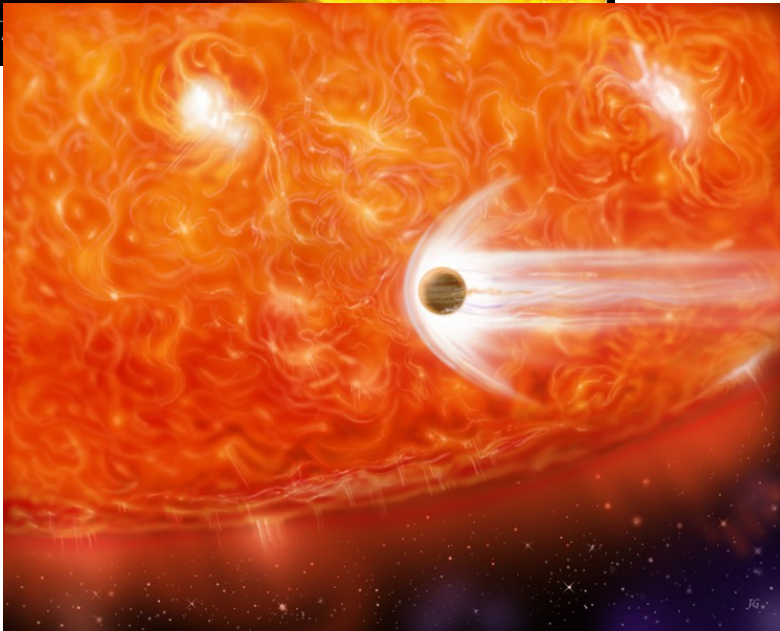
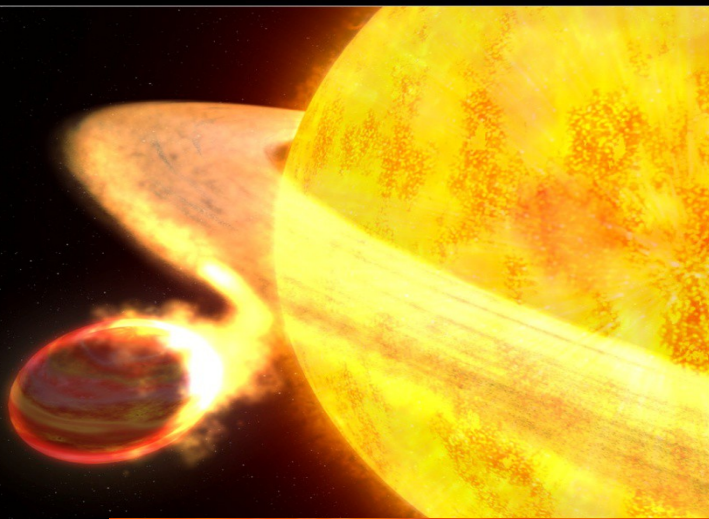
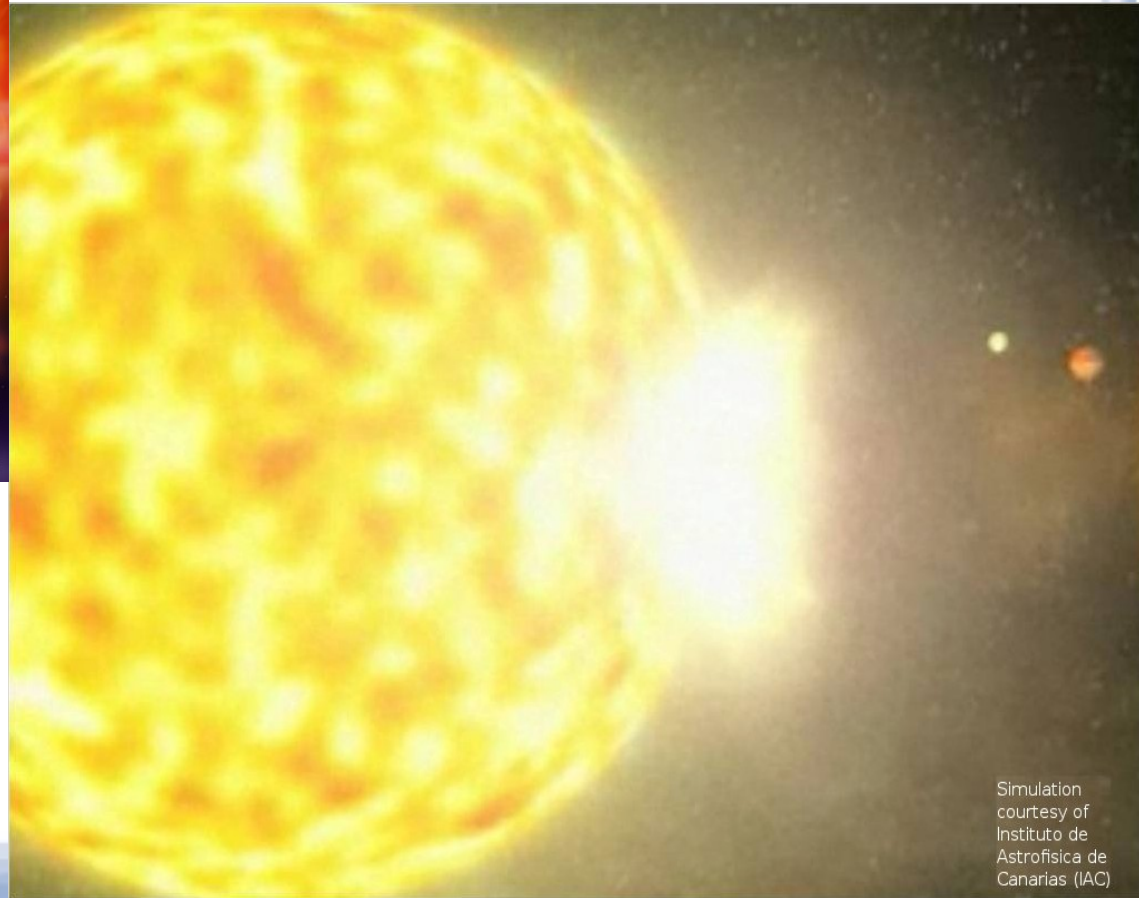


