

# X-ray spectral fitting in two dimensions

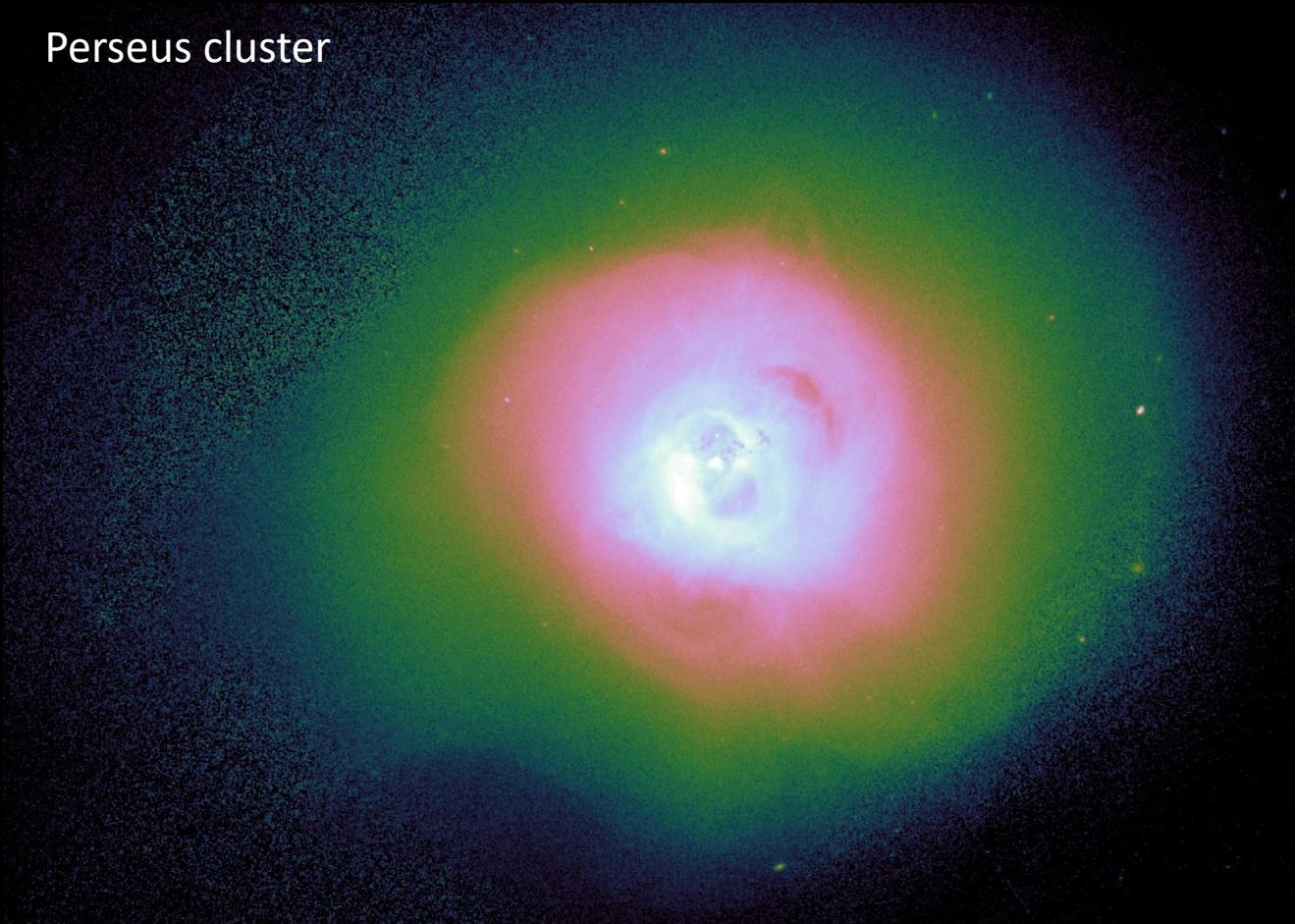
Jeremy Sanders, MPE

Note: not covering more specialised topics, such as RGS grating analysis

Extended sources can be complex

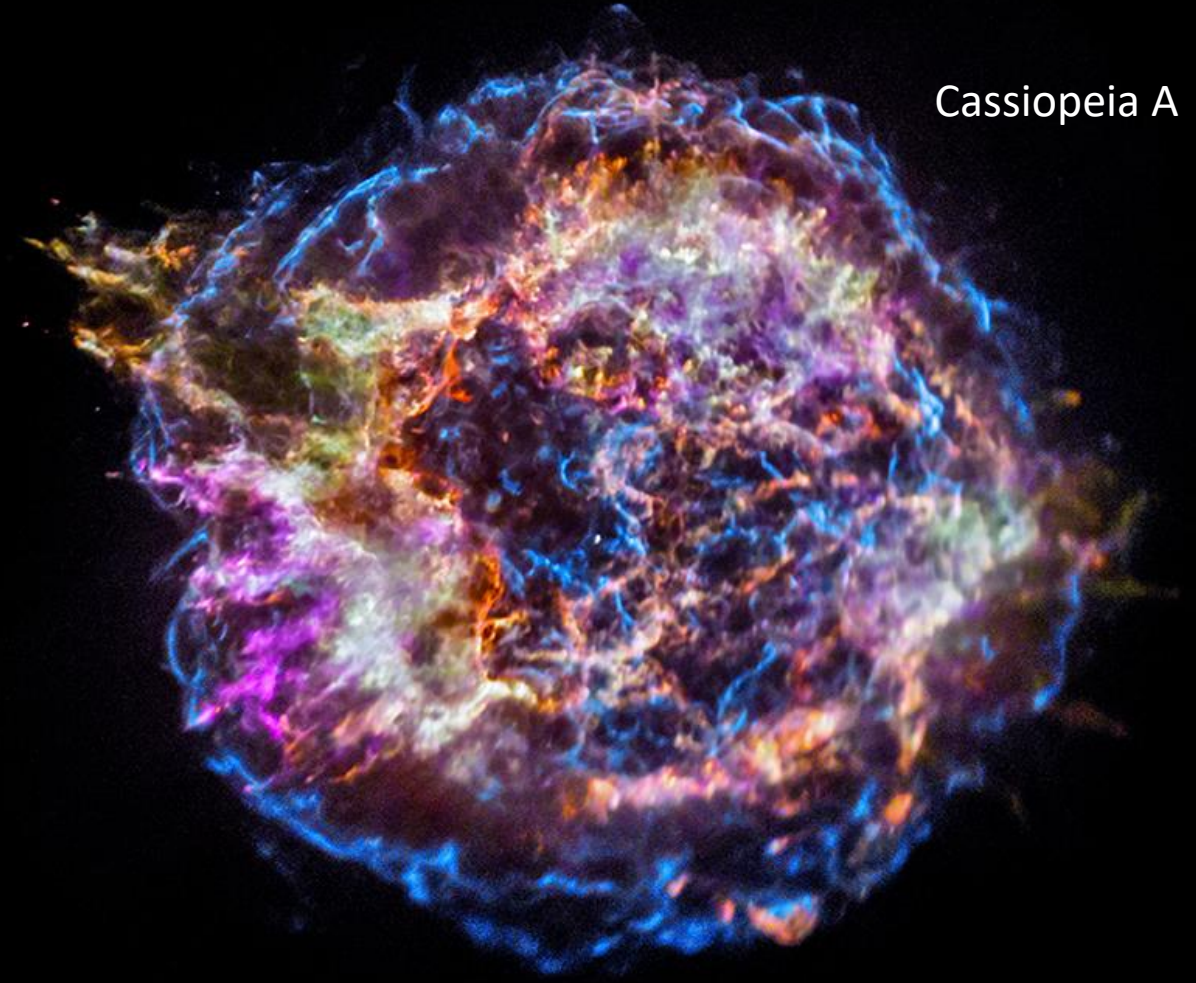
*How do you interpret the X-ray data and obtain information about the physics?*

Perseus cluster



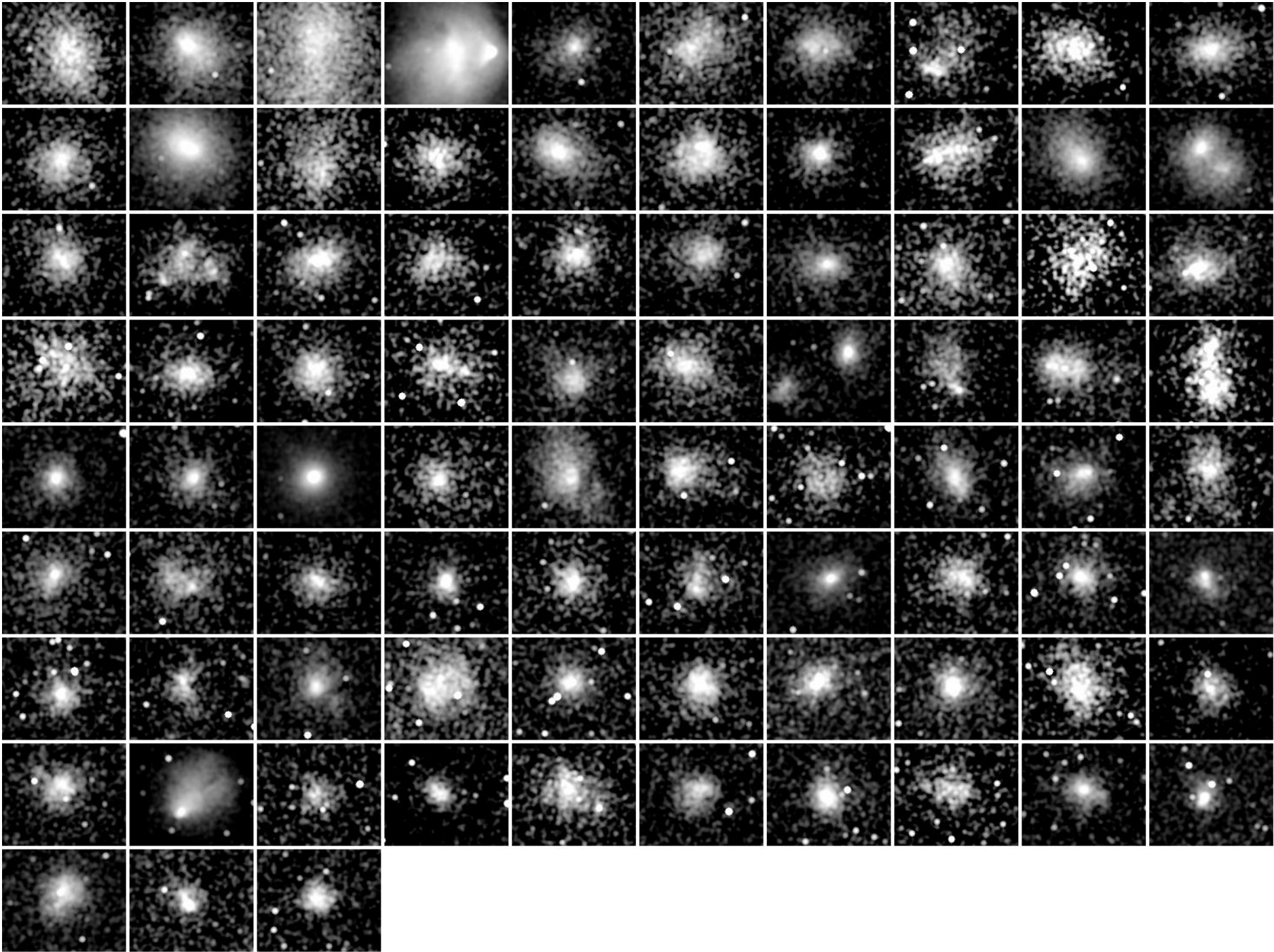
Galaxy cluster: want temperature, metallicity, density, pressure, entropy, (velocities)...

