

## Euclid preparation

### LXVI. Impact of line-of-sight projections on the covariance between galaxy cluster multi-wavelength observable properties: insights from hydrodynamic simulations

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#### ABSTRACT

**Context.** Cluster cosmology can benefit from combining multi-wavelength studies. In turn, these studies benefit from a characterisation of the correlation coefficients among different mass-observable relations.

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**Aims.** In this work, we aim to provide information on the scatter, skewness, and covariance of various mass-observable relations in galaxy clusters in cosmological hydrodynamic simulations. This information will help future analyses improve the general approach to accretion histories and projection effects, as well as to model mass-observable relations for cosmology studies.

**Methods.** We identified galaxy clusters in Magneticum Box2b simulations with masses of  $M_{200c} > 10^{14} M_{\odot}$  at redshifts of  $z = 0.24$  and  $z = 0.90$ . Our analysis included *Euclid*-derived properties such as richness, stellar mass, lensing mass, and concentration. Additionally, we investigated complementary multi-wavelength data, including X-ray luminosity, integrated Compton- $y$  parameter, gas mass, and temperature. We then examined the impact of projection effects on mass-observable residuals and correlations.

**Results.** We find that at intermediate redshift ( $z = 0.24$ ), projection effects have the greatest impact of lensing concentration, richness, and gas mass in terms of the scatter and skewness of the log-residuals of scaling relations. The contribution of projection effects can be significant enough to boost a spurious hot- versus cold-baryon correlations and consequently hide underlying correlations due to halo accretion histories. At high redshift ( $z = 0.9$ ), the richness has a much lower scatter (of log-residuals), while the quantity that is most impacted by projection effects is the lensing mass. The lensing concentration reconstruction, in particular, is affected by deviations of the reduced-shear profile shape from that derived using a Navarro-Frenk-White (NFW) profile; the amount of interlopers in the line of sight, on the other hand, is not as important.

**Key words.** methods: numerical – methods: statistical – galaxies: clusters: general – galaxies: clusters: intracluster medium – galaxies: halos

## 1. Introduction

Galaxy clusters are the largest gravitationally bound, collapsed, and virialised structures in our Universe. They represent unique laboratories for testing cosmological models, galaxy evolution, and thermodynamics of the intracluster medium (ICM, see Kravtsov & Borgani 2012, for a review on galaxy clusters). With respect galaxy cluster cosmology studies (see e.g. Rozo et al. 2010; Bocquet et al. 2019), an accurate characterisation of the selection function and of the mass-observable scaling relations requires a consideration of the dominant systematic uncertainties (see the review on the cluster mass scale in Pratt et al. 2019).

Cluster masses cannot be observed directly and their reconstruction requires both a number of assumptions and high-quality data (see e.g. Meneghetti et al. 2010). This means that precise estimates are rare (Okabe et al. 2010; Hoekstra et al. 2012; Melchior et al. 2015; van Uitert et al. 2016; Stern et al. 2019; Sugiyama et al. 2023; Bocquet et al. 2024). Once a set of highly accurate mass determinations are available, together with other mass proxies recovered from multi-band observations, well-calibrated mass-observable relations (for instance, the mass-richness relation or the mass-temperature relation) can be established and used to estimate galaxy cluster masses for larger samples with known observable properties. For this purpose, it is important to calibrate accurately the mass-observable relations (Giodini et al. 2013; Allen et al. 2011; Schrabback et al. 2021), including proper modelling of their associated scatter (Lima & Hu 2005; Bocquet et al. 2019).

This process is complicated by the fact that studies at different wavelengths are biased by various astrophysical processes and projection effects to various degrees. For instance, X-ray surveys tend to favour the selection of clusters with centrally peaked gas distributions (Pacaud et al. 2007; Hudson et al. 2010; Andreon & Moretti 2011; Andreon et al. 2016; Xu et al. 2018) and suffer from AGN contamination (see e.g. Bhargava et al. 2023); whereas projection effects are known to strongly impact weak lensing mass reconstructions (Meneghetti et al. 2014; Euclid Collaboration 2024) and richness evaluations (e.g. Castignani & Benoist 2016). This is particularly relevant for cluster cosmology studies, where the aim is to reduce uncertainty by combining constraints on different mass-observable relations. For *Euclid* (Euclid Collaboration 2025), this will include quantities such as richness, stellar mass, and the properties of stacked weak lensing signals (Pires et al. 2020) of the cluster samples detected using tools such as AMICO (Bellagamba et al. 2018; Maturi et al. 2019) or PZWav (Euclid Collaboration 2019). In addition, these data could be combined with other multi-wavelength observations Allen et al. (2011). Such properties are known to be biased by

projection effects (Meneghetti et al. 2014), accretion histories (Ragagnin et al. 2022a), mis-centring (Sommer et al. 2022, 2024), and the fit procedure (Sereno et al. 2016). Projection effects, in particular, are expected to generate some covariance between the richness and weak lensing signal; their uncertainty may significantly affect the performance of the mission for cluster population analyses. This effect is one the major sources of systematics for current optical cluster surveys (Costanzi et al. 2019; Abbott et al. 2020) and, thus, it is expected to play an even more critical role for the *Euclid* cluster sample.

Numerical simulations are thus a critical tool to mitigate the impact of the aforementioned biases on cosmological cluster studies. Indeed, the power of observations to constrain them is limited, thus increasing the final uncertainty budget. However, scatter and covariance parameters are also prime sources of uncertainty when aiming to combine information originating from different wavelengths. For instance, various observational works hint towards different directions for the hot- versus cold-baryon covariance (Farahi et al. 2019; Puddu & Andreon 2022; Ragagnin et al. 2022a), as different formation times are related with satellite accretion history (Giocoli et al. 2008).

In this context, numerical simulations have proven to be a very powerful tool for helping observational studies in modelling mass-observable relations, which are strongly affected by galaxy cluster accretion histories (Ludlow et al. 2012; Bose et al. 2019; Davies et al. 2020; Anbajagane et al. 2020; Ragagnin et al. 2022a), projection effects (Meneghetti et al. 2014), and deviations (see e.g. Ragagnin et al. 2021) from the Navarro-Frenk-White density profile (NFW, Navarro et al. 1997), which is often adopted in weak lensing studies. Thus, simulations can suggest the most suitable functional forms of scaling relations for cosmological studies (as in the works of Costanzi et al. 2019; Bocquet et al. 2016, 2019; Ghirardini et al. 2024). They can provide informative priors on their correlation coefficients, which are among the most difficult parameters to be constrained directly from observed quantities, guiding the forward modelling setup of cluster cosmology studies.

There are various works in the literature that study how simulations can help disentangle physical models (see e.g. Cui et al. 2022; Angelinelli et al. 2023), cosmological models (see e.g. Bocquet et al. 2020; Angulo et al. 2021; Villaescusa-Navarro et al. 2022), or dark matter types (see e.g. Ragagnin et al. 2024; Fischer et al. 2024; Contreras-Santos et al. 2024), and also study observable cross-correlations (see e.g. Stanek et al. 2010; Anbajagane et al. 2020).

In this work, besides focussing on correlations between observable properties of interests for multi-wave length studies, we also study the impact of projection effects. The impact of uncorrelated large-scale structure on the covariance between observable properties can be modelled analytically (Hoekstra

2003; McClintock et al. 2019; Costanzi et al. 2019), but the covariance of different observable properties below a few tens of Mpc requires dedicated simulations.

At these scales, numerical hydrodynamic simulations, with their self-consistent depiction of the ICM, emerge as an ideal tool for exploring multi-wavelength observable properties since they incorporate the effects of large-scale structures within which clusters are situated. Indeed, baryon feedback influences the ICM not only within cluster virial radii, but also beyond (see e.g. Angelinelli et al. 2022, 2023).

While it is true that cosmological simulations are influenced by the underlying sub-grid prescriptions, and it is also true that these simulations may diverge on small scales, they generally exhibit agreement on quantities integrated up to the sizes of galaxy groups and clusters (see e.g. Anbajagane et al. 2020). At the same time, different cosmological parameters can affect galaxy cluster properties, such as their masses (Ragagnin et al. 2021), satellite abundance (van den Bosch et al. 2005), and mass-observable relations (Singh et al. 2020). On the other hand, the qualitative significance of covariances and projection effects on observable properties is not expected to significantly hinge on cosmological parameters (Bocquet et al. 2019); thus, possible deviations from this expectation could be estimated using emulators (see e.g. Bocquet et al. 2020; Ragagnin et al. 2021, 2023; Angulo et al. 2021).

We study the impact of projection effects using hydrodynamic simulations to gain insight into which fraction of the scatter and skewness of scaling relations originates from projection effects (i.e., alignment with filaments and objects) or different accretion histories.

In Sect. 2, we present how we set up our *Euclid*-like observable properties and data coming from other wavelengths. In Sect. 3, we study how projection effects impact the scatter and skewness of log-residuals of scaling relations and discuss the impact of projection effects on observable covariance. In Sect. 4, we focus on the mass-concentration relation and how it is affected by projection effects and deviations from the functional form of profiles and the radial ranges of the fits. In Sect. 5, we focus on the covariance between observable properties and study how different accretion histories and projection effects impact them. Finally, we present our conclusions in Sect. 6.

## 2. Numerical setup

We conducted our study by analysing clusters obtained from the Magneticum<sup>1</sup> hydrodynamic cosmological simulations (Biffi et al. 2013; Saro et al. 2014; Steinborn et al. 2015, 2016; Dolag et al. 2016, 2015; Teklu et al. 2015; Bocquet et al. 2016; Ragagnin et al. 2019). They are based on the  $N$ -body code Gadget3, which is built upon Gadget2 (Springel et al. 2005a; Springel 2005; Boylan-Kolchin et al. 2009) with an improved smoothed particle hydrodynamics (SPH) solver from Beck et al. (2016). Magneticum initial conditions are generated using a standard  $\Lambda$ CDM cosmology with *Wilkinson* Microwave Anisotropy Probe 7 (Komatsu et al. 2011) cosmological parameters. The large-scale structure evolution in Magneticum simulations includes a treatment of radiative cooling, heating from a uniform redshift-dependent ultraviolet (UV) background, star formation, and stellar feedback processes as in Springel et al. (2005b). The stellar feedback is then connected to a detailed chemical evolution and enrichment model as in Tornatore et al. (2007), which follows 11 chemical elements (H, He, C, N, O, Ne, Mg, Si, S, Ca, and Fe, with cooling tables from

<sup>1</sup> <http://www.magneticum.org>

Wiersma et al. 2009) which are produced with the CLOUDY photo-ionisation code (Ferland et al. 1998). Fabjan et al. (2010) and Hirschmann et al. (2014) described prescriptions for black hole growth and feedback from AGNs. Halos that host galaxy clusters and groups are identified using the friends-of-friends halo finder (Davis et al. 1985), while subhalos, together with their associated galaxies, are identified with an improved version of SUBFIND (Springel et al. 2001), which takes into account the presence of baryons (Dolag et al. 2009).

