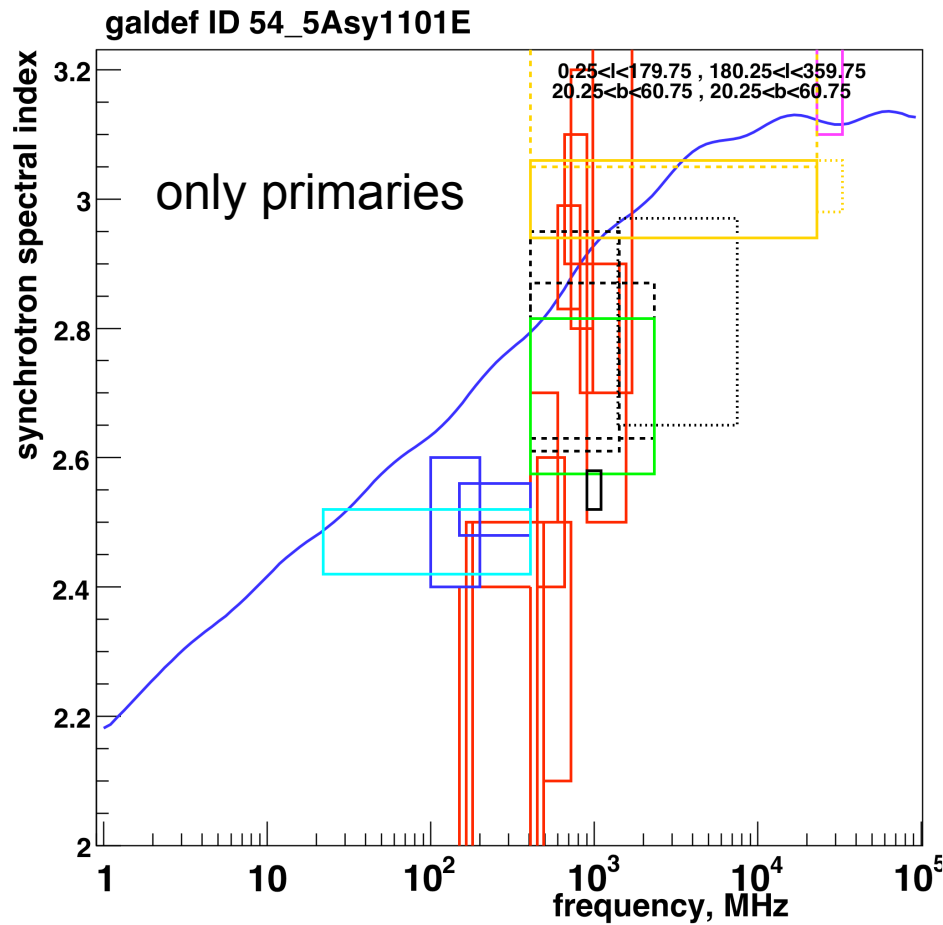


Best Galprop model with secondaries e- e+



Spectral index

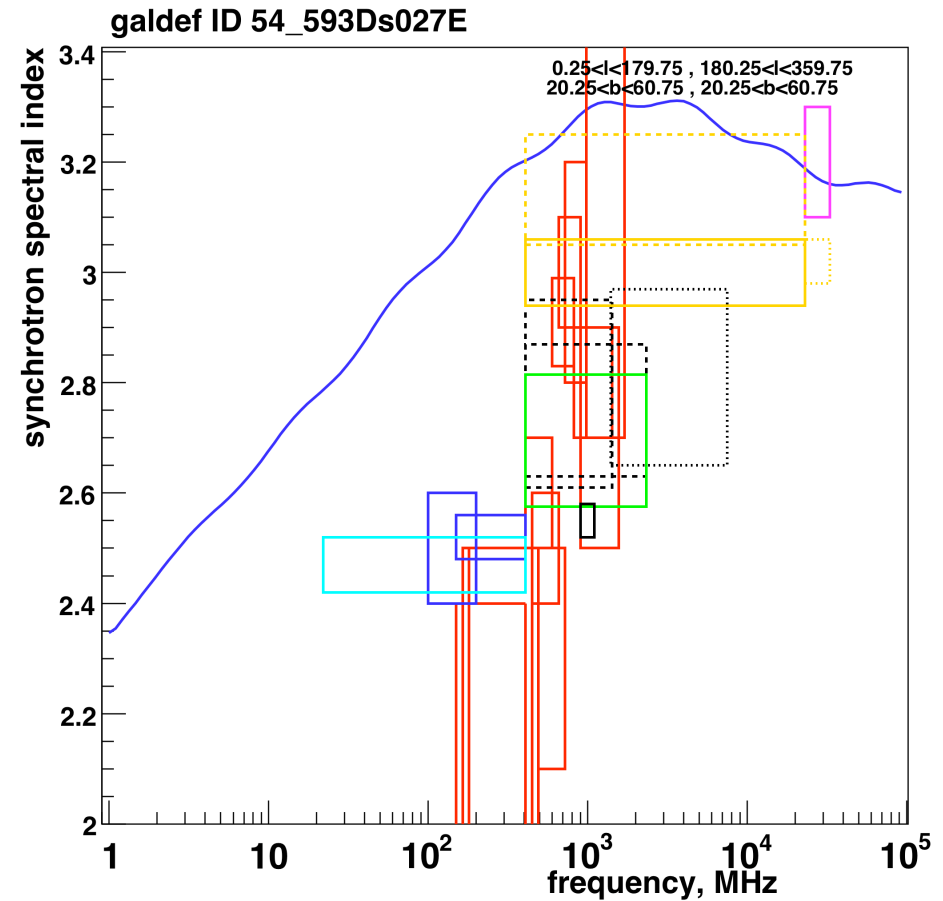
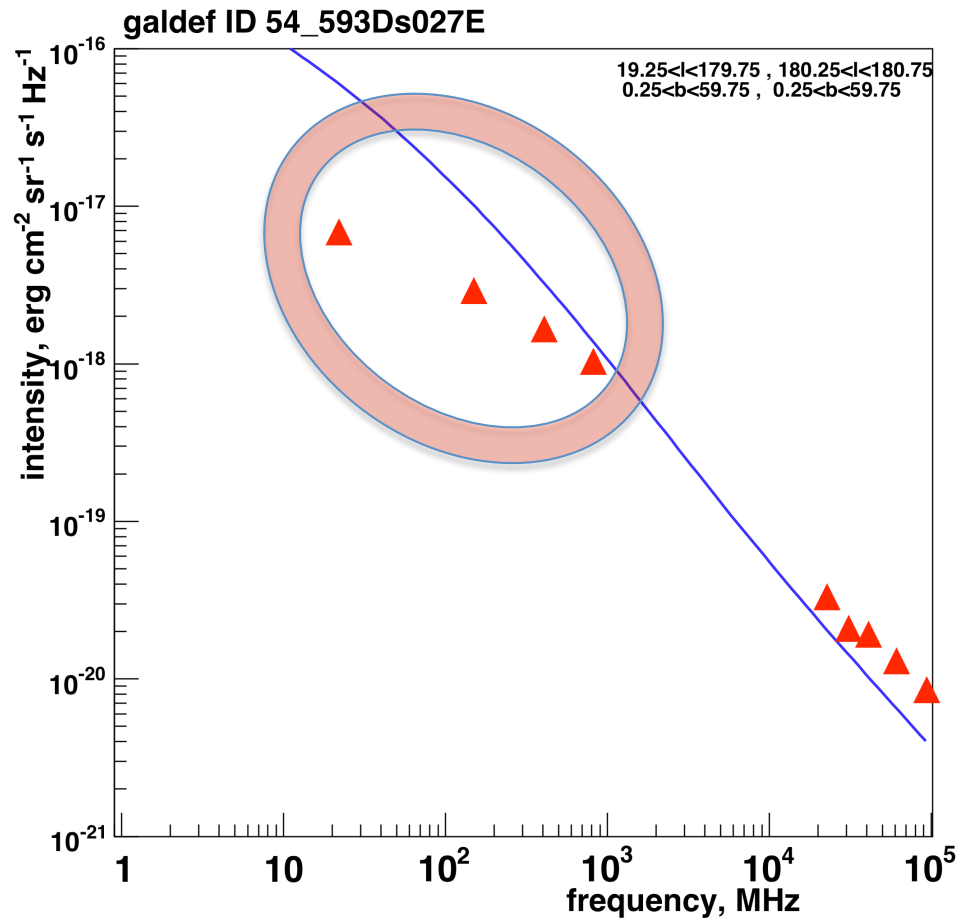
Spectral index $\sim 2 + (\gamma - 1)/2$ after propagation, with γ electron sp. index.



NOT SOLVED: THE SPECTRAL INDEX OBTAINED BY THE MODEL DOES NOT FIT THE OBSERVATIONS!

Evidence for break on the electron spectrum

An example WITHOUT the break (at 4 GeV) in the injection electron spectrum does not agree with the data



SYNCHROTRON DATA CONFIRM THE NEEDED OF A BREAK IN THE INJECTION ELECTRON SPECTRUM

Discussion

- Comparison of B models with data:
 - Tinyakov & Tkachev (2002) model does not match latitude and longitude profiles
 - Evidence of no radial dependence of B regular
 - A toroidal field with parameters as in Sun et al. 2008 does not give much contribution to the synchrotron emission.
 - Miville-Deschenes et al. 2008 model does not agree with synchrotron latitude profiles.
- One of the best models for galprop was defined
- Importance of secondary electrons and positrons
- Not solved: the Spectral index obtained by the model does not fit the observations below 400 MHz
- Evidence of the need for a break in the injection electron spectrum