Cassiopeia A



Supernova remnant: metals, ionization timescales, velocities...

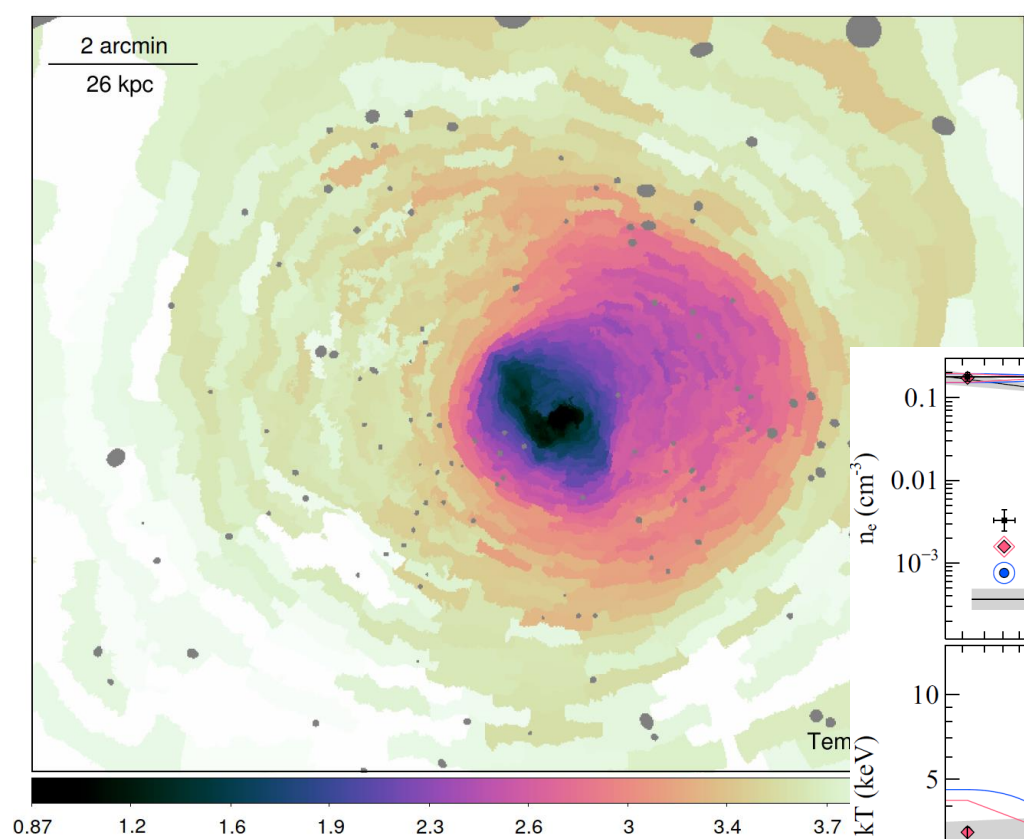




Data quality often poorer!

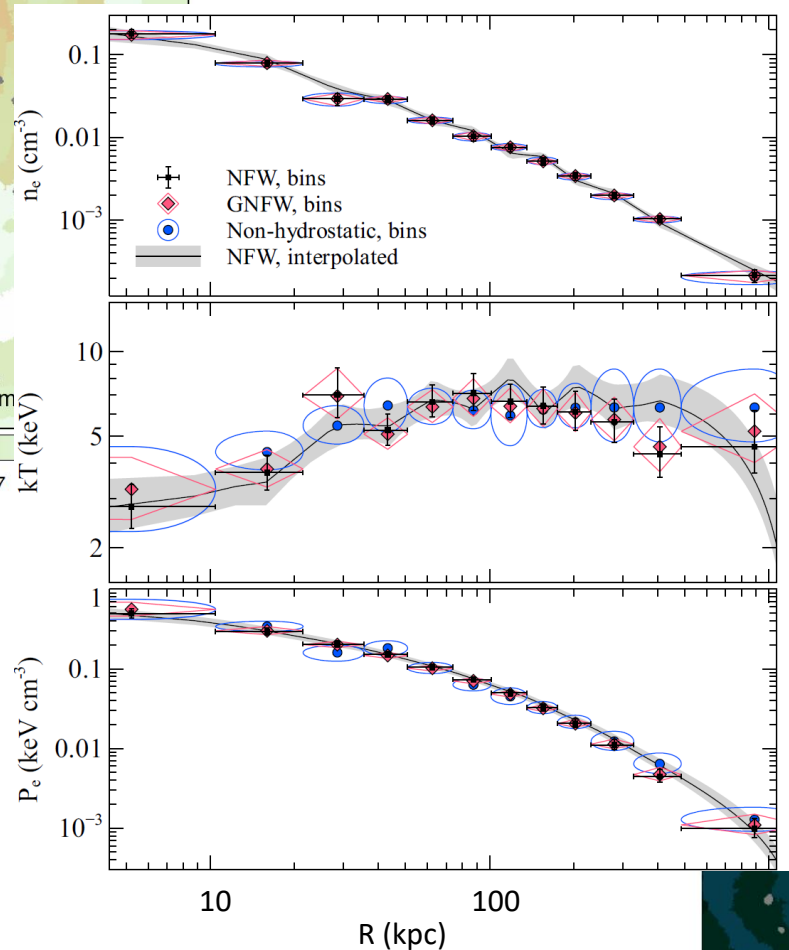
SPT sample of clusters observed by Chandra

For eROSITA, the typical cluster or group will have many fewer counts than this



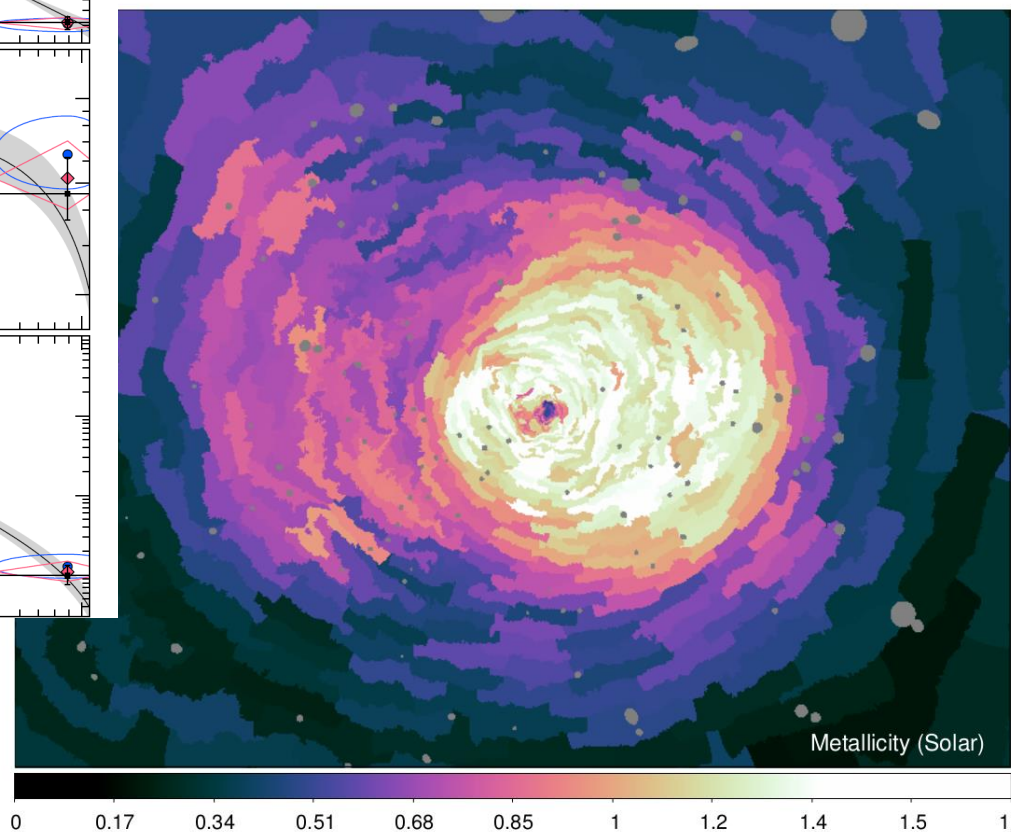
*Would like maps and profiles of relevant physical quantities*

Often no unique way to do this, unless you have a realistic 3D model!



Results are sets of maximum likelihood best fits!