We defined  $r_{\Delta_c}$  as the radius that encloses an average density of  $\Delta_c \rho_{\text{cr}}$ , where  $\rho_{\text{cr}}$  is the critical density of the Universe at a given redshift,

$$M_{\Delta_c} = \frac{4}{3} \pi r_{\Delta_c}^3 \Delta_c \rho_{\text{cr}}. \quad (1)$$

Throughout this paper, when we omit  $\Delta_c$  from masses and radii, we imply the usage of  $\Delta_c = 200$  (i.e.,  $M = M_{200c}$ ).

To disentangle the scatter of the mass-observable relation from projection effects, we computed quantities within a sphere of radius,  $r_{200c}$ , and integrated into a cylinder. Projected quantities will be denoted with the superscript 2D (for instance, the total mass inside the cylinder is denoted as  $M^{2D}$ ). We opted to employ a random projection plane for each cluster. Additionally, we set an integration depth of 20 comoving  $h^{-1}$  Mpc, corresponding to approximately 23 Mpc at  $z = 0.24$  and 15 Mpc at  $z = 0.9$  (with  $h = 0.704$ ). This cylinder depth is smaller than *Euclid*'s galaxy cluster photo- $z$  equivalent uncertainty (Euclid Collaboration 2020b) and, while we excluded some uncorrelated projection effects, they are known not to play an important role (Sunayama et al. 2020; Wu et al. 2022). Thus, we ensured that we did not overestimate any projection effect that could be mitigated using photo- $z$ . Consequently, all projection effects examined in this paper hold relevance with respect to interpreting forthcoming *Euclid*-based catalogues.

This study is based on the results from Box2b/hr (Hirschmann et al. 2014) Magneticum simulation, which covers a length of 900 comoving Mpc, with dark matter particle masses  $m_{\text{DM}} = 9.8 \times 10^8 M_{\odot}$ , gas initial particle masses of  $m_{\text{gas}} = 2 \times 10^8 M_{\odot}$ , and a gravitational softening of both gas and dark matter of  $\epsilon = 3.75$  comoving kpc. *Euclid* is expected to detect clusters with masses  $M > 10^{14} M_{\odot}$  up to a redshift of approximately  $z \approx 2$  (Sartoris et al. 2016; Euclid Collaboration 2019), where the bulk of the cluster population which will be used for mass-calibration will lie below redshift  $z \approx 1$ . Furthermore, the number of halos contained in this Magneticum simulation drops significantly beyond the same redshift value. Therefore, we decided to extract halos at two representative redshift slices: at an intermediate redshift of approximately  $z \approx 0.24$ , yielding 4300 objects, and at a higher redshift of approximately  $z \approx 0.9$ , yielding 1300 objects. These extractions were performed using the web portal<sup>2</sup> introduced in Ragagnin et al. (2017). We focussed most of the analyses on the qualitative effect of projection effects at our intermediate redshift slice because of the larger statistics of clusters to help us determine projection effects. We stress that this mass threshold is high enough so that all of our galaxy clusters have at least  $10^4$  particles and, therefore, they can be considered to be well-resolved in terms of their density profile fitting (Navarro et al. 1997).

### 2.1. Observable properties

We go on to discuss the properties that we compute for each cluster and report a summary in Table 1. We compute the total

<sup>2</sup> <https://c2papcosmosim.uc.lrz.de/>

**Table 1.** Observable properties used in this work and described in Sect. 2.1.

Quantity	Notation	Comments
Stellar mass	$M_\star$	
Temperature	$T$	Weighted by X-ray emissivity
Richness	$n$	Satellites with $\log_{10}(M_\star/M_\odot) > 10.65$ , and background subtraction as in <a href="#">Andreon et al. (2016)</a>
X-ray luminosity	$L_X$	In [0.5, 2] keV band
Gas mass	$M_g$	
Thermal SZ parameter	$Y$	See Eqs. (2) and (3)
NFW profile fit parameters	$M_{\text{NFW}}, c_{\text{NFW}}$	In 3D: 100 log-spaced bins with $60 \text{ ckpc} < r < r_{200c}$ , in 2D: reduced shear fit as in Eq. (4), and uncertainty as in Eq. (6), on 12 log-spaced bins with $300 \text{ kpc} < R < 3000 \text{ kpc}$ , a cylinder depth of 20 cMpc, and a source distribution in redshift as in <a href="#">Euclid Collaboration (2024)</a>

stellar masses  $M_\star$  and  $M_\star^{2D}$  as the sum of all stellar particles within the respective volumes. We compute the richness  $n$  with a cut of satellites of  $\log_{10}(M_\star/M_\odot) > 10.65$ , and the projected version  $n^{2D}$  that includes *Euclid*-like corrections for projection effects, similarly to the procedure in [Andreon et al. \(2016\)](#). In particular, we computed the average projected richness between 3.5 and 8 Mpc radii from the cluster centre, divided the annulus in 8 slices of equal angles, excluded the two least dense and most dense slices, and removed the average projected number density of the 4 remaining octants from the projected richness within  $r_{200c}$ <sup>3</sup>; We compute the X-ray luminosities  $L_X$ , and  $L_X^{2D}$ , in the [0.5, 2] keV energy band computed using the APEC model ([Smith et al. 2001](#)), using SPH particle temperatures together with the XSPEC package<sup>4</sup> ([Arnaud 1996](#)), which considers the emission of a collisionally ionised, chemically enriched plasma implemented with metallicity values taken from the simulated particles<sup>5</sup>. We computed the temperature  $T$  and  $T^{2D}$  as weighted by the X-ray emissivity of gas particles. We computed the hot gas mass  $M_g$  and  $M_g^{2D}$ , computed as the sum of the mass of SPH particles with a cold gas fraction greater than 0.1 and  $T > 3 \times 10^4$  K to filter out cold gas.

We note that the projected gas mass is not to be confused with the one inferred from X-ray observations, as X-ray observational works typically include a de-projection of the surface brightness,  $\propto n_e^2$ , which provides a gas-mass estimate that is closer to the spherical  $M_g$ , with the addition of some possible alignment effects coming from the central region of clusters. Moreover, observational works have the capability to mask possible bright substructures, thus minimising the presence of interlopers. Consequently, we can conceptualise the observed projected gas mass as an intermediate value between our  $M_g$  and  $M_g^{2D}$ .

We estimate the integrated Compton- $y$  parameter produced by thermal Sunyaev-Zeldovich (SZ, [Sunyaev & Zeldovich 1972](#)). The Compton- $y$  parameter is defined as

$$y = \frac{k_B \sigma_T}{m_e c^2} \int T n_e dl, \quad (2)$$

<sup>3</sup> Note that *Euclid* richness will be based on detection algorithms such as AMICO ([Bellagamba et al. 2018](#)) or PZWav, which may provide similar or different removal for projection effects. However, we do not have Magneticum Box2b light cones to feed to these algorithms. We stress that our richness computation anyway is very close to what is used in other observational works as [Andreon et al. \(2016\)](#).

<sup>4</sup> <https://heasarc.gsfc.nasa.gov/xanadu/xspec/>

<sup>5</sup> We credit [Biffi et al. \(2017\)](#) and [Truong et al. \(2018\)](#) for the routines and cooling tables we used.

where  $T$  is the temperature,  $n_e$  the number density of the electrons,  $k_B$  the Boltzmann constant,  $\sigma_T$  the Thomson cross-section,  $c$  the speed of light, and  $m_e$  the electron rest mass. We compute the integrated Compton- $y$  parameter  $Y = \int y d\Omega$ , both within the volume of sphere of ( $Y$ ) and a cylinder ( $Y^{2D}$ ). We estimate the integral in Eq. (2) as

$$\int T n_e dl \approx \frac{1}{\pi R^2} \sum_i T_i f_{e,i} \frac{m_i}{m_p}, \quad (3)$$

where the sum runs over all SPH particles,  $m_i$  is the  $i$ -th SPH particle mass,  $T_i$  its temperature and  $f_{e,i}$  is its electron fraction, expressed as local electron number density normalised to the hydrogen number density, and  $m_p$  is the proton mass.

For each halo, we also perform fits of the NFW profile  $\rho_{\text{NFW}}$ , defined as

$$\rho_{\text{NFW}}(r) = \frac{\rho_0}{r/r_s (1 + r/r_s)^2}, \quad (4)$$

where free parameters span the scaling density,  $\rho_0$ , and the scale radius,  $r_s$  (i.e. the radius where the density log-slope equals  $-2$ ). We performed this fit on the total matter density profile on 100 log-spaced radial bins between 75 ckpc (which corresponds to 60 kpc at  $z = 0.24$ , and to 40 kpc at  $z = 0.9$ ; as it is enough to exclude the deep central potential of baryons) and  $r_{200c}$ , and define the corresponding NFW masses and concentration parameters as  $M_{\text{NFW}}$  and  $c_{\text{NFW}}$ , respectively, and the concentration as  $c_{\text{NFW}} = r_{\text{NFW}}/r_s$ , where  $r_{\text{NFW}}$  is obtained from  $M_{\text{NFW}}$  via the Eq. (1).

The projected version of the mass and concentrations are obtained by mimicking a lensing reconstruction procedure by fitting the corresponding reduced shear. We defined the derived masses and concentrations as  $M_{\text{NFW}}^{2D}$  and  $c_{\text{NFW}}^{2D}$ , where  $c_{\text{NFW}}^{2D} = R_{\text{NFW}}^{2D}/r_s$ , where  $R_{\text{NFW}}^{2D}$  is obtained from  $M_{\text{NFW}}^{2D}$  via the Eq. (1). We note that here, ‘2D’, as for the other quantities, indicates that the quantity is computed in projection; however, a correct fit of the mass from reduced shear NFW profile (i.e. our  $M_{\text{NFW}}^{2D}$ ) should provide an estimate of the same NFW halo mass  $M_{\text{NFW}}$  that would otherwise be recovered from a 3D fit.

The fit was computed within the cylinder described above, with a projected radial range of [300, 3000] kpc at  $z = 0.2$ . We performed the analyses at  $z = 0.9$  by rescaling that range with  $H^{-2/3}(z)$ , where  $H(z)$  is the Hubble parameter, in order to retain the same fractional distances from the virial radius (at fixed mass), which resulted in a range of [234, 2300] kpc. We note that in this work, we are not interested in estimating the contribution of the uncorrelated large-scale structure in the reduced shear

reconstruction; therefore, we limited our density projection to a cylinder of the depth of 20 cMpc, (see e.g. [Euclid Collaboration 2024](#); [Becker & Kravtsov 2011](#)).