# Planet Flow, Not Weak Tidal Evolution, Produces Excess of Short-Period Planets



**Stuart F. Taylor**  
Job Seeking  
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Planet occurrence of giant and medium planets show an inner fall off that has a power index close to that produced by tidal migration for eccentricity of zero.

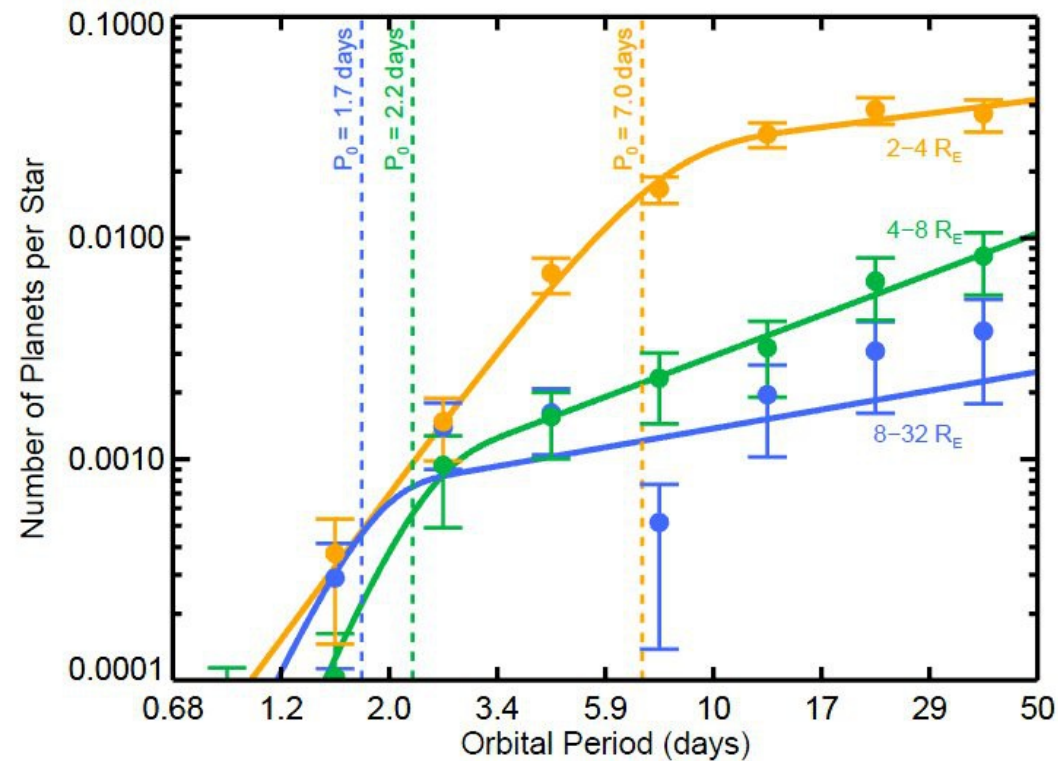
(“Planets” includes “planet candidates”, throughout)