Take care when fitting other models to them, particularly for deprojected profiles



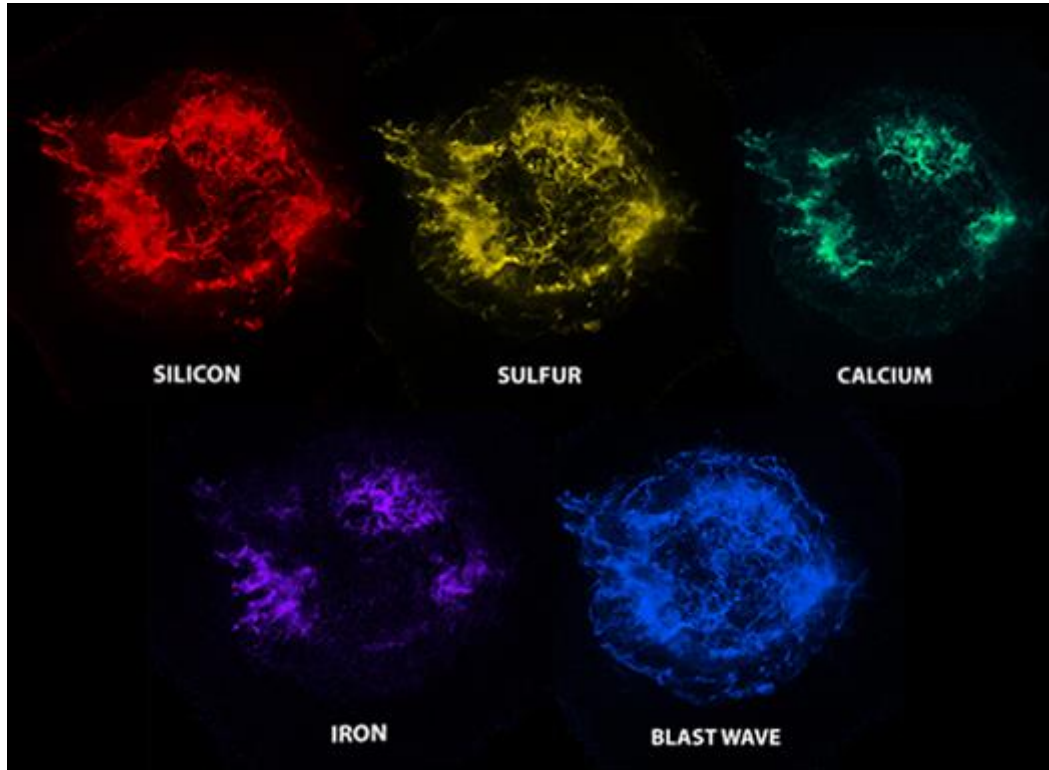
# Problems in interpreting 2D data

- How do you choose which regions to examine, or do you try to fit some sort of global 3D model?
- Do you want maps or radial profiles?
- How do you account for 3D→2D projection?
- Which models do you fit? (model selection)
- Instrumental or modelling issues
  - PSF, background, vignetting, response, chip gaps
  - Point source removal / modelling

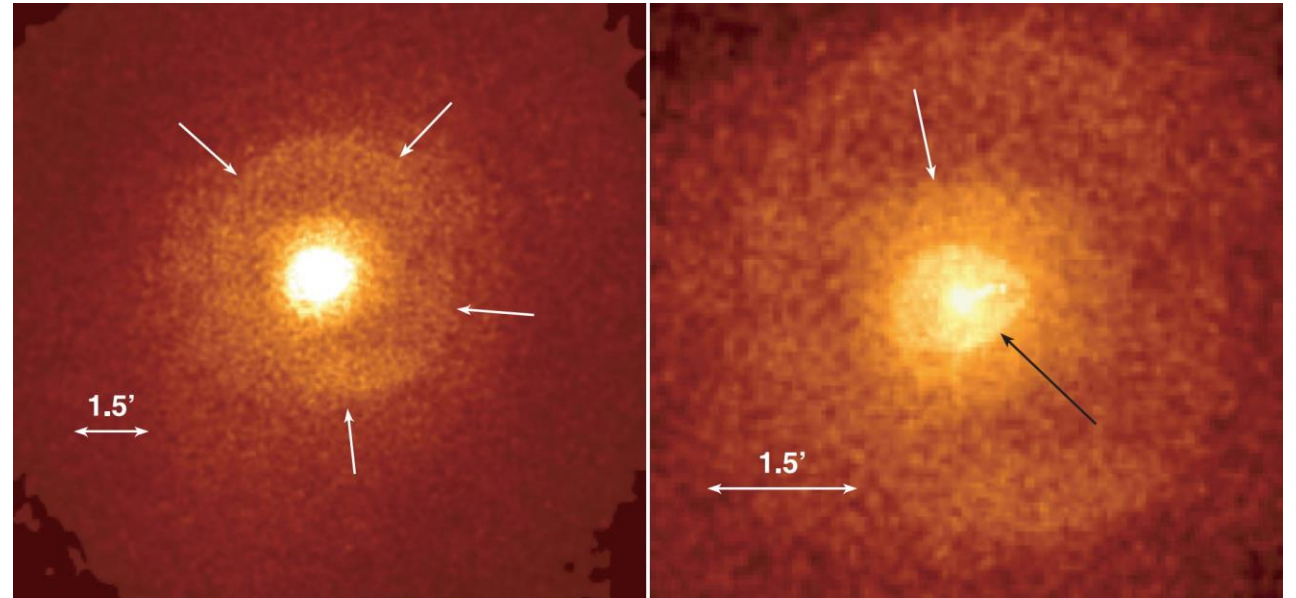


# Avoid spectral fitting altogether?

- Make narrow- or appropriate-band images to examine physics
- In future likely more common-place (e.g. X-IFU on Athena)



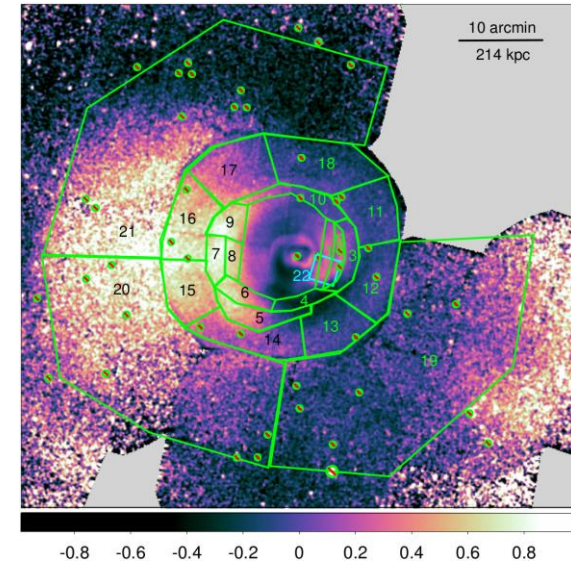
Narrow band images of Cas A (Chandra web site)



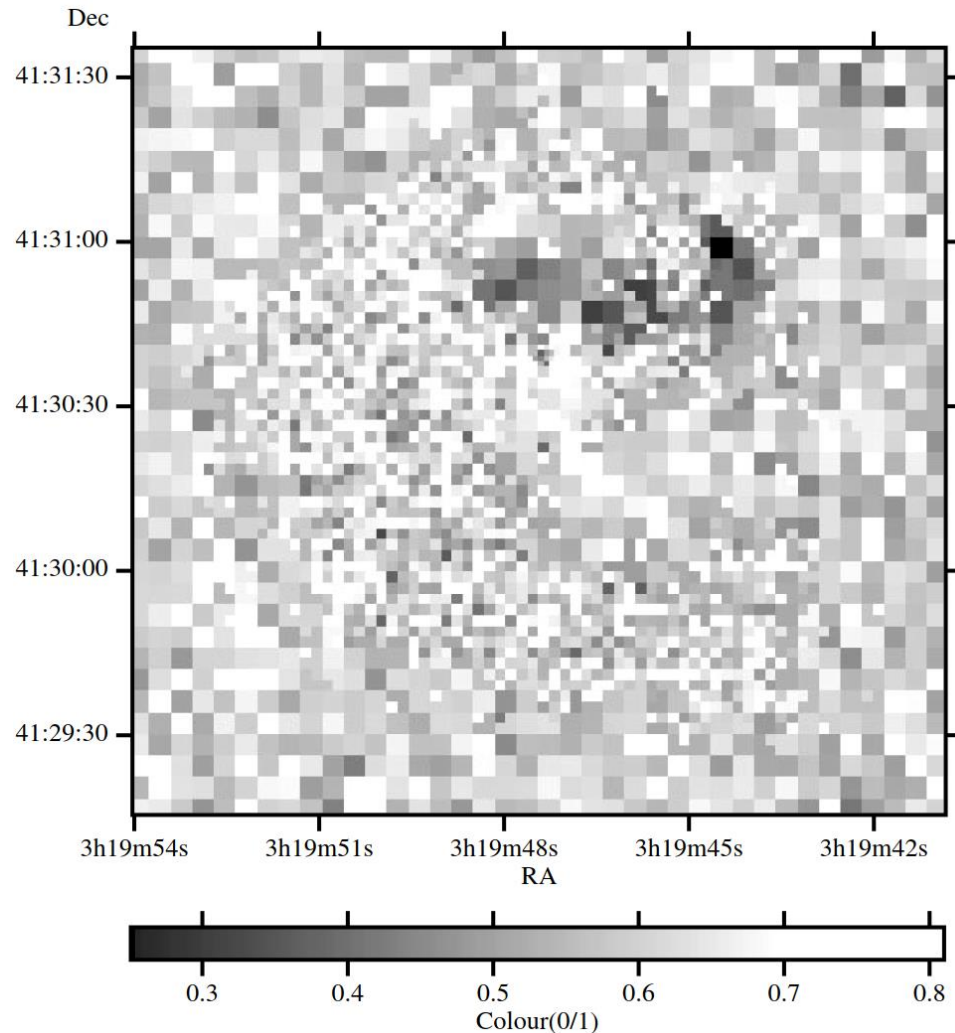
High-energy pressure-sensitive image of M87 (Forman et al. 07)

# Region choice

- We want to do spectral fitting and make 2D maps
- What regions do we choose?
  - Independent spatial regions – e.g. choose by hand, adaptive binning, Voronoi tessellation, contour binning...
  - Overlapping regions
- Independent regions are easier to compare
- We can extract spectra from each region, fit and create maps from the parameters