The signal from the source-averaged excess surface mass density,  $\Delta\Sigma_{\text{gt}}$ , averaged over circular radii,  $R$ , and a population of sources distributed in redshift, can be written as

$$\langle \Delta\Sigma_{\text{gt}} \rangle (R) \simeq \frac{\langle \Delta\Sigma_{\text{t}} \rangle (R)}{1 - \langle \Sigma_{\text{cr}}^{-1} \rangle (\Sigma) (R)}. \quad (5)$$

Here,  $\Sigma$  denotes the surface mass density. The symbol  $\langle \dots \rangle$  denotes an average over radial bins and redshift lens sources, where we used a redshift distribution as proposed in [Euclid Collaboration \(2023\)](#), and [Euclid Collaboration \(2024\)](#).

The quantity  $\langle \Delta\Sigma_{\text{t}} \rangle$  is the excess of surface mass density, averaged over polar coordinates, and defined as

$$\langle \Delta\Sigma_{\text{t}} \rangle (R) = \frac{1}{\pi R^2} \int_0^R 2\pi r \langle \Sigma \rangle (r) dr - \langle \Sigma \rangle (R). \quad (6)$$

The symbol  $\Sigma_{\text{cr}}$  in Eq. (5) is the critical surface mass density; for a given redshift and source, this is equal to

$$\Sigma_{\text{cr}} = \frac{c^2 D_s}{4\pi G D_{\text{ds}} D_d}, \quad (7)$$

where  $G$  the universal gravity constant,  $D_s$  the angular diameter distance to the source,  $D_d$  the angular distance to the lens, and  $D_{\text{ds}}$  the angular distance between the source and the lens. Similarly to [Euclid Collaboration \(2024\)](#), we define the error associated with each radial bin of the profile in Eq. (5) as

$$\delta \langle \Delta\Sigma_{\text{gt}} \rangle = \langle \Sigma_{\text{cr}} \rangle \frac{\sigma_\epsilon}{\sqrt{\pi n_g (R_2^2 - R_1^2)}}, \quad (8)$$

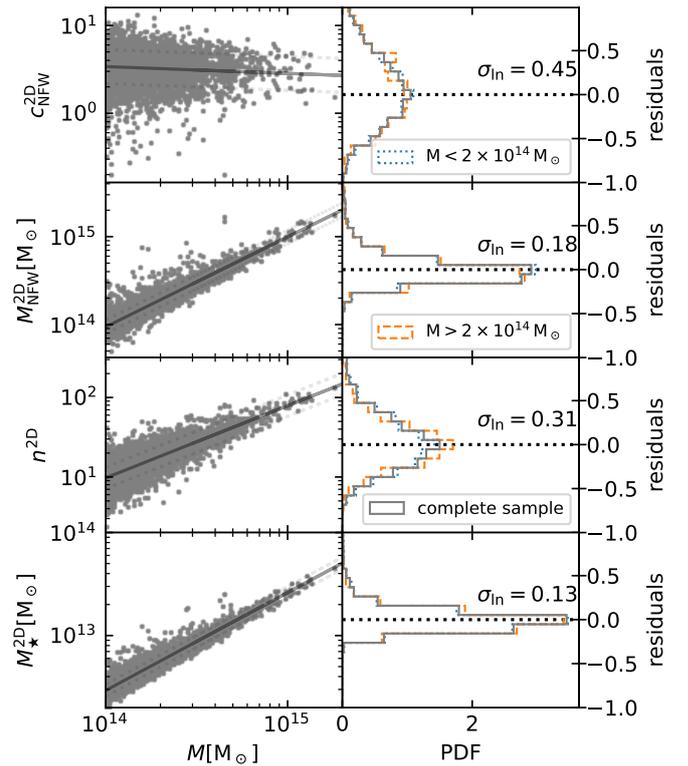
where  $\sigma_\epsilon = 0.3$  ([Hoekstra et al. 2012](#); [Euclid Collaboration 2020a](#)) is the dispersion of the total intrinsic ellipticity  $\epsilon = (1 - q)/(1 + q)$ , where  $q$  is the axis ratio,  $R_1$  and  $R_2$  represent the inner and outer radius of a bin, and  $n_g$  is the number density of galaxies. For our redshift source distribution (we assume the same as in [Euclid Collaboration 2024](#)), we find that  $n_g \approx 28 \text{ arcmin}^{-2}$  for lenses at redshift  $z = 0.24$  and  $n_g \approx 14 \text{ arcmin}^{-2}$  for lenses at redshift  $z = 0.9$ .

## 2.2. Scaling relations

In Fig. 1, we show the observable properties versus true mass,  $M$ , of clusters, derived from Magneticum Box2b/hr simulation for properties that could be derived using *Euclid*-like catalogues, such as the lensing concentration (first row from top), lensing mass (second row), projected richness (third row), and projected stellar mass (last row), as presented in Sect. 2.1. For each property, we fit a scaling relation performed using a linear regression in the log-log space. We utilised a log-log linear regression because a single power law proves to be effective in modelling our scaling relations.

In the right panel of Fig. 1, we show the log-residual distribution for both low-mass halos ( $M < 2 \times 10^{14} M_\odot$ ), high-mass halos ( $M > 2 \times 10^{14} M_\odot$ ), and for the complete sample of the log-residuals,  $\sigma_{\text{ln},i}$ , defined as the logarithmic ratio between the  $i$ -th cluster property and the corresponding scaling relation value at its mass. In the second column, we also report the log-scatter  $\sigma_{\text{ln}}$  defined here as the corresponding standard deviation of the log-residual, namely,

$$\sigma_{\text{ln}} = E \left[ (\sigma_{\text{ln},i} - E[\sigma_{\text{ln},i}])^2 \right]^{1/2}, \quad (9)$$

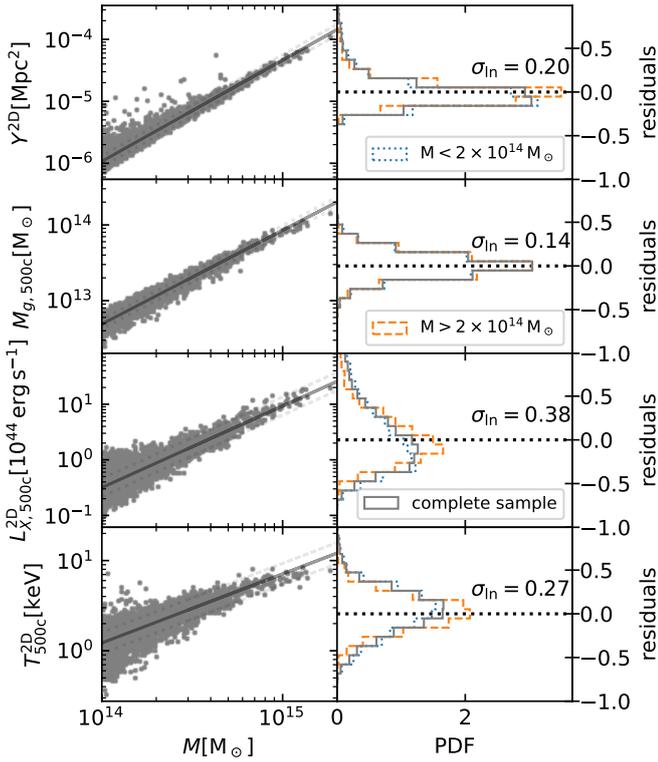


**Fig. 1.** Magneticum mass-observable relation for *Euclid*-like derived quantities. The left column shows scaling relations, relative fit (solid grey line), and a corridor corresponding to one standard deviation (dashed grey line). The right column shows the residual PDF and scatter of log-residuals  $\sigma_{\text{ln}}$ . We report the following properties: lensing concentration  $c_{\text{NFW}}^{2\text{D}}$  (first row), lensing mass  $M_{\text{NFW}}^{2\text{D}}$  (second row), projected richness  $n^{2\text{D}}$  (third row), and projected stellar mass  $M_{\star}^{2\text{D}}$  (fourth row). The histogram of residuals for halos with  $M < 2 \times 10^{14} M_\odot$  is in blue dotted lines, for halos with  $M > 2 \times 10^{14} M_\odot$  is in orange dashed lines, and for the complete sample is in solid grey lines. Note: the three histograms almost overlap. Each distribution panel reports the value of the natural log scatter  $\sigma_{\text{ln}}$  for the complete sample.

where  $E$  is the expectation operator that averages over our catalogue data. We note that the concentration has a scatter of 0.45, which is higher than theoretical expectations (see e.g. [Child et al. 2018](#)). Throughout this paper, we aim to show that this is due to projection effects; in fact, the 3D concentration has a scatter of  $\approx 0.33$ .

We note that our scatter in temperature exceeds that reported in the theoretical work published by [Truong et al. \(2018\)](#). We verified that if we compute mass-weighted temperature, which is known to behave very well in a power-law scaling relation, reveals a log scatter of 0.07. This is in agreement with their work. The additional scatter that we see may be due to different X-ray temperature computations (the cited authors used core-excised temperature, whereas we have taken the contribution of the core into account).

In Fig. 2, we show the mass-observable relations of quantities that could potentially be obtained from various multi-wavelength observations that could enrich studies based on *Euclid*-like data products: the integrated Compton- $y$  parameter, gas mass,  $M_{\text{g},500\text{c}}$ , X-ray luminosity,  $L_{\text{X},500\text{c}}^{2\text{D}}$  converted in the soft band of [0.5, 2] keV, and the temperature,  $T_{500\text{c}}$ . We decided to plot the X-ray luminosity, gas mass, and temperature within  $r_{500\text{c}}$  because this radius is typically used in various X-ray observations (see e.g. [Vikhlinin et al. 2006](#); [Sun et al. 2009](#)).



**Fig. 2.** Same as Fig. 1, but for the following multi-wavelength observable properties: Projected integrated Compton- $y$  parameter  $Y^{2D}$  (first row), the 3D gas mass  $M_{g,500c}$  (second row), the projected X-ray luminosity in the soft band (in range [0.5, 2] keV)  $L_{X,500c}^{2D}$  (third row), and the projected temperature  $T_{500c}^{2D}$  (fourth row). The values of X-ray luminosity, gas mass, and temperatures are reported within an overdensity of  $r_{500c}$  as this definition is a typical choice in X-ray-based observations.

The typical *Euclid* cluster cosmology analysis will therefore rely on mass-observable relations calibrated within  $r_{200c}$  (e.g. richness, weak-lensing mass), and follow-up observations calibrated within  $r_{500c}$  (e.g. X-ray and SZ mass-proxies). Thus, we must consider the covariance between observable properties extracted at different radii.