Above: Distribution of Kepler candidates with fit by Howard et al. (2011; H12). The slope gives the power law index (PLI).

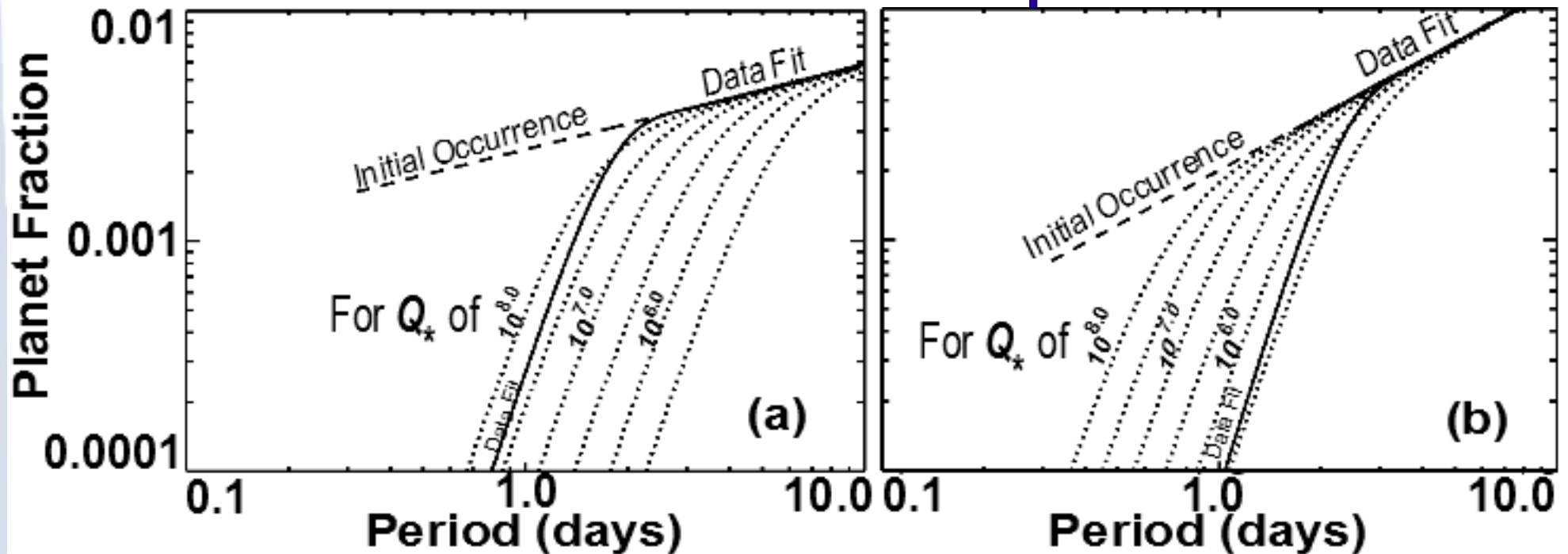
Largest planets (Jupiters:  $8-32 R_{\text{earth}}$ ): Inner PLI matches expected distribution for planets undergoing tidal migration,  $13/3$ .