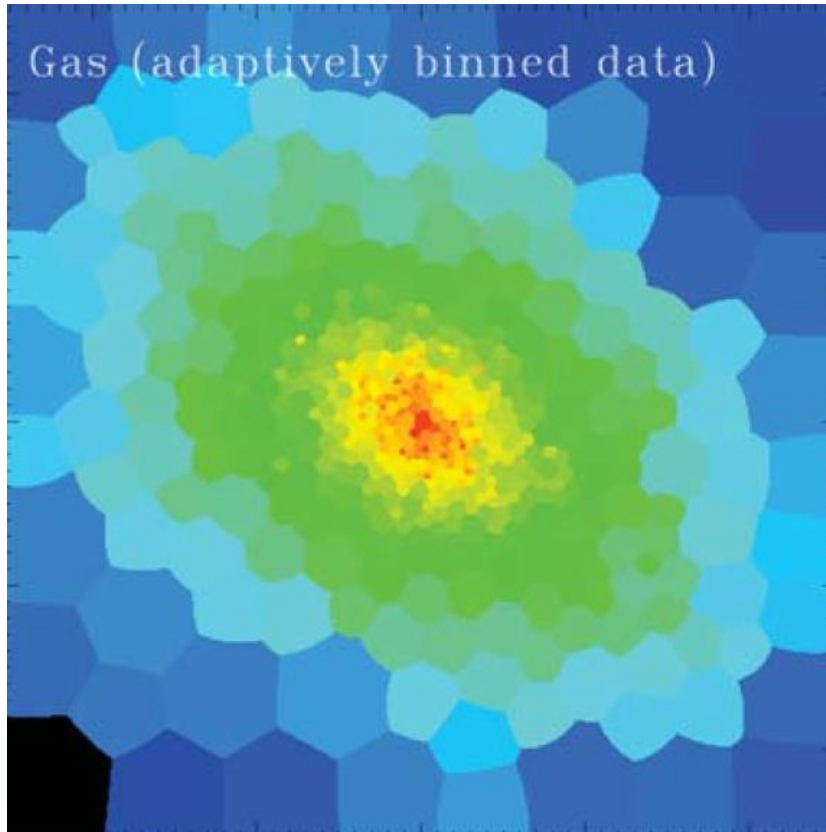
# Adaptive binning (aka quadtree)



- Sanders & Fabian (2001)
- Bin brightest pixels first
- Double bin size until fractional error on counts (or count ratio) is reached
- Negative: ugly, big steps in bin size
- I probably wouldn't use this any more

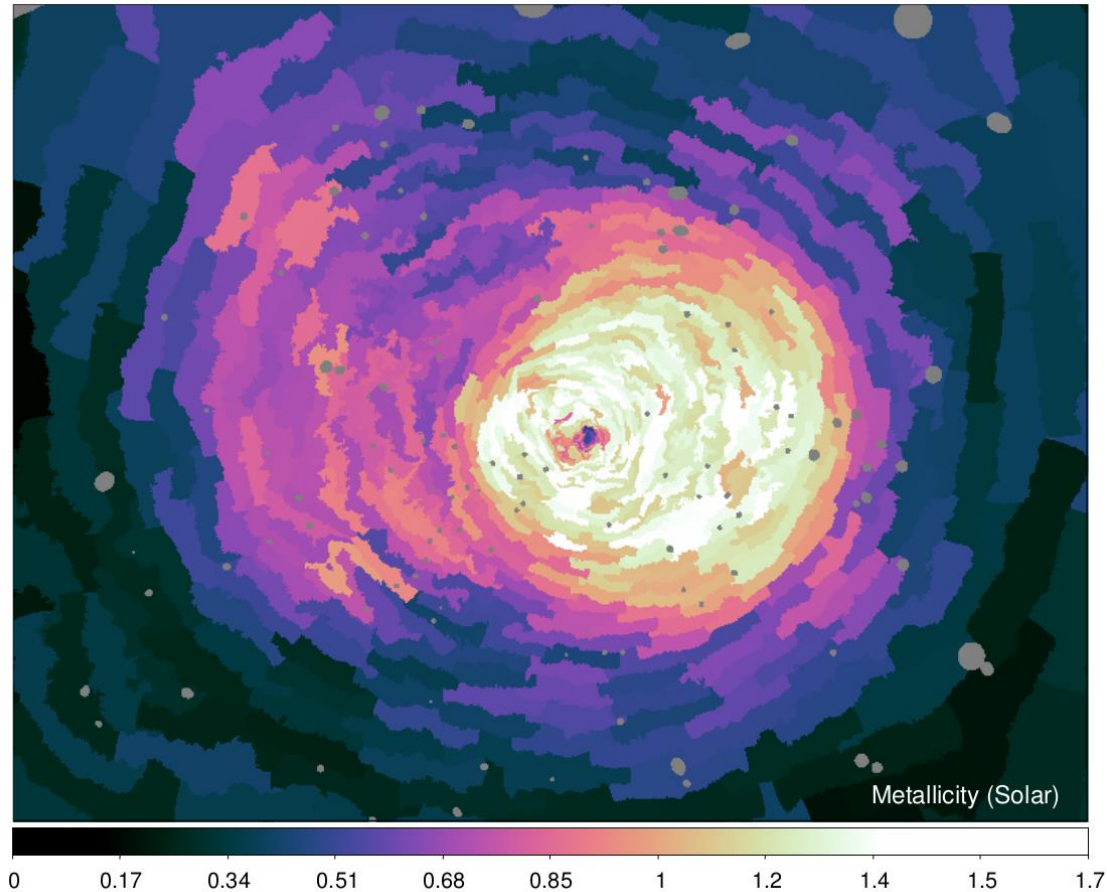


# Voronoi tessellation adaptive binning



- Diehl & Statler (2006)
1. “Accrete” bins from brightest remaining region to be above a S/N threshold
  2. Calculate centroids of bins
  3. Perform Voronoi tessellation on centroids
  4. Repeat 2.
- Positive: pretty unbiased choice of bins around a S/N value
  - Positive: spatially-compact bins
  - Negative: non-optimal shape

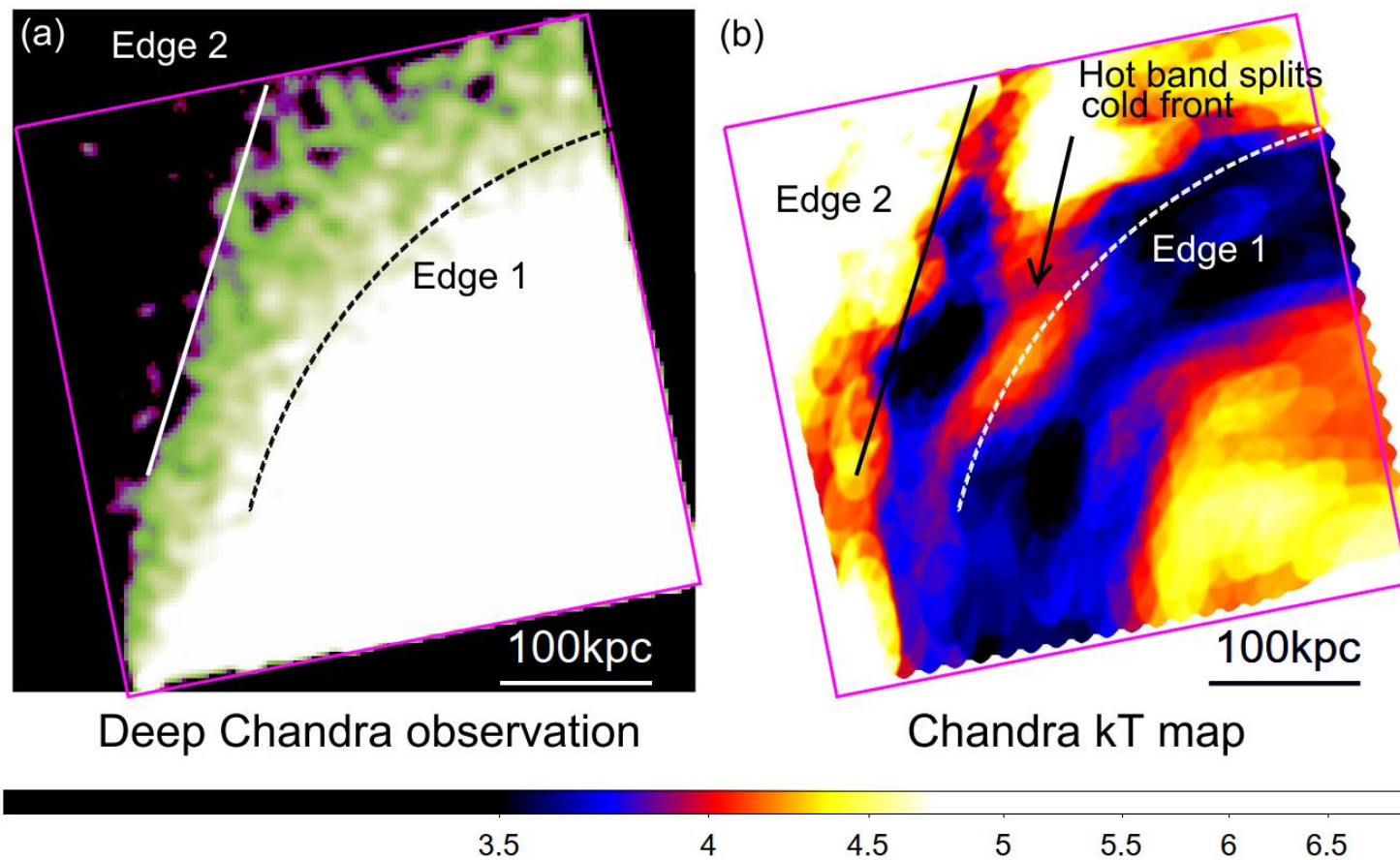
# Contour binning



- Sanders (2006) – assumes spectral properties follow image
- Take adaptively smoothed image
- Grow bins along surface brightness contours in map until S/N threshold reached
- Geometric constraints factor to stop elongation of bins
- Positive: Great if spectral properties follow image, and can look nice
- Negative: Possible bias in assuming this