Finally, we note that generally, X-ray observations are expected to align more closely with the 3D mass rather than the projected one (Etori et al. 2013), although several details adopted to analyse the X-ray observations (e.g. including masking of substructures, de-projection procedures, etc.) can significantly impact the final result. These choices critically depend on the quality of the observations themselves. Dedicated mocks will thus be required to properly consider all these effects and, thus, they are beyond the purpose of this work. For simplicity, in this work, we consider an X-ray-derived gas mass as close to  $M_g$ , while an SZ-derived gas mass closer to  $M_g^{2D}$ .

### 3. Projection effects

The main objective of this work is to disentangle the amount of scatter and skewness in scaling relations that is purely due to projection effects. We note that the observational data are also affected by measurement errors that we have not tackled in this work (e.g. the Poisson error of the limited number of galaxies used to infer the richness). In this section, we discuss the scatter and skewness of mass-observable relation qualitatively and limit the discussion to the data at a redshift of  $z = 0.24$ . We made this

choice because we have a larger sample of galaxy clusters and the results are qualitatively similar to the ones at  $z = 0.9$ . We stress that we leave the quantitative discussion of the scatter and correlation coefficients for both redshifts on Sect. 5.

To assess the role of projection effects, Fig. 3 reports the 3D and 2D scatter of our cluster properties. In the left panel of Fig. 3, we show the value of the scatter (see Eq. 9) of log-residuals  $\sigma_{\ln}$  for all our mass-observable relations. In the shaded region, we also report the values computed within  $r_{500c}$  for the X-ray luminosity, gas mass, and temperature values because this is the characteristic overdensity used in X-ray analyses.

For each observable, we report (with different symbols) in Fig. 3 both the scatter of the complete sample as well as the one of two separate mass ranges of  $10^{14} < M < 2 \times 10^{14} M_{\odot}$  and  $M > 2 \times 10^{14} M_{\odot}$  respectively. We note that the lower-mass bin ( $M < 2 \times 10^{14} M_{\odot}$ ) is the one with the largest scatter because, for a given external object in the line-of-sight (LoS), the profile of a small cluster will be more perturbed with respect to a cluster.

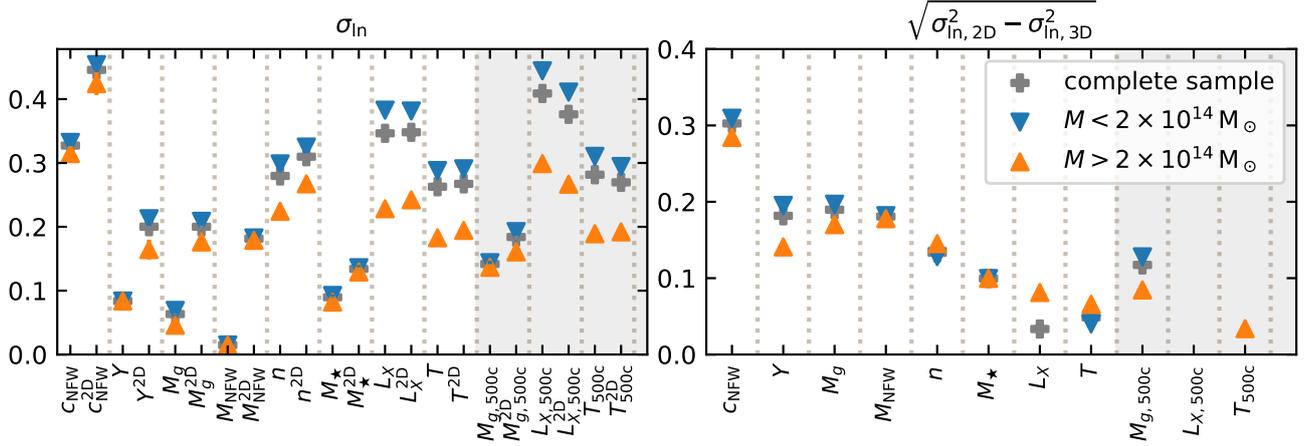
In the left panel of Fig. 3, we see that some quantities have a low scatter in the 3D space and do gain a large amount of scatter once they are seen in projection. To better quantify what is the actual impact of projection effects, in the right panel of Fig. 3,

we present the metric  $\sqrt{\sigma_{\ln,2D}^2 - \sigma_{\ln,3D}^2}$ . This metric shows that the quantities that are most affected by projection effects are the weak lensing concentration, integrated Compton- $y$  parameter, gas mass, and NFW profile lensing mass. This is expected as all these observable properties (except for weak lensing concentration and X-ray luminosity) scale linearly with the respective observable mass. Further, we note that the scatter in the richness agrees to the theoretical predictions from Castignani & Benoist (2016).

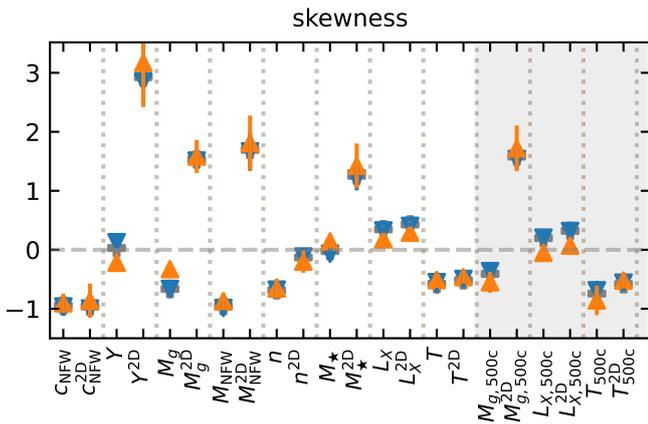
We observe that X-ray luminosity and temperature are the least affected by projection effects. This is attributed to the fact that X-ray luminosity is contingent upon the square of gas density, thereby being primarily influenced by the most bright regions within an image. Similarly, the temperature is predominantly influenced by the innermost regions of a cluster. We note that we lack the value of projection effects for  $L_{X,500c}$  because the 2D scatter is slightly smaller than the 3D one. This happened because projection effects impact under-luminous halos more strongly than overly luminous halos (at a fixed mass bin), with the consequence of the projected X-ray luminosity having a higher normalisation and a lower scatter (see Fig. B.4).

Some mass-observable relations have a large skewness, to aid observational works in modelling these relations, we will estimate their skewness. Therefore, we also quantify deviations of residuals from a symmetrical distribution by means of the Fisher-Pearson coefficient of skewness,  $m_3/m_2^{3/2}$ , where  $m_k$  is the sample  $k$ th central moment<sup>6</sup>. We report its dependency on projection effects in Fig. 4, showing that the properties whose skewness is most impacted by projection effects are the integrated Compton- $y$  parameter, the gas mass, and the lensing NFW mass. We also notice that some scaling relation residuals move from having a negative skewness (for the NFW concentration, e.g. due to un-relaxed and merging clusters) to a positive one once projection effects are taken into account (i.e. from an asymmetry towards negative residuals towards an asymmetry towards positive residuals).

<sup>6</sup> Where the central moment,  $m_k$ , for a random variable  $X$  is defined as  $E[(X - E[X])^k]$ , where a skewness of zero implies a symmetric distribution, a positive (negative) value implies a distribution skewed towards the right (left) part.



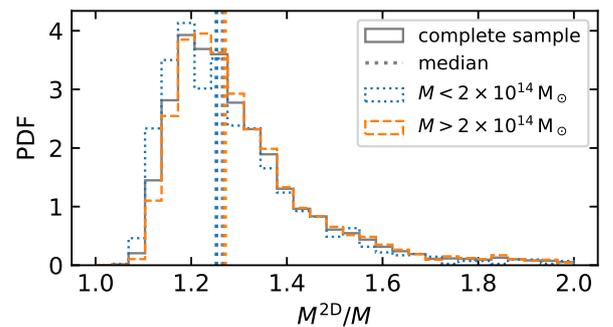
**Fig. 3.** Scatter of our mass-observable relations, paired with their projected version: concentration, integrated Compton- $y$  parameter, gas mass, NFW mass, richness, stellar mass, X-ray luminosity, and temperature, within a radius of  $r_{200c}$ ; the grey band reports the gas mass, X-ray luminosity, and temperature within  $r_{500c}$ . The left panel reports the fractional scatter of both 3D and 2D quantities. Each dotted vertical line separates the regions that report a given quantity and its 2D version. The right panel reports the contribution of projection effects. Points are coloured by their mass range as in Fig. 1, blue inverted triangles represent the low mass bin, orange up-triangles represent the high mass bin, and grey crosses represent the complete sample. Note: we lack the value of projection effects for  $L_{X,500c}$  (see discussion). Points are ordered according to the value of the second panel. Error bars are computed using the jackknife method.



**Fig. 4.** Skewness parameters for our cluster properties. Data, line styles, and colours are as in Fig. 3. Error bars are computed using the jackknife method.

To assess the impact of projection effects, we introduced a variable to quantify the amount of additional matter in the line of sight that can skew our observable properties. We define it as the ratio of the mass within the cylinder and the mass within a sphere,  $M^{2D}/M$ , both of a radius of  $r_{200c}$ , where the length of the cylinder is described in Sect. 2. We present the distribution of  $M^{2D}/M$  in Fig. 5, where we can see that this quantity is strongly skewed and its median value is  $M^{2D}/M \approx 1.26$  (note that for a NFW profile with  $c = 4$ , the corresponding analytical cylinder vs. spherical mass is 1.25). Although this quantity is not directly observable, we still use it to assess the contribution of LoS objects in the scatter of scaling relations. We note that besides objects in the LoS, different fitting procedures may impact the scatter of projection effects, as we will see in Sect. 4.

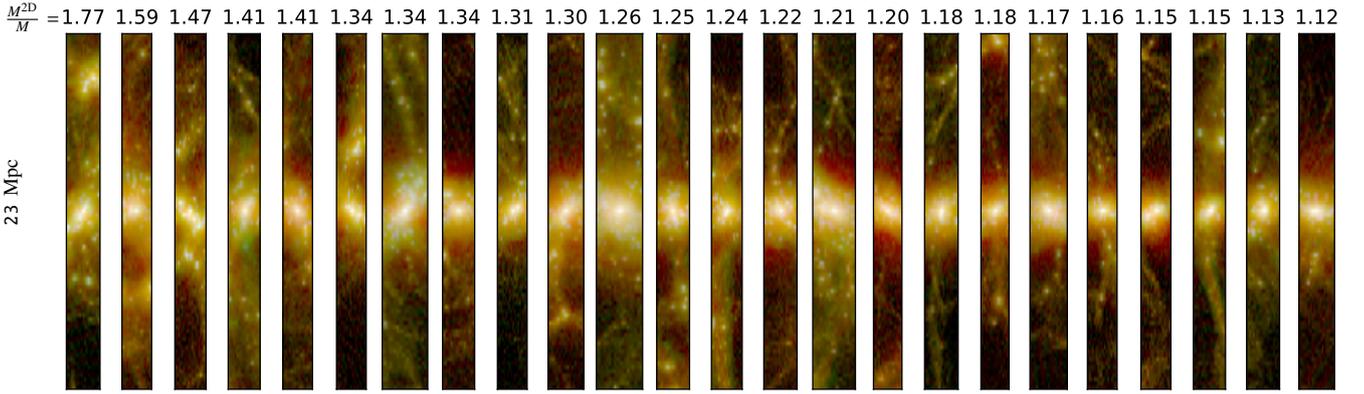
In Fig. 6, we show a random selection of clusters, ordered by decreasing  $M^{2D}/M$  from left to right. Objects with high  $M^{2D}/M$  (the objects in the left-most panels) include clusters that are merging, elongated, or in the LoS. In the rest of this paper, we refer to the objects with a  $M^{2D}/M$  value greater than the median of the distribution 1.26 as having LoS excess.