Medium planets (Neptunes:  $4-8 R_{\text{earth}}$ ): Inner PLI matches expected distribution for planets in range,  $13/3$ . However, the turnover point is further out.

Small(er) planets (Super earths:  $2-4 R_{\text{earth}}$ ): Inner PLI lower than  $13/3$ . Fall off is likely too far out, so distribution may be primordial.



# Occurrence distribution power index



**Giant** planets, summed for 8 to 32  $R_{\oplus}$  **Medium** planets, summed 4 to 8  $R_{\oplus}$

Data compared to model fall off for sum of giant planets of 100 to 2000  $M_{\oplus}$  and 10 to 100  $M_{\oplus}$  at representative age of 4.5 Gigayears.

- Consistent with fall in for giant and medium planets (above).
- but too low for sub-Neptune planets.
  - The difference could be a flow of giant planets. –

# The values: Tidal migration

Tidal migration rate from Jackson et al. (2009) gives a  $P$  dependence on  $t$  to the power of  $P^{-13/3}$ , after converting to period  $P \propto a^{3/2}$

$$\frac{1}{a} \frac{da}{dt} = - \left( \frac{63}{2} (GM_*^3)^{1/2} \frac{R_p^5}{Q'_p M_p} e^2 + \frac{9}{2} (G/M_*)^{1/2} \frac{R_*^5 M_p}{Q'_*} \left( 1 + \frac{57}{4} e^2 \right) \right) a^{-13/2}$$

Plotting the planet distribution  $d \log f(P)/d \log P$  gives a power law index of 13/3 due to its dependence on  $dt/da$ .

Power index of 13/3: Tidal migration due to tides on the star (“stellar TM”) for circular orbits.

Lower power index would result for eccentricity increasing as a function of semi-major axis.

# The values: Kepler planet distribution

H12 find values of a little over 4 for the PLI (the slope of the log-log distribution) of the closest Kepler candidates, where they fit to

$$\frac{df(P)}{d \log P} = k_P P^\beta \left(1 - e^{-(P/P_0)^\gamma}\right)$$

and obtain these best fits:

$R_p$ ( $R_\oplus$ )	$k_P$	$\beta$	$P_0$ (days)	$\gamma$
2-4 $R_\oplus$	$0.064 \pm 0.040$	$0.27 \pm 0.27$	$7.0 \pm 1.9$	$2.6 \pm 0.3$
4-8 $R_\oplus$	$0.0020 \pm 0.0012$	$0.79 \pm 0.50$	$2.2 \pm 1.0$	$4.0 \pm 1.2$
8-32 $R_\oplus$	$0.0025 \pm 0.0015$	$0.37 \pm 0.35$	$1.7 \pm 0.7$	$4.1 \pm 2.5$
2-32 $R_\oplus$	$0.035 \pm 0.023$	$0.52 \pm 0.25$	$4.8 \pm 1.6$	$2.4 \pm 0.3$

As  $P \rightarrow 0$ , this equation goes towards  $P$  having a power law of  $\beta+\gamma$  :

$$d \log f(P)/d \log P \rightarrow k_P P^{\beta+\gamma}$$

The power law values  $\beta+\gamma$  for the three planet radii ranges (in  $R_{\text{earth}}$ ) are:

$$\mathbf{8-32 R_{\text{earth}} \quad \beta+\gamma = 4.5 \pm 2.5}$$

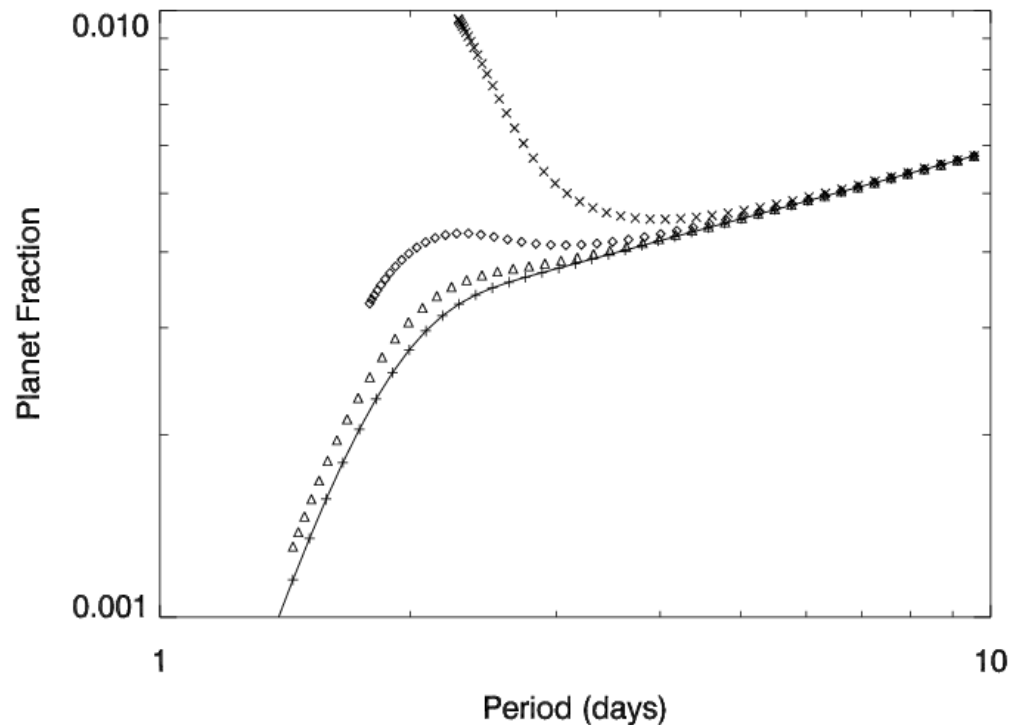
$$\mathbf{4-8 R_{\text{earth}} \quad \beta+\gamma = 4.8 \pm 1.3}$$

$$\mathbf{2-4 R_{\text{earth}} \quad \beta+\gamma = 2.9 \pm 0.4}$$

# Pileup can be produced by flow

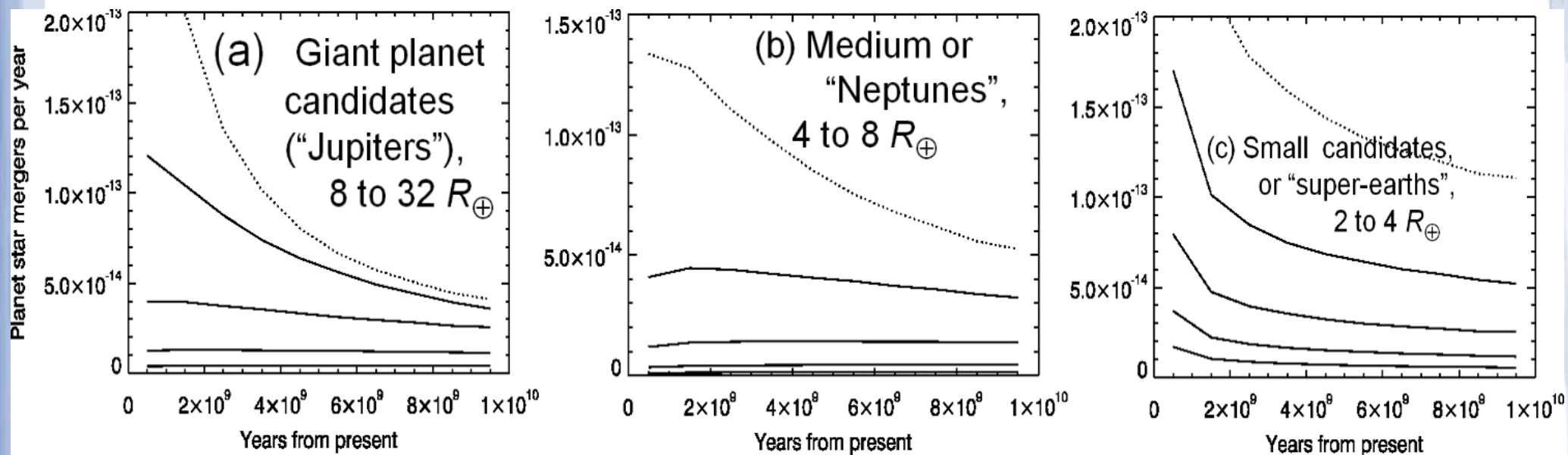
Taking an initial distribution without a pileup (bottom curve) backwards in time gives a pileup. Modeling backwards for three tidal dissipation strengths gives limit on  $Q'_{star}$ .