# Non-independent binning

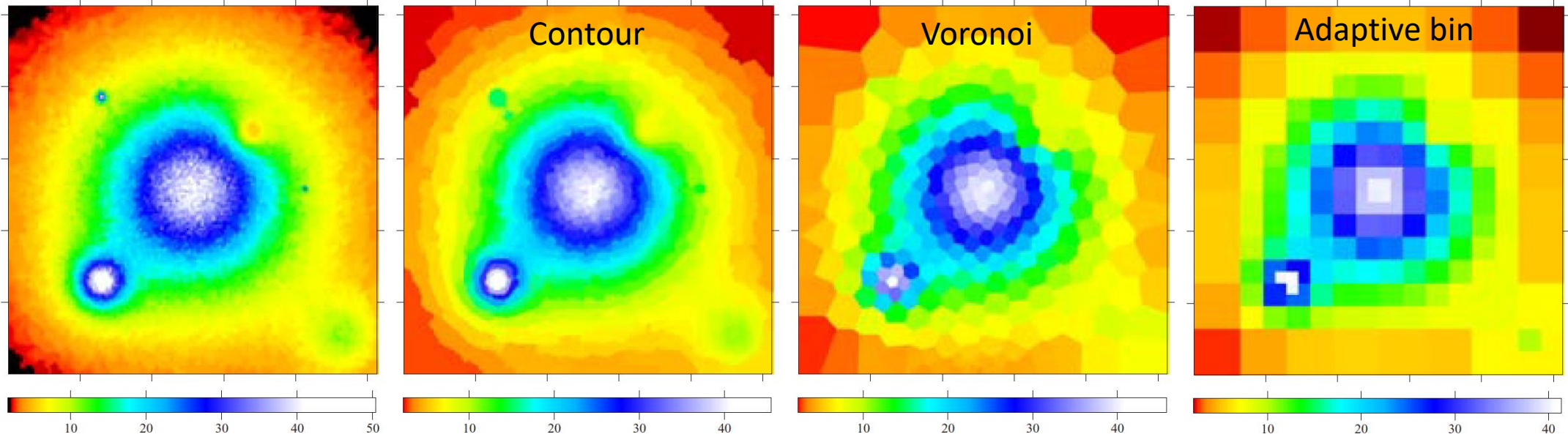
- Overlapping circles or ellipses, with size chosen to give S/N ratio, e.g.
  - O’Sullivan et al. (2014)
  - Walker et al. (2018)
- Smoother maps
- More statistically difficult to interpret fluctuations



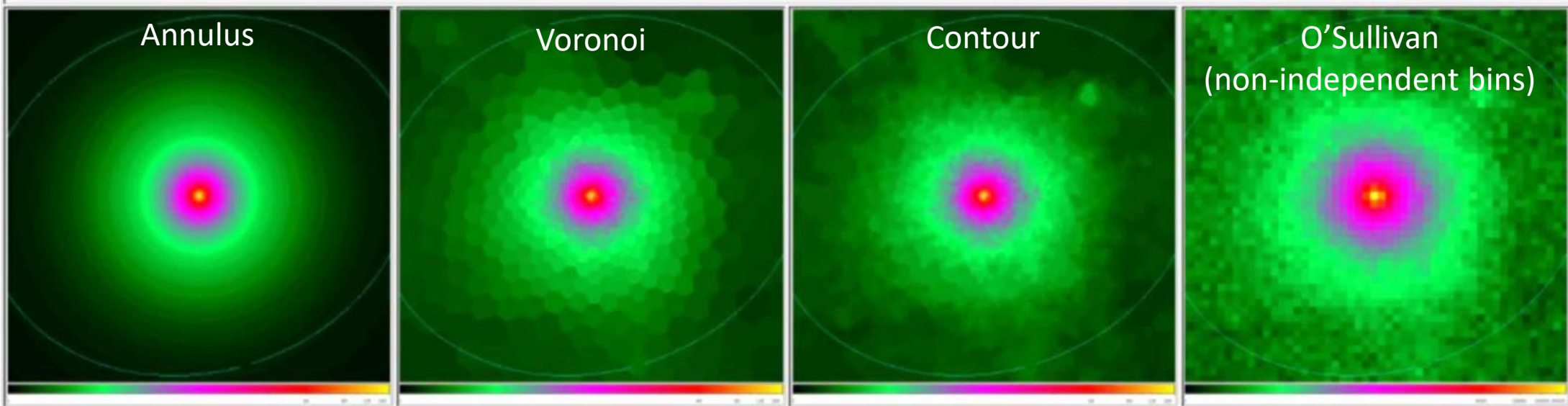


# Comparison

S/N=100 threshold on model simulated data (Sanders 2006)

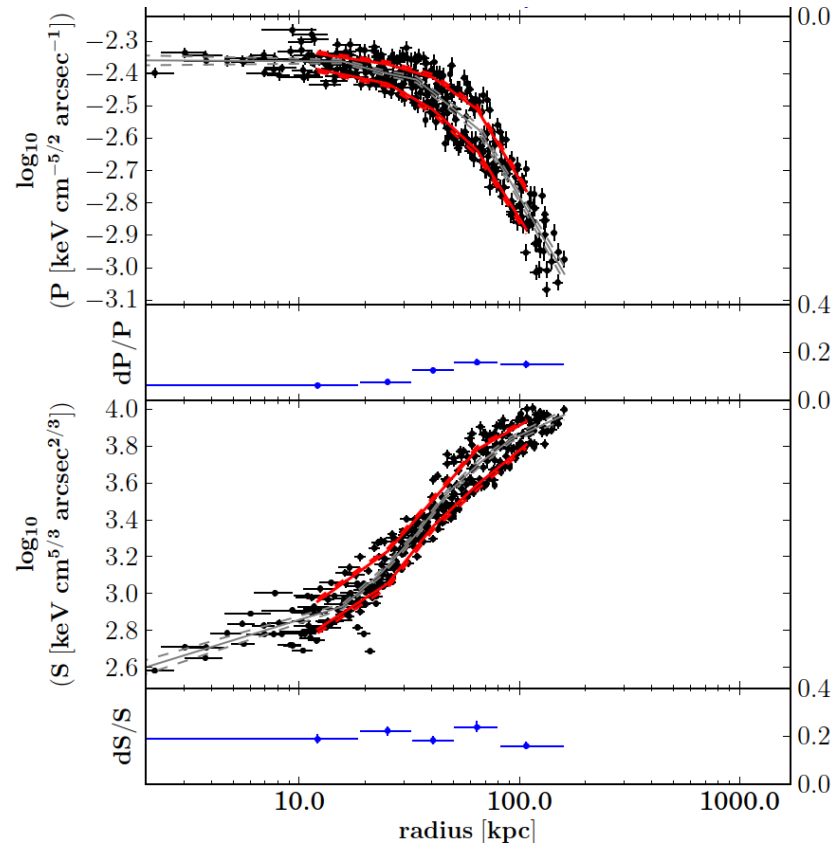


Binned images of NGC 4649 (Kim et al. 2019)

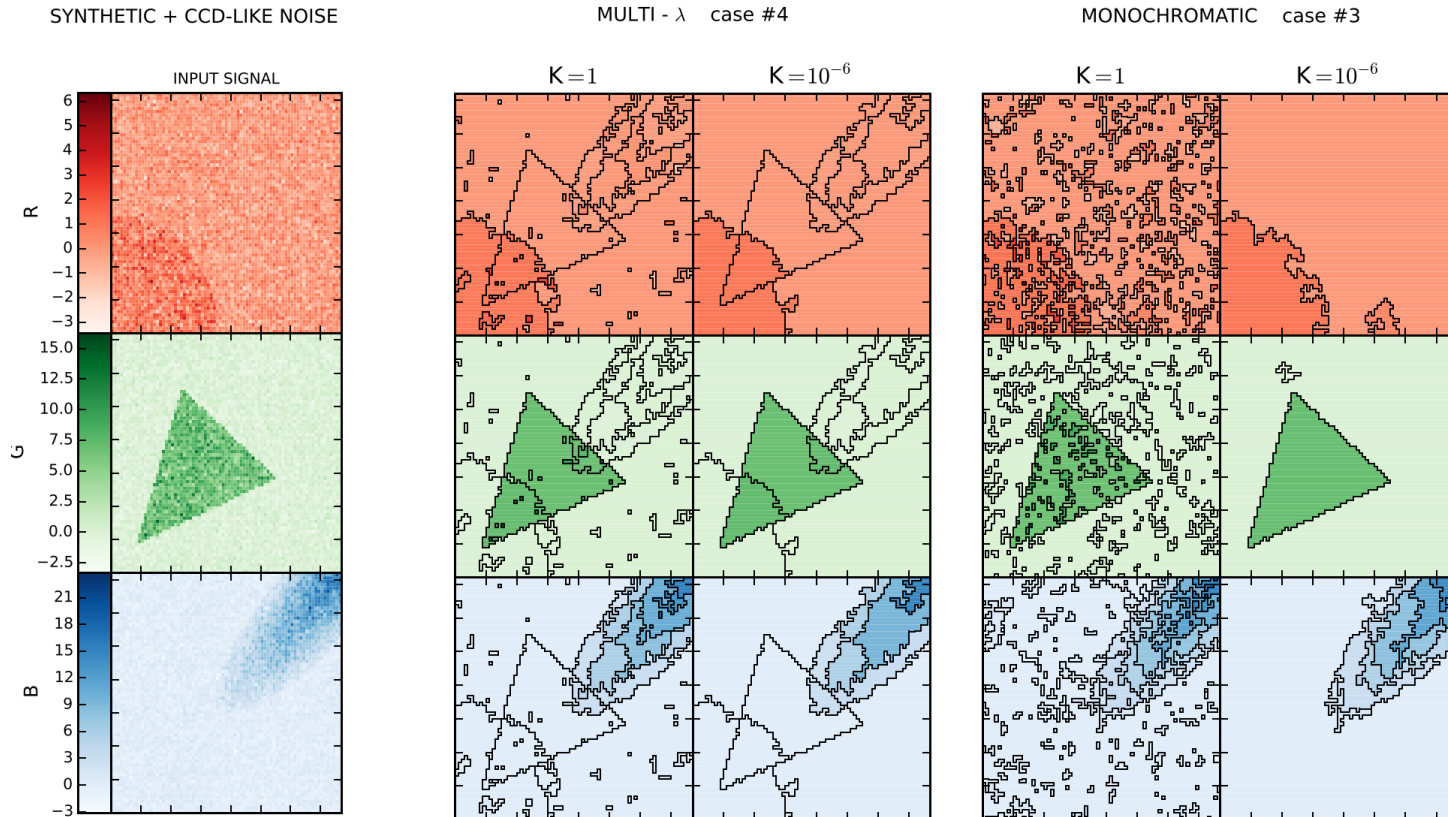


# Mapping difficulties

- Not obvious how to choose bin size for optimal mapping
- Statistical significance of physical parameters hard to see in maps
  - Can use radial profiles to help (e.g. Hofmann et al. 2016)