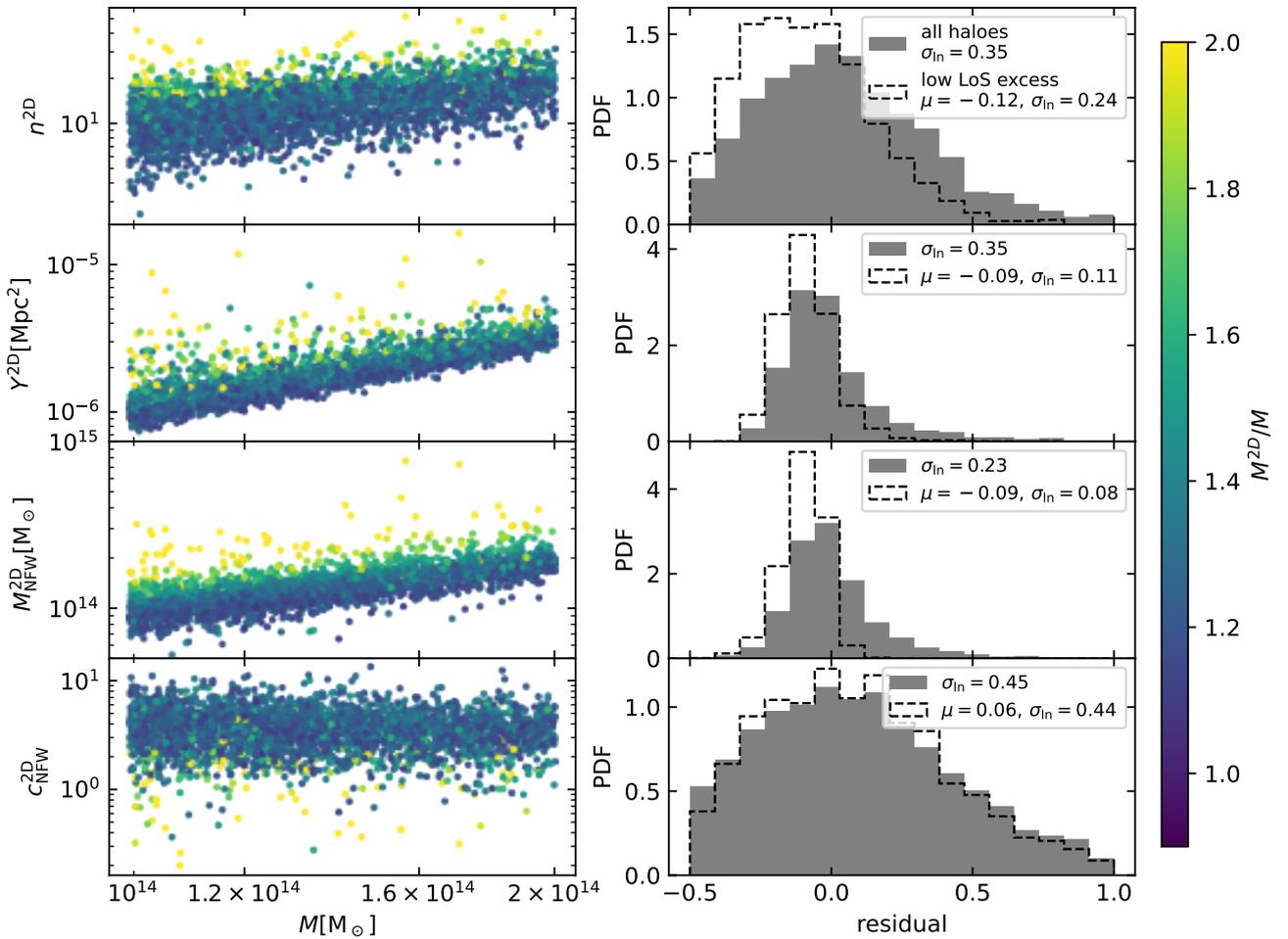
**Fig. 5.** Probability density distribution of  $M^{2D}/M$  at different mass bins: for halos with  $M < 2 \times 10^{14} M_{\odot}$  as a blue dotted line, for halos with  $M > 2 \times 10^{14} M_{\odot}$  as a dashed orange line and for the complete sample as a grey solid line. For each mass bin, the vertical line represents the median values (note: the three lines are very close together).

To study the impact of projection effects in scaling relations, in Fig. 7, we show the scaling relations of the following projected quantities: richness, integrated Compton- $y$  parameter, lensing mass, and concentrations, which are the ones that are most affected by projection effects. We colour-code these points by  $M^{2D}/M$  and focus on a narrow mass range of  $M \in [1, 2] \times 10^{14} M_{\odot}$  to better visualise how LoS excess impacts these scaling relations. On the left column, we visually depict the fact that (with the exception of the concentration), they are strongly correlated with  $M^{2D}/M$ , as the upper points of the scatter plot tend to have higher values of  $M^{2D}/M$ .

We quantified this finding in the right column by comparing the residual distributions (of the power-law fit over the complete mass range presented in Sect. 2.2) of the complete sample with the distribution of objects with low LoS contamination only (we adopted the criteria of  $M^{2D}/M < 1.26$  as the median of the  $M^{2D}/M$  distribution, shown in Fig. 5). We then reported the respective scatter,  $\sigma$ , and average value,  $\mu$ , of the residual distributions (for the complete sample we have that  $\mu = 0$ ). Except for the concentration, residuals of halos with low  $M^{2D}/M$  (see dashed histogram) significantly shift towards negative values of  $\mu$  and  $\sigma$ . For instance, when we consider only objects with a low



**Fig. 6.** Projected maps along a cylinder of length 23 Mpc, with radius  $r_{200c}$  and centred on a random sample of our galaxy clusters, ordered by their  $M^{2D}/M$  (over-plotted above each map) values decreasing from left to right. The pixel red, green, and blue channels are used as follows: the red channel maps the gas projected mass, the green channel maps the dark matter projected mass, and the blue channel maps the stellar projected mass. Column widths are proportional to the cluster radii.



**Fig. 7.** Impact of LoS contamination in scaling relations. We show halo properties as a function of halo mass  $M$  in the left column, and colour-coded by the fractional amount of mass in a cylinder ( $M^{2D}/M$ ), and the residuals PDFs in the right column (grey shaded histogram). Rows correspond to richness, the integrated Compton- $y$  parameter, lensing mass, and lensing concentration. We also show the residuals of a subset of halos with low LoS contamination (in particular  $M^{2D}/M < 1.26$ , dashed line histogram). Each panel reports the scatter of the residuals  $\sigma$  and the mean  $\mu$  of the low LoS residuals.

LoS excess, the scatter of  $Y^{2D}$  decreases from 0.35 down to 0.11, while the  $M_{\text{NFW}}^{2D}$  scatter goes from 0.23 to 0.9. The lensing mass is, in fact, generally known to be affected by projection effects (Meneghetti et al. 2014; Euclid Collaboration 2024).

In this paper, we refer to projection effects as all effects that take place when going from 3D to projection; they include both LoS effects and model uncertainties. This definition becomes relevant when dealing with concentration, which is impacted not

only by LoS objects, but also by the NFW profile fitting procedure. We stress that in Fig. 3 we proved that our projected concentration is actually highly impacted by projection effects, yet only weakly affected by LoS effects. We show in the next section the reason for concentration being strongly affected by projection effects is that their reduced shear profile deviates strongly from the one produced by NFW profile (see, e.g. Ragagnin et al. 2021), which is used to reconstruct the reduced shear profile.

To conclude this part of the paper, we go on to study how correlations between cluster observable properties can be affected by projection effects. To this end, we take the case of a possible hot- versus cold-baryon correlation by studying the stellar mass versus integrated Compton- $y$  parameter (as the latter should strongly correlate with the gas mass). In Fig. 8, we show the integrated Compton- $y$  parameter scaling relation, colour-coded by stellar mass for the 3D quantities (top panel) and projected quantities (bottom panel).

Examining the correlations at a constant halo mass among the computed quantities within spheres (as depicted in the top panel of Fig. 8), we find no discernible weak anti-correlation between stellar mass and the integrated Compton- $y$  parameter (which is defined in Sect. 5). Conversely, when investigating the properties in the projected space, a more pronounced correlation becomes evident. This implies that projection effects can strongly impact the correlation between observable properties. While this analysis is purely qualitative, we go on to quantify the impact of these projection effects in Sect. 5, where we compute the correlation coefficients for both 3D quantities and 2D quantities.

#### 4. Projection effects on lensing concentration

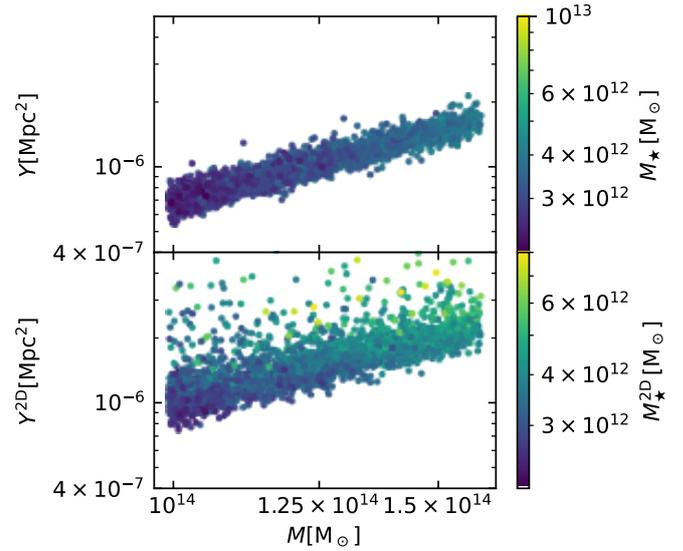
As we found in the previous section, projection effects significantly increase the scatter and skewness in the scaling of lensing concentration with mass. However, this scatter increase is not related to external objects along the LoS. Next, we can assess if the high scatter of lensing concentration is due to deviations of the reduced shear profile from the one induced by an NFW profile.