Top (crosses) shows  $Q'_{star} = 10^{6.5}$  would be too strong.  
Middle two curves (triangles and diamonds) show that  $Q'_{star} = 10^{7.0}$  and  $Q'_{star} = 10^{7.5}$  would be reasonable.



# Future infall: Modeling Fit Distribution

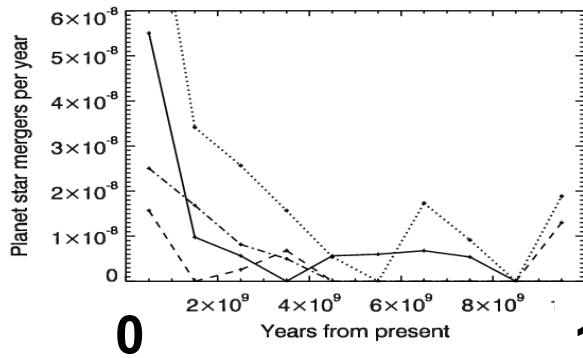
Rate of calculated future infall for giant, medium, and (relatively) small planets. Rate given for  $Q'_{star}$  values of  $10^{6.5}$  (top line, dotted) to  $10^{8.5}$  in increments of  $10^{0.5}$ .



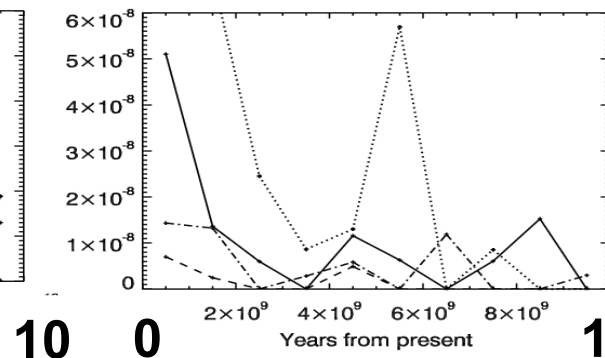
Planet infall should remain constant, other than the stars in this population will age, so reject for  $Q'_{star}$  values that make "now" different from future.

- Not consistent with same tidal dissipation strength
- The difference could be made up by an increasing flow new giant planets