# An alternative

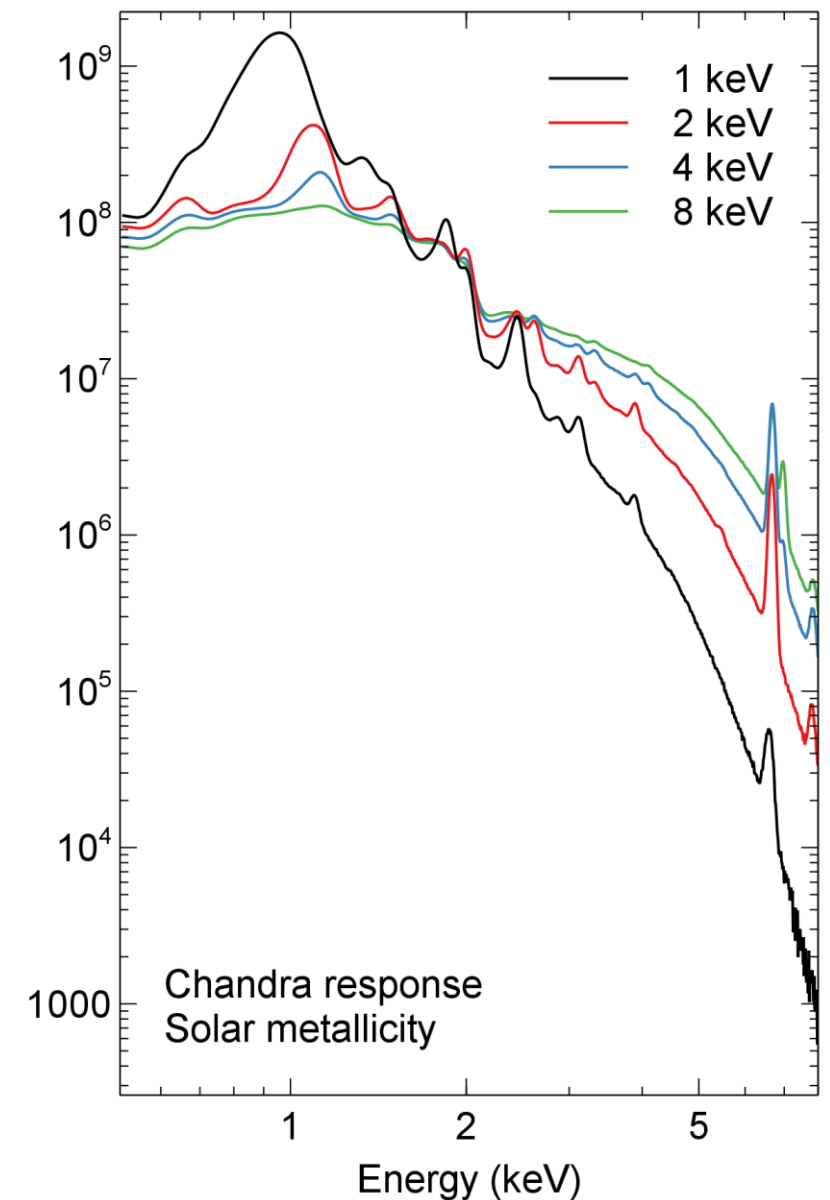


- BATMAN: Bayesian Technique for for Multi-Image Analysis (Casado+17)
- Merge regions which are consistent with carrying same region
- Not aware of any X-ray analyses using this
- Issue: huge possible parameter space for regions, so need heuristics



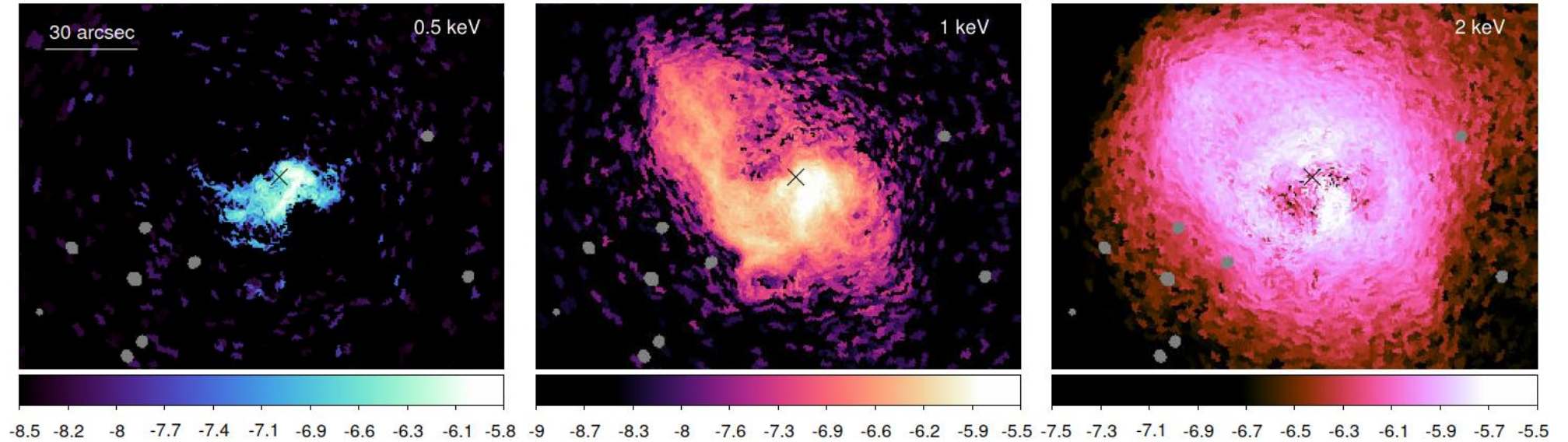
# Models

- For galaxy clusters, usually thermal, collisionally-ionized plasma (APEC or MEKAL/SPEX), with Galactic absorption is assumed
  - Parameters: temperature, metallicities (assume Solar or not), redshift, emission measure (can be used to derive density, given geometry)
  - Possible two-component fits in cool cores
- More complex in SN remnants and galaxies
  - Stronger velocities
  - Non-ionization equilibrium
  - Non-thermal components (e.g. binaries in galaxies)

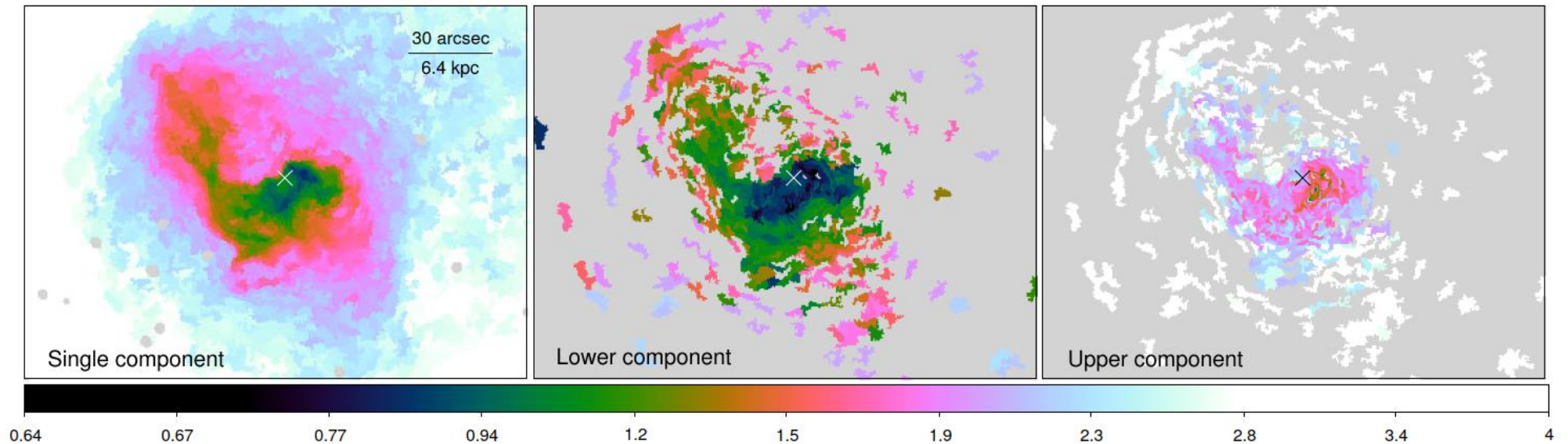


# More complex models: Centaurus

Multi-component model with fixed temperatures, showing normalisation of each component (Sanders+17)

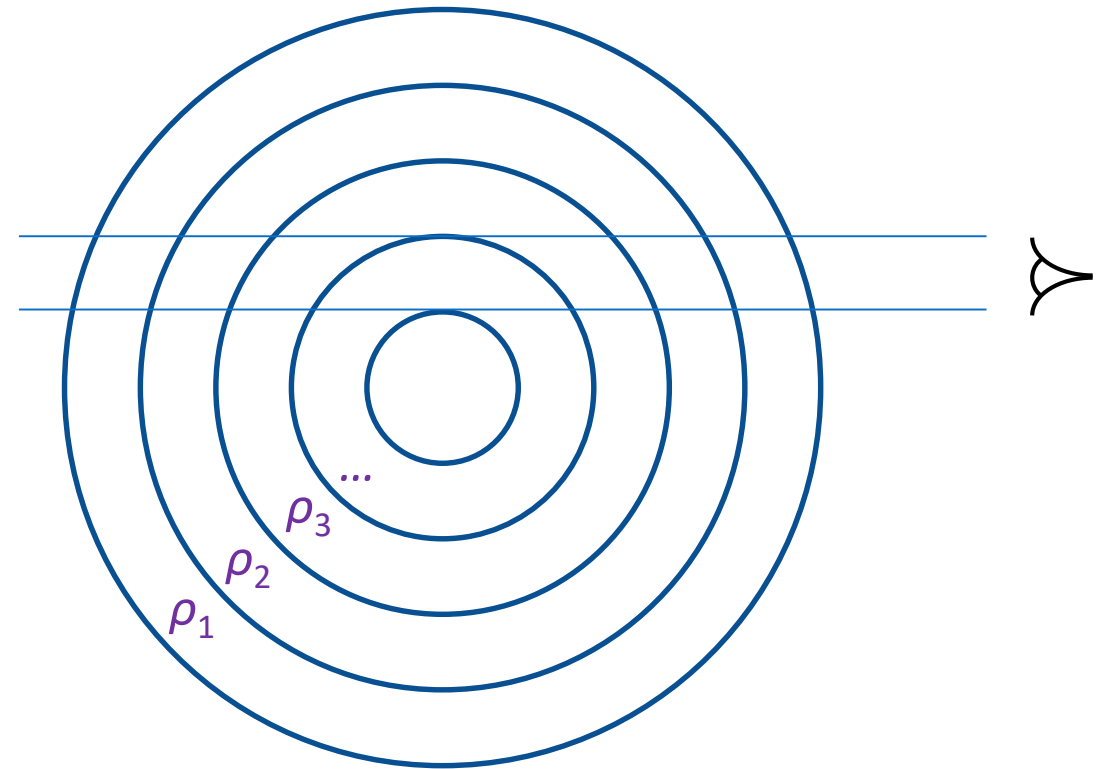


Model with a range of temperatures, using simulations to decide statistical significance