In this work, we do not delve into the origin of this deviation as it falls beyond the scope of this paper. Such deviation may arise due to halo elongations, suggesting that alternative profiles such as truncated NFW profiles may better suit galaxy clusters (Oguri & Hamana 2011). Alternatively, it could stem from the expectation that the NFW profile is intended to describe stacked halos rather than individual objects. Our focus in this paper is to understand the impact of assuming an NFW profile for each of our halos. We emphasise that these NFW deviations only affect weak lensing signal reconstruction, as the NFW profile is highly effective in recovering halo mass in 3D.

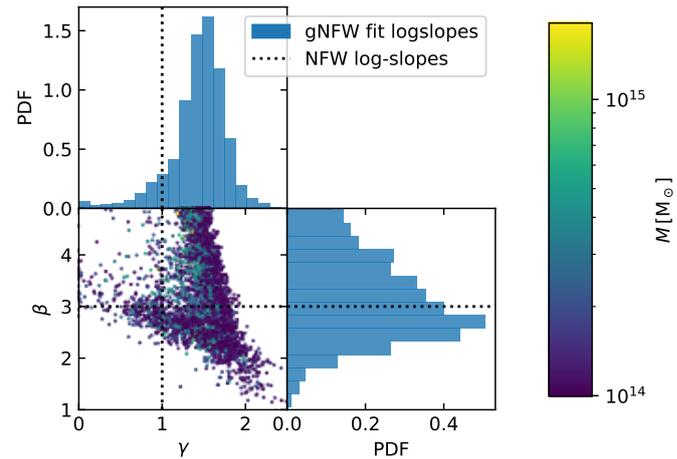
To study deviations from the NFW profile of halos we fit a generalised NFW profile (Nagai et al. 2007); hereafter, gNFW, in spherical coordinates over the same radial range as our previous NFW profile (described in Sect. 2.1), where the density profile  $\rho_{\text{gNFW}}(r)$  is defined as

$$\rho_{\text{gNFW}}(r) = \frac{\rho_0}{(r/r_s)^\gamma (1 + r/r_s)^{\beta-\gamma}}. \quad (10)$$

Here,  $\gamma$  and  $\beta$  are respectively the internal and external log-slopes of the total matter density profiles. The case  $\gamma = 1$  and  $\beta = 3$  produces the NFW profile as in Eq. (4). We note that the Nagai et al. (2007) gNFW profile also depends on the parameter  $\alpha$  that we fixed to  $\alpha = 1$  in this work to explore internal and external log-slope variations only.

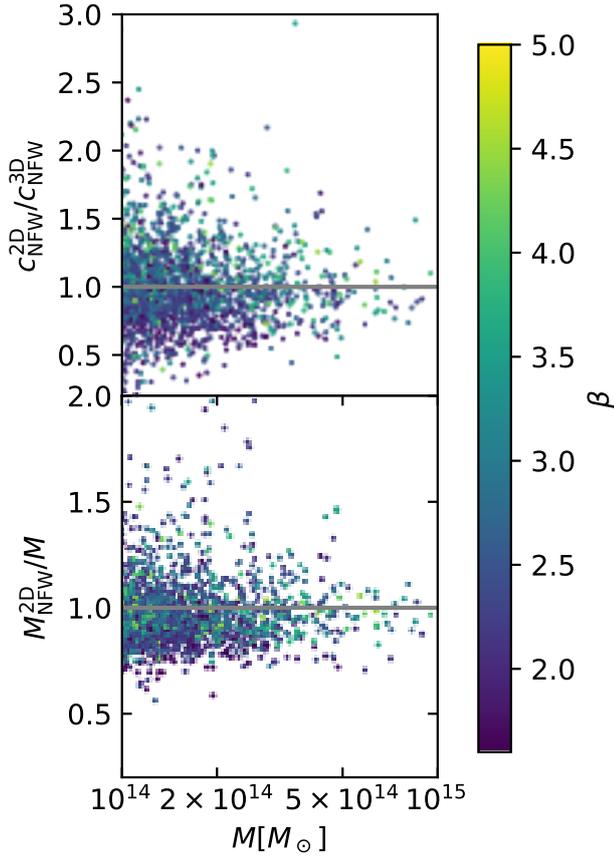


**Fig. 8.** Integrated Compton- $y$  parameter vs halo mass, colour-coded by a stellar mass fraction. The top panel shows quantities computed within a sphere of radius  $r_{200c}$ , while in the bottom panel, they are computed within a cylinder (of radius  $r_{200c}$  and length 23 Mpc as already presented in Sect. 2). We limit the plot in the mass range  $M \in [1, 2] \times 10^{14} M_\odot$ .



**Fig. 9.** Probability density distribution of the parameters  $\gamma$  (inner slope, upper panel) and  $\beta$  (outer slope, right panel) of Eq. (10) of the successful gNFW profile fits. The central panel shows the scatter plot between the two parameters colour-coded by  $M$ . The dotted lines show the NFW parameters  $\gamma = 1$  and  $\beta = 3$ .

We present the PDF for the gNFW profile parameters  $\gamma$  and  $\beta$  in Fig. 9, where the fit was performed in 3D with a flat priors for  $\gamma \in [0, 3]$  and  $\beta \in [0, 6]$ . The data points are colour-coded according to the variable  $M$ , revealing no discernible strong trend with respect to the fitted parameters. For 19% of the objects, the resulting best-fit parameters hit the boundaries of hard-cut priors. Upon visual inspection, these objects are characterised by a very steep matter density profile at large cluster-centric distances, possibly suggesting that a truncated NFW profile might be a better model choice. As our objective is to examine the effects of deviations from the generalised NFW profile, we omitted these objects from the subsequent analysis in this section. Given the substantial deviation of these objects from NFW profile, they could potentially offer additional insights for our analyses. However, incorporating them would necessitate the use of a profile more general than Eq. (10). Therefore, we excluded them in order to make our analysis clearer.

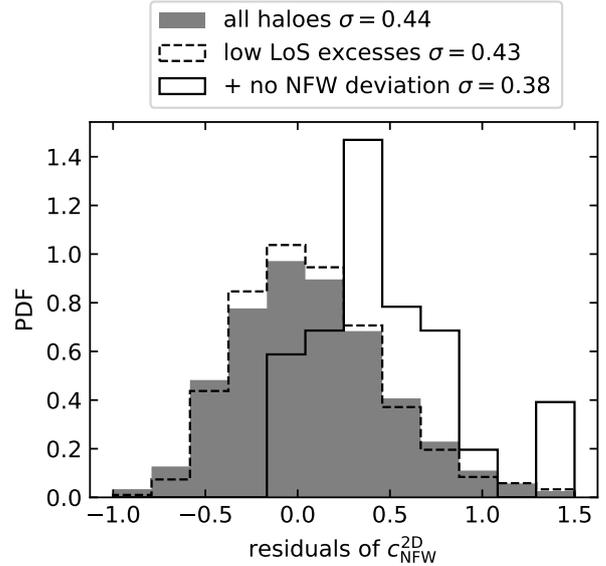


**Fig. 10.** Ratio between 2D NFW profile fit parameters and 3D parameters for halos with a successful 3D gNFW profile fit. Upper panel: Ratio between concentrations. Lower panel: Ratio between halo masses. Points are colour-coded by the external log-slope  $\beta$  of the 3D fit of gNFW.

We observe that the external logslope of Magneticum profiles appears to be slightly flatter than  $-3$ . While we emphasise that this discrepancy does not affect the accurate recovery of mass and concentration parameters in 3D NFW fits (such fits can still yield precise estimates of halo mass and concentrations). However, these deviations in the NFW profiles may affect the reduced shear fit, particularly when observed over large radii (noting that in this work, we use 3 Mpc).

Furthermore, we observe a degeneracy between the  $\beta$  and  $\gamma$  parameters, indicating that our profiles deviating from NFW profile tend to exhibit a flatter profile compared to NFW profile (as illustrated in Fig. A.1). However, investigating this discrepancy is beyond the scope of this paper, as the internal log slope of clusters is not currently captured by existing weak lensing studies.

In Fig. 10, we plot the values of concentration and mass obtained from reduced shear fit, divided by the corresponding 3D quantities and colour-coded by the external 3D gNFW slope  $\beta$  for our intermediate redshift halos. As we can see, halos with large values of  $\beta$  have a projected concentration that is significantly higher than the 3D one (see upper panel). In Appendix A, we report the example of a simulated halo with low LoS excess (see Fig. A.1) and an analytical one (see Fig. A.2), both with a flat external log-slope. We show how the under-estimation of the concentration is caused by the fact that the NFW profile fit on the reduced shear is disproportionately weighting the external part of the profile, which makes it deviate from an NFW profile.



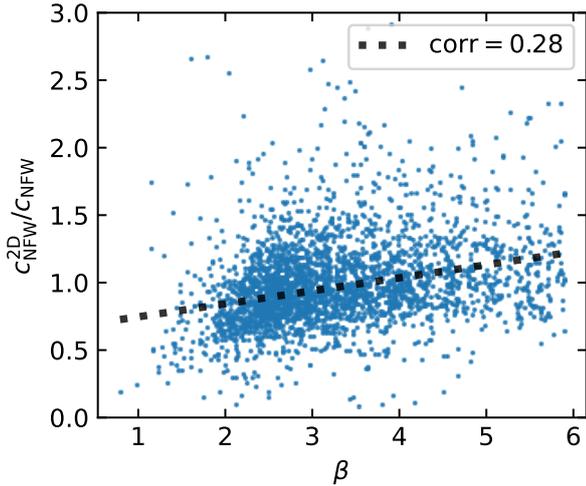
**Fig. 11.** Residuals of lensing concentrations with respect to the power-law fit. As in Fig. 7, the dashed line histogram indicates the residuals for objects with low LoS effects (low value of  $M^{2D}/M$ ). The solid line histogram contains the additional constraints of halos with  $\beta$  and  $\gamma$  parameters close to the ones of an NFW profile ( $2.8 < \beta < 3.2$  and  $0.8 < \gamma < 1.2$ ). Each histogram label reports the scatter  $\sigma$  of the residuals.

We show the concentration residual distribution in Fig. 11 and report their scatter. We note that the projected concentration scatter is not affected by external material along the LoS (where the dashed line and shaded histograms match). However, if we restrict our sample to objects having NFW-like profile log-slopes (we use the criteria of  $2.8 < \beta < 3.2$  and  $0.8 < \gamma < 1.2$ ), then the scatter distribution changes drastically. The concentration residuals decrease from 0.43 to 0.38, and the residuals shift towards higher values, suggesting that these objects are more relaxed. This effect is widely known, as studied, for instance, in Macciò et al. (2007).