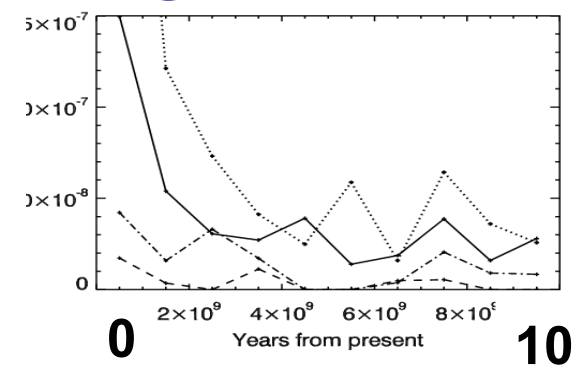
# Future infall: Modeling Data



(a) Giant planet candidates  
("Jupiters"),  
8 to 32  $R_{\oplus}$



(b) Medium or  
"Neptunes",  
4 to 8  $R_{\oplus}$



(c) Small candidates,  
or "super-earths",  
2 to 4  $R_{\oplus}$

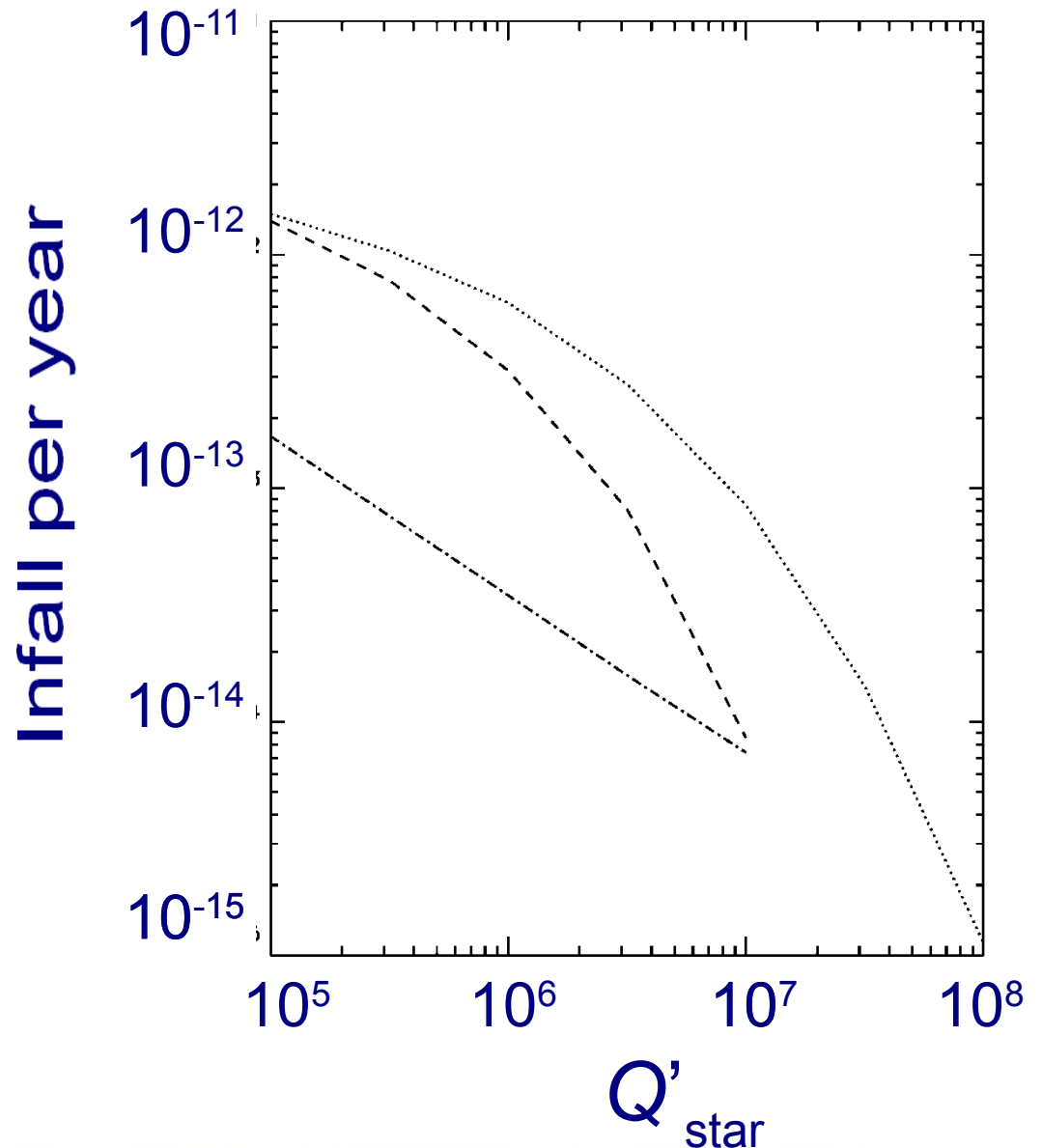
Consistent with results from fit, but noisier.