# Projection

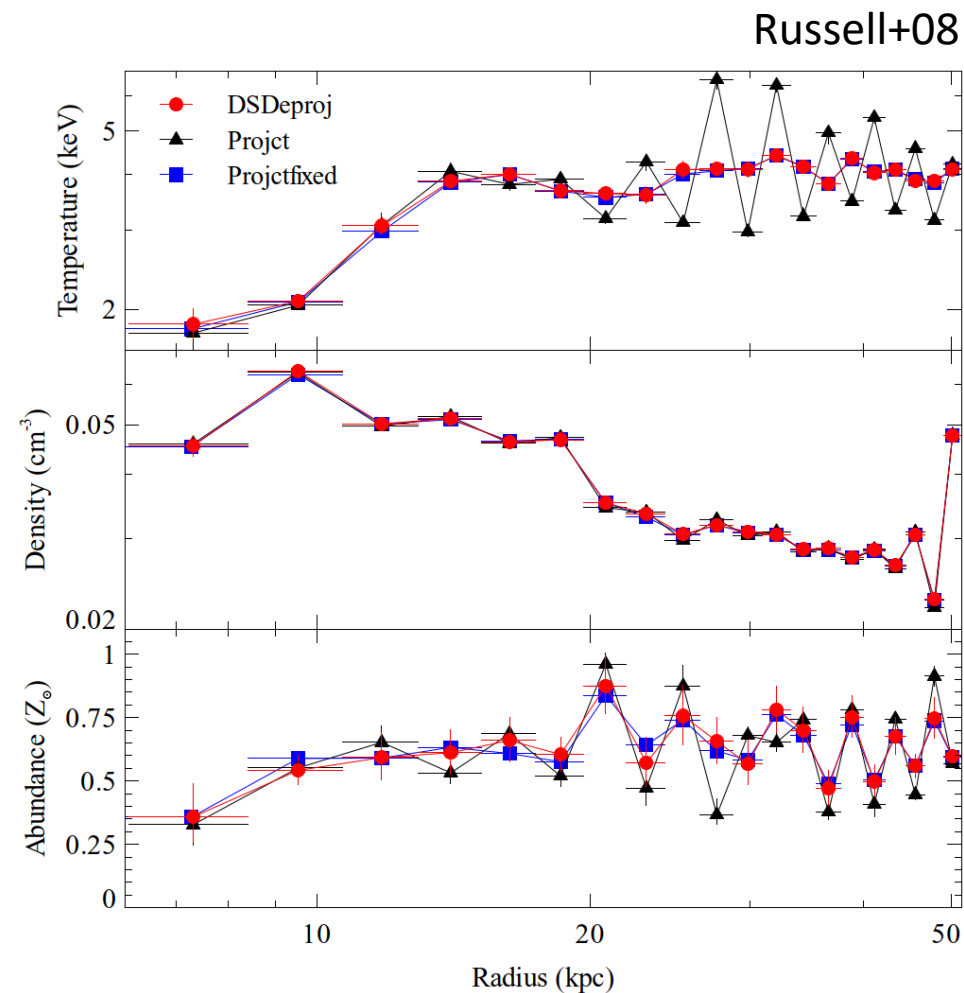
- The quantities plotted in maps are obtained from spectra projected along the line of sight (emission-weighted)
- How important projection is depends on the line-of-sight structure/profile
- Usually in X-rays (for clusters) plasma is optically thin (except in resonance lines)
- Intrinsic 3D variations are larger than seen in 2D
- Would like radial profiles, examining spectra in 2D annuli / annular ellipses
  - When examining radial profiles, obtain “projected quantities”
  - Would like 3D profiles of the intrinsic values





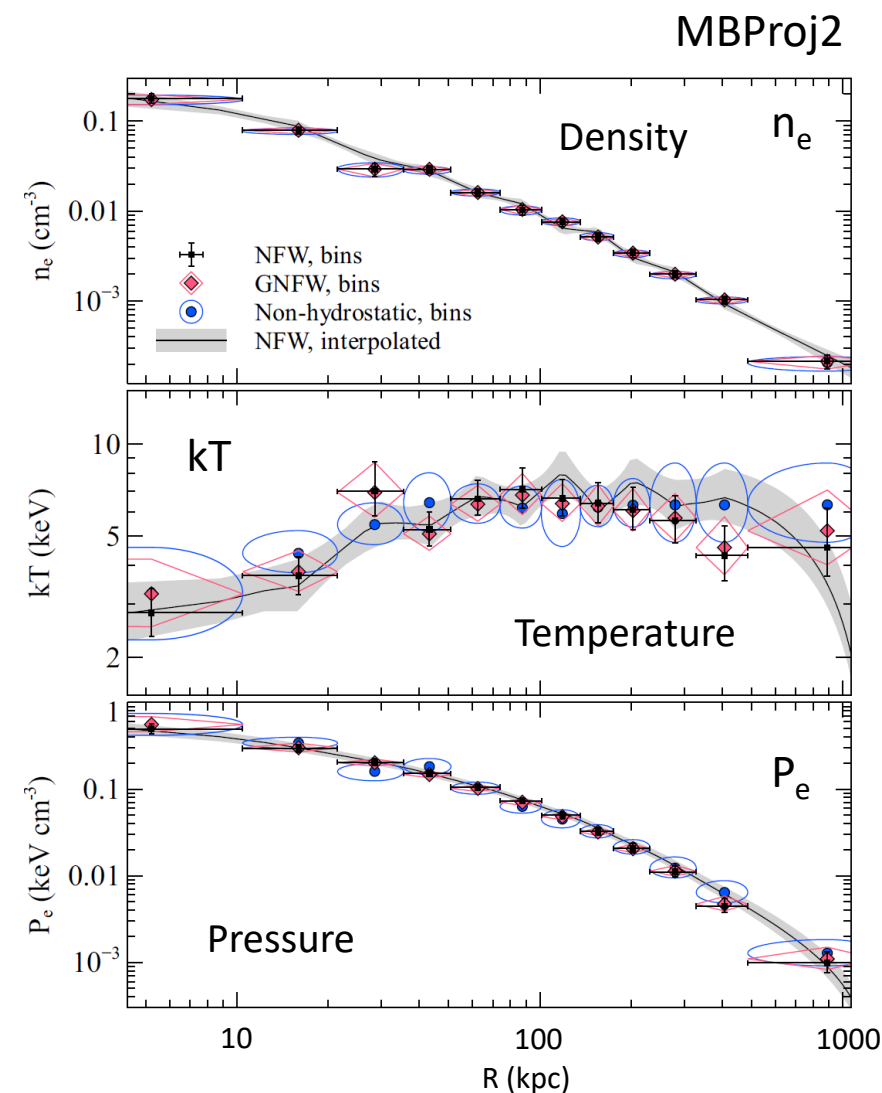
# Decoding projection

- Modelling with assumptions (e.g. spherical) to get 3D intrinsic profile
  - Correcting projected quantities (e.g. Ettori+02) – would be hard to do properly
  - PROJCT in Xspec – forward modelling spectra from annuli with 3D shells – sometimes problems with instabilities in fits (e.g. oscillations in parameters) – see Russell+08
  - DSDeproj – deproject spectra (not so nice statistically!), but avoids instabilities (Sanders+07)



# Decoding projection

- Forward fitting of mass + temperature to spectra extracted from shells (Mahdavi+08, Nulsen+10)
- MBProj2 – forward modelling of surface brightness profiles in multiple energy bands (Sanders+18), either with or without the assumption of hydrostatic equilibrium. Uses MCMC, producing uncertainties on output profiles.
- Bayes-X – forward-model events from 3D model (Olamaie+18), using multinest



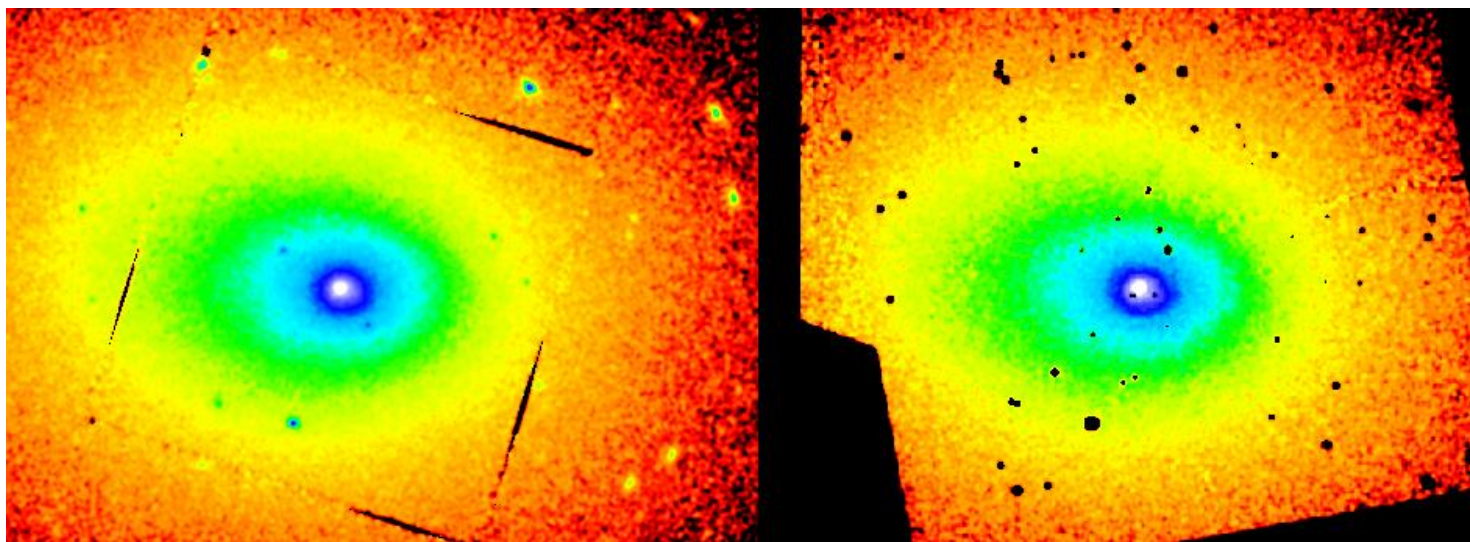
# Instrumental and modelling difficulties