We also show how the external log-slope of the halo profile affects the lensing reconstruction by plotting the ratio between the projected and 3D concentration (i.e.  $c_{NFW}^{2D}/c_{NFW}$ ) value versus the 3D log-slope  $\beta$  in the narrow mass bin of  $M \in [1, 2] \times 10^{14} M_{\odot}$  in Fig. 12. We find a positive correlation coefficient of  $\approx 0.28$ , in agreement with a shift of residuals as given in Fig. 11.

## 5. Correlations between properties

In the last sections of this paper, we describe our investigation of the origin of the impact of projection effects in the scatter and skewness of observable properties. We go on to quantify how projection effects impact the correlation between observable properties. To this end, we quantified the Pearson correlation coefficients between their log-residuals (as defined in Sect. 2.2). We adopted the standard error associated with the Pearson coefficient,  $\rho$ , as derived from two normal distributions, given by  $\sigma_{\rho} = \sqrt{1 - \rho^2} / \sqrt{N - 2}$  (see Eqs. 12–93 in Pugh & Winslow 1966), where  $N$  represents the number of objects. This corresponds to a maximum error of 0.015 (for  $\rho = 0$ ) for the sample size at  $z = 0.24$  and a maximum error of 0.028 for the sample size at  $z = 0.90$ . It is worth noting that in the correlation coefficient matrices generated in subsequent analyses, we only coloured values with correlation coefficients of  $|\rho| > 0.3$ , with



**Fig. 12.** Scatter plot of ratio between 2D concentration and 3D concentration against  $\beta$ , namely, the outer slope of Eq. (10), of good 3D gNFW profile fits in a narrow mass range of  $M \in [1, 2] \times 10^{14} M_{\odot}$ . We also report the correlation coefficient.

an aim to highlight strongly correlating properties. We defined a mild correlation as  $0.2 < |\rho| < 0.3$ , as we chose to exercise caution. Correlation coefficients with  $|\rho| < 0.1$  were disregarded.

### 5.1. Analysis at $z=0.24$

In this section, we focus on the halos at intermediate redshift at  $z = 0.24$ . In Fig. B.1, we show the correlation coefficient matrix between log-residuals at fixed halo mass of our projected observable both from *Euclid*-like data (lensing concentration, lensing mass, richness, and stellar mass, respectively) and possible outcomes from multi-wavelength observations (integrated Compton- $y$  parameter, gas mass, X-ray luminosity, and temperature) for intermediate-redshift objects.

In the lower triangle, we present scatter plots alongside the slope derived from the correlation coefficient. This visualisation allows for the identification of instances where the correlation coefficient slope accurately captures the trend of the residuals. Typically, this alignment occurs for quantities that exhibit strong correlation coefficients. For example, our data points show a robust correlation between certain hot baryon tracers ( $M_{\text{g}}^{2\text{D}}$  and  $Y^{2\text{D}}$ ), some cold baryon components ( $n^{2\text{D}}$  and  $M_{\star}^{2\text{D}}$ ), and weak lensing mass,  $M_{\text{NFW}}^{2\text{D}}$ . The underlying reason for these strong correlations lies in projection effects: the greater the amount of matter along the line of sight, the higher the observed values. We demonstrate this further in the subsequent section by presenting the correlation coefficient matrix for 3D quantities, where many of these correlations diminish. This can be anticipated by observing that  $L_{\text{x}}^{2\text{D}}$  and  $c_{\text{NFW}}^{2\text{D}}$  do not exhibit this positive trend of correlations.

Notably, we observe that the correlation between richness and stellar mass ( $\rho = 0.48$ ) is not exceptionally high. Moreover, the stellar mass appears to be more influenced by projection effects compared to richness (evident in their correlations with  $M_{\text{NFW}}^{2\text{D}}$ , where they exhibit  $\rho = 0.69$  and  $\rho = 0.42$ , respectively). We can speculate on two potential causes: firstly, unlike stellar mass, our richness computation incorporates some observationally-motivated background subtraction; alternatively, since stellar mass encompasses all stellar particles (while richness involves a luminosity-motivated galaxy stellar-mass cut), it is plausible that small subhalos are influencing the projected stellar mass.

We note that the concentration is anti-correlated with the gas-mass (and integrated Compton- $y$  parameter). This is in agreement with recent analyses of simulations. In fact, richness is anti-correlated with concentration (Bose et al. 2019), while low concentration is an index of the system being perturbed (Ludlow et al. 2012) and un-relaxed systems tend to be gas-rich (Davies et al. 2020). We refer to Ragagnin et al. (2022a) for a more comprehensive study on low luminous groups. Moreover, at fixed halo mass, the lensing mass correlates strongly with total projected stellar mass ( $\rho = 0.69$ ) and projected gas mass ( $\rho = 0.59$ ), which may be due to the fact that both correlate strongly with LoS contamination. The same holds for the correlation among richness, gas mass, and stellar mass. This is due to projection effects, where LoS excess amplifies all these quantities, as discussed in Sect. 2.2. We note that the 2D lensing mass and projected X-ray luminosity have a slightly positive ( $\rho = 0.20$ ) correlation, in agreement with the observational work of Sereno et al. (2020).

In Fig. B.2, we show the covariance matrix of non-projected quantities for intermediate redshift objects. We see that (as opposed to what is seen Fig. B.1), the 3D covariance matrix shows a mild yet negative covariance between gas mass and stellar mass ( $\rho = -0.24$ ), along with a positive correlation between richness and gas mass ( $\rho = 0.23$ ) because most of their correlations in the projection are due to the line of sight excess, which significantly increases the values of the gas mass, the richness, and the stellar mass. In Fig. B.3, we report the correlation matrix as in Fig. B.1 where we present X-ray luminosity, gas mass, and temperature, as computed within  $r_{500\text{c}}$ , which shows an anti-correlation between the gas mass and the concentration residuals ( $\rho = -0.14$ ), which is significantly lower than the one found in Figs. B.1 and B.2 ( $\rho$  is equal to  $-0.26$  and  $-0.34$ , respectively). One possibility is that this change in sign of the correlation is caused by the fact that mixing overdensities (concentration is within  $\Delta_{\text{c}} = 200$  and gas-mass is within  $\Delta_{\text{c}} = 500$ ) does introduce an additional correlation with the sparsity (Balmès et al. 2014; Corasaniti et al. 2022), which itself is correlated with the concentration (see Appendix B).

For completeness, we report the correlation coefficient matrix and the scatter of log-residuals of all quantities in Table B.1. There, we also added the core-excised projected X-ray luminosity  $L_{\text{x,ce500c}}^{2\text{D}}$ , as it is typically used in X-ray-based observational studies. Thus, we can see that the scatter and most of the correlation coefficients are smaller than  $L_{\text{ce500c}}^{2\text{D}}$ , while the correlations with the concentration and gas mass increase. We note that we have not reported the 3D NFW mass ( $M_{\text{NFW}}$ ) because it has an extremely low intrinsic scatter  $\sigma_{\text{ln}}(M_{\text{NFW}}) \approx 0.01$  and its correlation coefficients are not meaningful.

### 5.2. Analysis at $z=0.9$

In this section, we focus on observational property covariance matrixes of our halos at  $z = 0.9$ . At this redshift, we computed projected quantities within a cylinder depth of 35 Mpc to retain the same relative ratio as the photo- $z$  uncertainty of the low-redshift analysis (it scales with  $1+z$ ). With respect to the cylinder used to integrate  $\Delta\Sigma_{\text{gt}}$ , we re-scaled so as to keep it constant in comoving units with the low-redshift analyses. We re-scaled the 3D NFW profile minimum radius to 40 kpc while we kept the maximum radius at  $r_{200\text{c}}$ . With respect to the radial range of the lensing fit, we re-scaled it with  $H^{-2/3}(z)$ ; thus, it was carried out in the range of [234, 2300] kpc.

We stress that we do not model observational uncertainty. Therefore, the decrease in background source count with redshift

does not impact our best fits. However, it still impacts the fact that we weigh external radial bins more than the internal ones. We report the values of the scatter and the projection contribution at  $z = 0.9$  in Fig. B.6, while we report the log-residuals and the skewness for each property in Fig. B.7.

In particular, the quantities most affected by projection effects are the lensing mass and concentration, whereas the temperature is the lowest. These results are qualitatively similar to the low redshift analyses, with the Compton- $Y$  parameter and gas mass being slightly less affected by projection effects. We note that since the virial radius is smaller at higher redshift values, our radial range of the reduced shear is closer to the NFW scale radius; therefore, the weak lensing reconstruction is more effective in capturing the scale radius and more sensitive to deviations from an NFW profile. As a consequence, we found that the increase of scatter going from  $c_{\text{NFW}}$  to  $c_{\text{NFW}}^{2D}$  compared to the low redshift analyses.

We report the correlation coefficient matrix and the scatter log residuals of the quantities at  $z = 0.9$  in Table B.2. We corroborate the tables with the scatter and skewness analyses at  $z = 0.9$  in Figs. B.6 and B.7 respectively. As for the case at  $z = 0.24$ , we note that we do not report the 3D NFW mass ( $M_{\text{NFW}}$ ) because it has an extremely small intrinsic scatter of 0.01; thus, its correlation coefficients have no impact in our study.

## 6. Conclusions

In this work, we have analysed a number of galaxy clusters from Magneticum hydrodynamic simulation Box2b/hr. We carried out our study in a mass range, tailored for *Euclid*-like data products (see Sartoris et al. 2016; Euclid Collaboration 2019); namely, with a mass of  $M_{200c} > 10^{14} M_{\odot}$ . To this end, we computed properties that could come from *Euclid* catalogues of galaxy clusters, such as richness, stellar mass, and lensing masses and concentration, along with plausible properties coming from multi-wavelength studies, such as X-ray luminosity, integrated Compton- $y$  parameter, gas mass, and temperature. All these properties were computed both within a sphere and within a cylinder (both with radius  $r_{200c}$ ) to account for projection effects. Our study considers the remarkable capabilities of *Euclid* photo- $z$  measurements in identifying interlopers. However, their importance decreases significantly at scales as small as a few tens of Mpc. This depth is still enough to contain multiple halos along the LoS. Hence, we studied the projection effects on a scale that is significantly smaller than the *Euclid* photo- $z$  uncertainty. We then studied how the scatter and skewness change when we are measuring quantities in 3D space or in projection. We summarise our findings below.