# Rate of infall

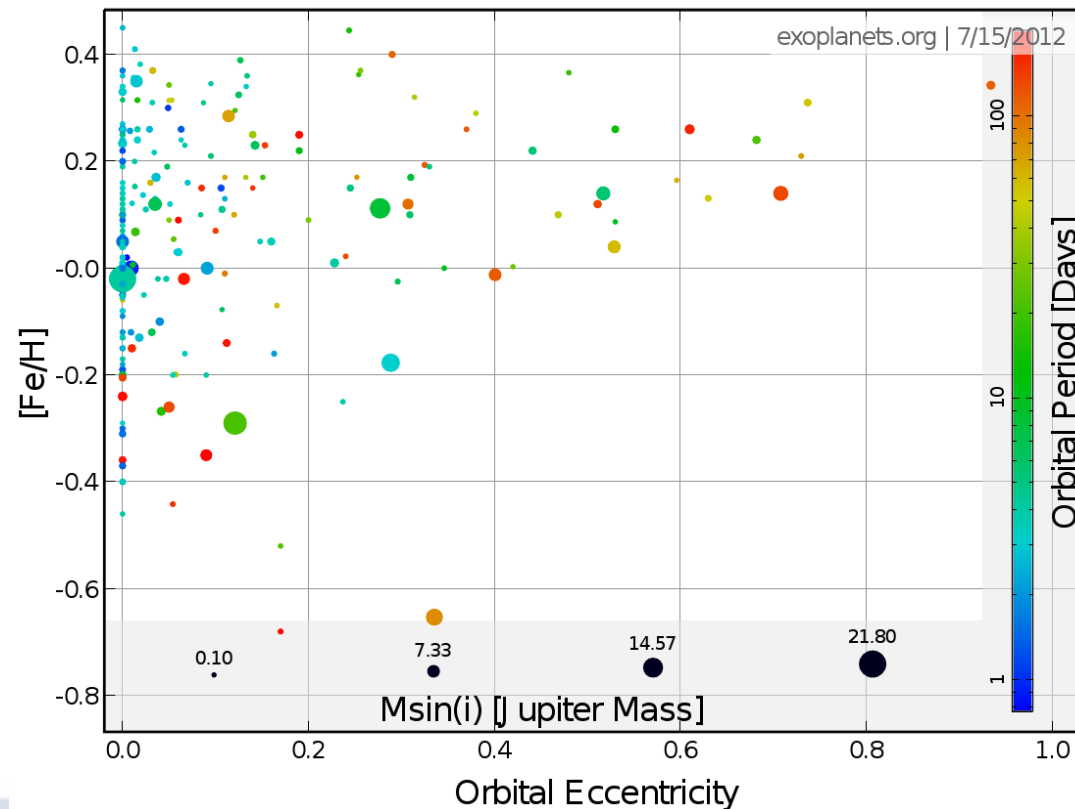
Rate as function of tidal dissipation strength  $Q'_{\text{star}}$ , shown for giant, medium, small planets

- Does not require too many planets: order of 1/1000 stars or less per gigayear



# Correlation of higher Fe/H with higher eccentricity

- Few hot Jupiters in multiplanet systems, more hot Neptunes in multiplanet systems (Fabrycky et al. 2012; Latham et al. 2012)
- Others rule out pollution looking at other element ratios of short period planets



# Future work:

- Watch for period decreases – However, for  $Q'_{\text{star}}$  of  $10^{7.0}$ , the period of WASP-18b will decrease by only 1.3 milliseconds per year.
- Compare the numbers of planets required for infall with eccentric planets and the rates of inward scattering.
- Migration of non-zero eccentricity, including higher order terms.
- Model whether moderate eccentricity could create pileup, and extreme eccentricity could send planets right through pileup.
- Better statistics needed: Follow whether these results hold.
- Fit pile up of giant planets
- Model pollution in stars, first to estimate time of convection to mix away from stellar surface.

# Conclusions

- Excess of shortest period giant planets would require a different tidal dissipation strength than medium planets if no new planet supply.
- Flow of planets could also explain pile up of giant planets:
  - Possible that more giant planets migrate in
  - Possible that smaller planets migrate more quickly
- Is migration of one planet correlated with planet/star mergers of other planets?
- Posting on astro-ph appeared today.