- Point sources
- PSF
- Vignetting / response
- Multiple datasets
- Background
- Out-of-time events

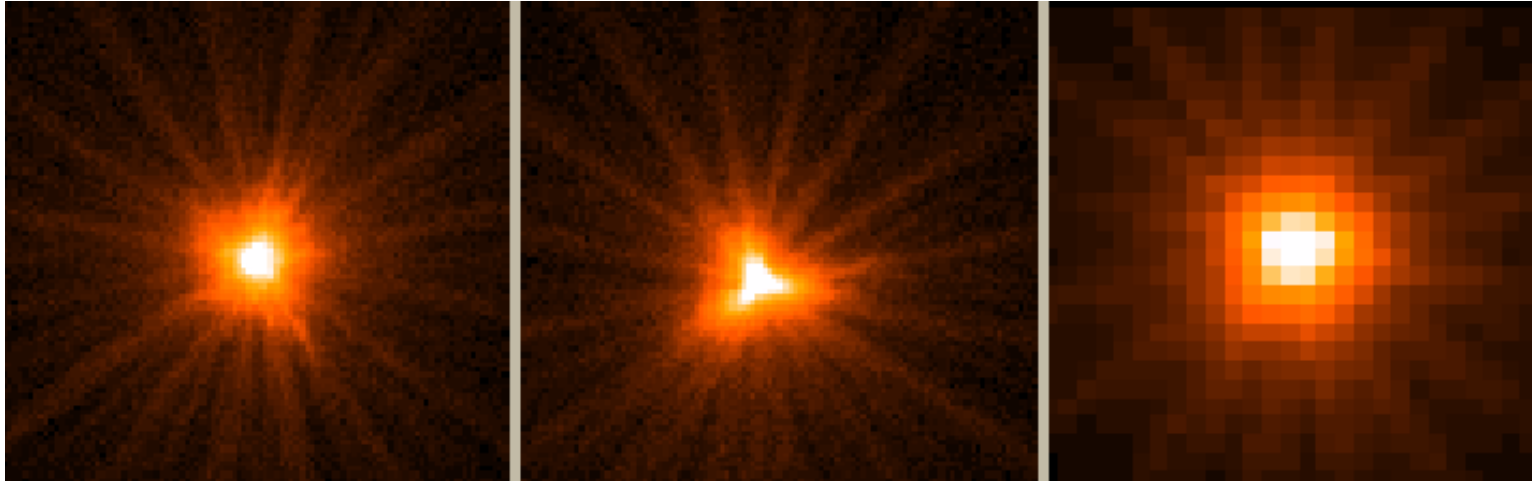


# Point sources

- Usually masked out during spatial analysis (take care of PSF!)
  - Or could be modelled in analysis (e.g. Bayes-X)
- Point sources can be difficult to detect and remove in bright extended sources
  - Structures in extended sources can be confused as point sources by source detection codes
  - Sometimes need to be fixed by hand



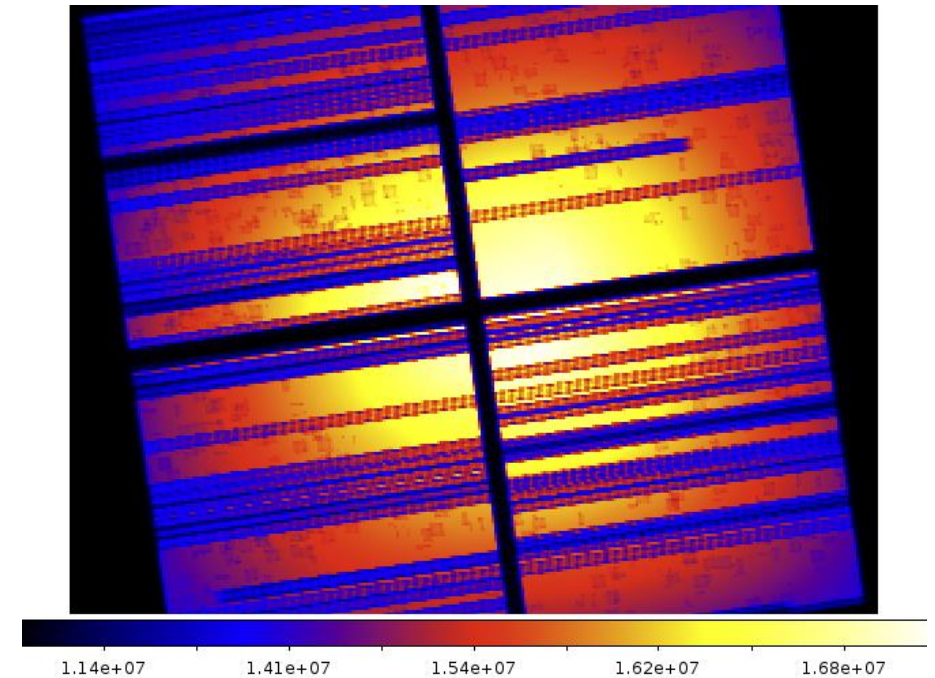
# PSF



- Varies as a function of energy and position
- If region size  $\gg$  PSF, then not so important
- Difficult to account for in mapping
  - See NuStar results, e.g. Wik+14
  - Difficult to model mixing between different bins – potential parameter instabilities
- In 2D profiles, e.g. MBProj2, can account for PSF by using some sort of mixing model when calculating projected spectra

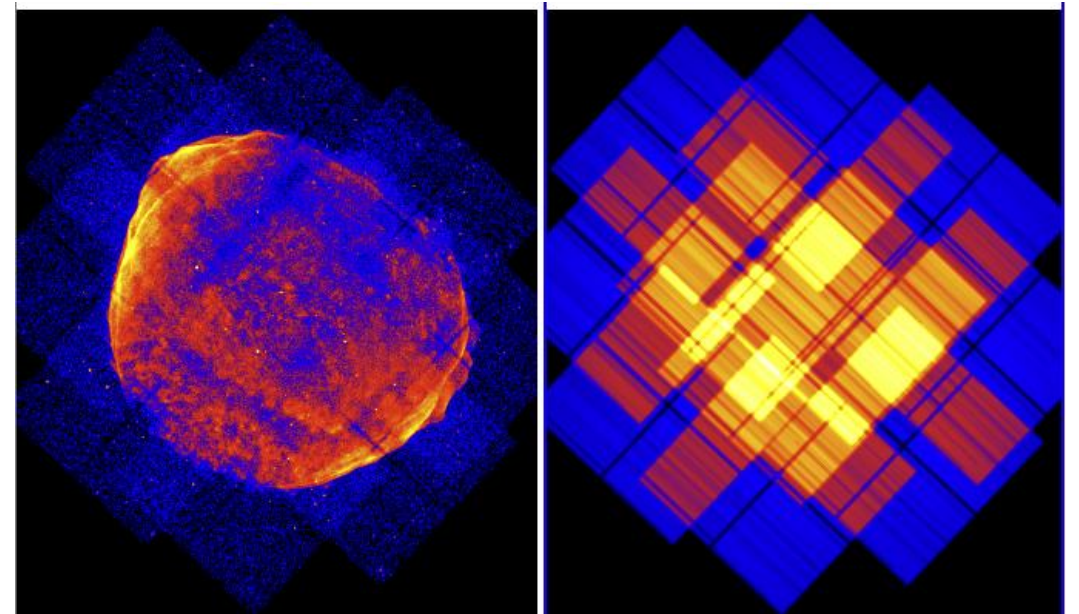
# Vignetting and response

- ARF and RMF varies over detector
- Sometimes simplified to single RMF or single ARF
- Possible issues to do with
  - Weighting of regions of the detector when calculating ARF/RMF – people often use distribution of counts when weighting spatial regions, but not completely statistically proper
  - Chip gaps and detector edges – are these properly included in ARF?



# Multiple datasets

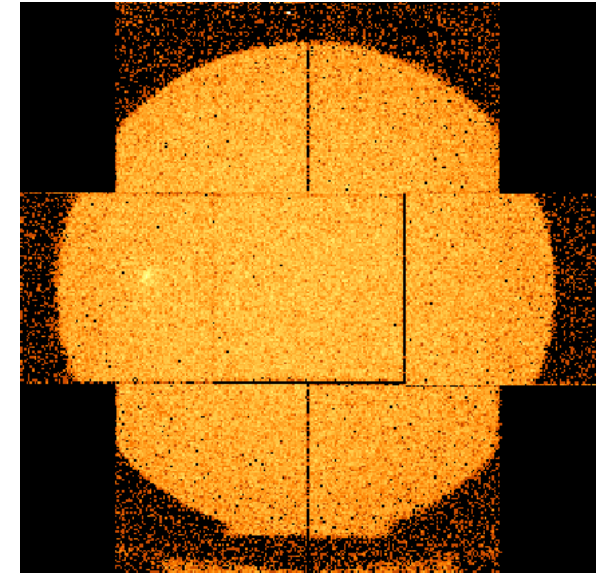
- Possibilities
  - Simultaneous fit of spectra, allowing varying normalizations between spectra (differences in vignetting, chip gaps, detector edges)
  - Add spectra together and weight responses, ARFs
- Adding is a lot easier, but less statistically nice – be very careful!
  - Don't add data if the detectors have different performance!





# Background

- Complex and difficult topic (e.g. Molendi 2017)
- Various components, e.g.
  - Unresolved point sources
  - Soft Galactic foreground
  - Quiescent particle background
  - Soft protons which can flare
- Need appropriate model for spectra of background components over detector, or a background event file, with low systematic uncertainties
- How important this is depends on the faintness of region to analyse (vital in cluster outskirts)
- Far easier if you have a source-free region in your observations
  - Can use to model or to check background modelling
  - Corners of XMM EPIC-MOS cameras can be used to normalise background



# Background 2

- For XMM EPIC-MOS, there is an ESAS package for modelling background, though can be inflexible
- New XMM EPIC task for quiescent background creation: eqvpb
- Chandra has blank-sky background event files if background is less critical
- Closed-filter particle background event files very helpful
- May need to optimize energy band to minimize background

# Out-of-time events (readout streak)

- Event arrives during readout – position is wrong
- Particularly important for certain detector modes and instruments
- Leads to a streak along the readout direction
- More of a problem if you have large contrast in source (e.g. cool core cluster)
- Usually treated as a synthetic background in the analysis
- Tools to create OoT event files from input event files, by randomizing along readout direction