- The properties that are most affected by projection effects are the mass and concentration from lensing, the integrated Compton- $y$  parameter, and the gas mass. In contrast, the temperature and X-ray luminosity are the quantities least affected by projection effects.
- In both redshift slices ( $z = 0.24$  and  $z = 0.9$ ), the influence of LoS effects is substantial and potentially leads to a spurious correlation between gas and stellar masses. These projection effects have the capacity to markedly enhance correlations between gas and stellar mass (they go from a negative value of  $-0.24$  to a significantly high value of  $0.57$ ), effectively masking the intrinsic underlying correlation (e.g. one driven by distinct accretion histories).
- The lensing concentration, on the other hand, is mainly affected by the fact that the profile outskirts of reduced shear deviate from the one coming from an NFW profile (which

is the profile typically used in WL analyses). We found that deviations from an ideal NFW profile increase the skewness from 0.6 to 2.5 and increase the scatter of log-residuals from 0.33 (in agreement with theoretical works) up to 0.46.

The analysis presented here has been carried out using a single suite of hydrodynamic simulations. Regarding weak lensing masses and concentration, since in this work, we did not consider the profile noise due to the finite number of background galaxies. Future studies are needed to improve our estimations.

Some works have shown that both scatter and correlation coefficients vary between cosmological simulations with different cosmologies (Ragagnin et al. 2023), the presence of feedback schemes (Staneke et al. 2010), and different cosmological simulation suite in the market (see Fig. 7 in Anbajagane et al. 2020). So, while simulations can provide directions on how to model correlation coefficients, it is possible that when using simulated data, we need to allow for variation due to the different baryon physics. Further studies that assess the role of baryon physics may also help reduce recent tensions between simulations and observations (see e.g. Ragagnin et al. 2022b).

Furthermore, when striving for even more precise results, it is important to acknowledge that mass-observable relations are not exact power laws. Therefore, employing more generic fitting techniques, such as a running median, could yield improvements. Additionally, there is room for enhancement in how we compute correlation coefficients in future studies. One potential approach could involve simultaneously fitting both the mass-observable relation scatter and the correlation coefficients by maximising multi-variate likelihoods. We anticipate that future studies combining *Euclid* data with multi-wavelength observations may encounter challenges in shedding light on residual correlations, which are puzzling at present and primarily dominated by projection effects.

## Data availability

Raw simulation data were generated at C<sup>2</sup>PAP/LRZ cosmology simulation web portal <https://c2papcosmosim.uc.lrz.de/>. Derived data supporting the findings of this study are available from the corresponding author AR on request.

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## Appendix A: Fit of gNFW

In Fig. A.1, we present the density profile of a halo that deviates from the NFW profile and has no LoS contamination. In particular, it has  $\beta \approx 1.8$  and  $\gamma = 1.5$ . We show its NFW profile fit profile on the 3D density in the upper panel of Fig. A.1, where we can see that 3D NFW profile (performed on radial bins in a sphere) is capable of capturing the shape of the halo and to estimate its mass with high accuracy (within  $\approx 5\%$ ). In the central panel, we show the reduced shear profile and best fits, where we can see that the fit performed on the reduced shear underestimated the concentration and is not able to capture the more internal part of the shear profile, as it is done by the profile that was fit in 3D.

We first exclude this mismatch as being due to projection effects by showing that both the reduced shear from the particle data (orange line) matches the one recovered by performing an analytical projection of the 3D profile (blue solid line). In particular we project the density profile  $\rho(r)$  and derive the surface mass density  $\Sigma_{\text{conv.}}$ , as follows

$$\Sigma_{\text{conv.}}(R) = \int_{-\infty}^{+\infty} \rho(\sqrt{R^2 + z^2}) dz = 2 \int_R^{\infty} \rho(r) \frac{r}{\sqrt{r^2 - R^2}} dr. \quad (\text{A.1})$$

What we find is that the shear obtained with the aid of an analytical projection  $\Sigma_{\text{conv.}}$  matches very well the real one (i.e., orange and blue lines do match). This hints that there are no strong LoS effects for this cluster.

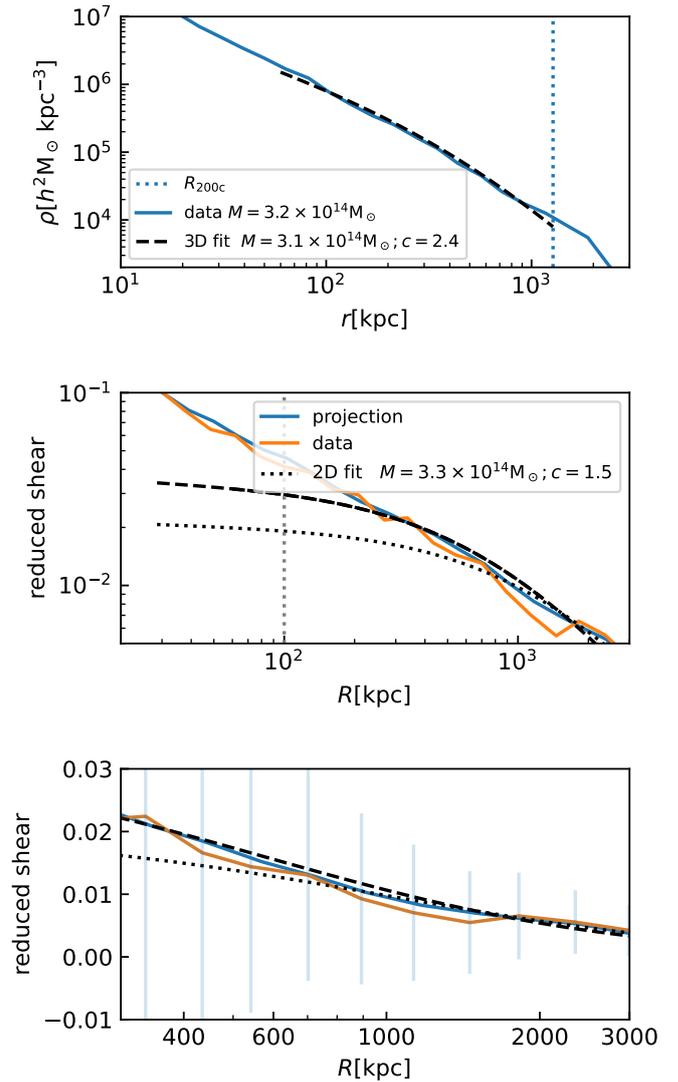
To understand why the fit on the shear is not able to capture the concentration of the original halo, we zoom our fit in the bottom panel of Fig. A.1, where it looks like the fit is very good in capturing the final part of the profile and not able to capture the internal. It is crucial to emphasise that we did not include observational uncertainties in these analyses. Therefore, the uncertainty outlined in Eq. (8) affects the fit by assigning more weight to external radial bins compared to internal ones. It is worth noting that the proportionality factors in Eq. (8) will not affect our best fit.

To validate this point in Fig. A.2 we study the bias on fitting an NFW profile on a mock gNFW profile that has  $\beta = 1.8$  and  $\gamma = 1.5$ , a mass of  $3 \times 10^{14} M_{\odot}$  and a concentration  $c = 2.4$  (as the halo presented in Fig. A.1). We see that the 3D NFW profile is capable of estimating both its mass and its gNFW concentration with high accuracy (see top panel match between blue and dashed black lines). On the other hand the fit of the shear (we report in the bottom panel of Fig. A.2) has the same problems as the one on the cluster in Fig. A.1: it recovers a low concentration (with a value of 1.5). This may be because, at outer radii, the model fits the data. It is possible that the under-estimation of concentration at low radii is caused by the combination of two factors: the fit under-estimates the shear at lower radii (with the result of under-estimating the lensing concentration), or the fact that  $\gamma$  is different than 3 induces an NFW profile fit with a low concentration.

We then performed the experiment of fitting the analytical profile with constant (yet unrealistic) error bars. While the fit captured the profile's shape, it recovered a concentration of 1.6, implying that there is indeed a degeneracy between the shear of low-concentrated NFW profiles and steeper-NFW profiles.

## Appendix B: Correlation matrices

In this appendix, we report the correlation coefficient matrices between log-residuals of our mock observables. In Fig. B.2 we

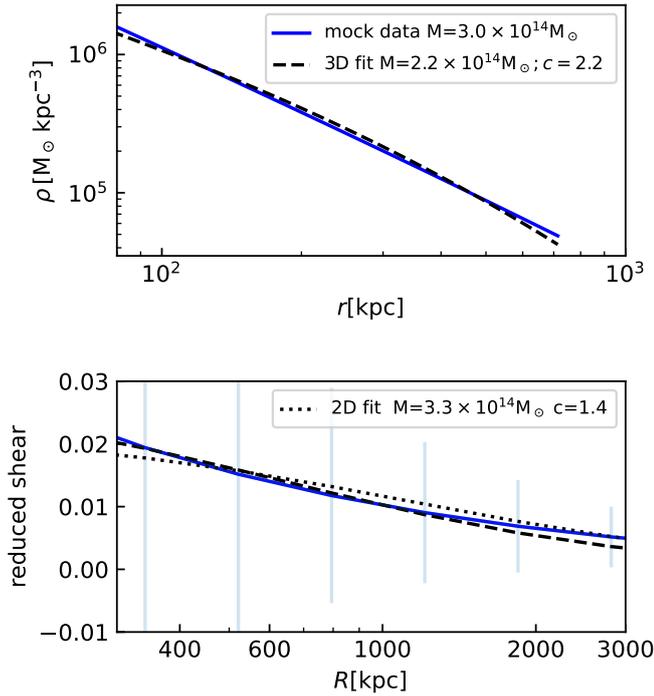


**Fig. A.1.** Density profiles of a simulated halo and the corresponding NFW profile fit. Upper panel: total matter density profile (blue solid line) and the respective NFW profile fit profile (black dashed line). Central panel: reduced shear from simulated particles (orange solid line), and from the analytical projection of the density profile  $\Sigma_{\text{conv.}}$  presented in Eq. (A.1) and performed in the radial range [60, 3000] kpc, in the blue solid line. The dashed vertical line indicates the minimum radius of the shear fit, and the fit profiles (black lines) are extrapolated down to 10 kpc to enhance the central densities predicted by the two fits. The bottom panel shows the same as the central panel but focuses on the radial range of the fit. The error bars indicate the uncertainty for each radial bin, as defined in Eq. (8).

show the covariance matrix of non-projected quantities for intermediate redshift objects. In Fig. B.3, we report the correlation matrix as in Fig. B.1 where we present X-ray luminosity, gas mass, and temperature.

We now discuss the differences between scaling relation scatters and covariance values at different overdensities. First of all, we set out to address the fact that when we compute X-ray luminosity within  $r_{500c}$  (instead of  $r_{200c}$ ), we find that the scatter of the scaling relation of the projected quantity is larger than the 3D one.

To investigate this feature, we will focus on the bolometric X-ray luminosity. We report the 3D and projected bolometric X-



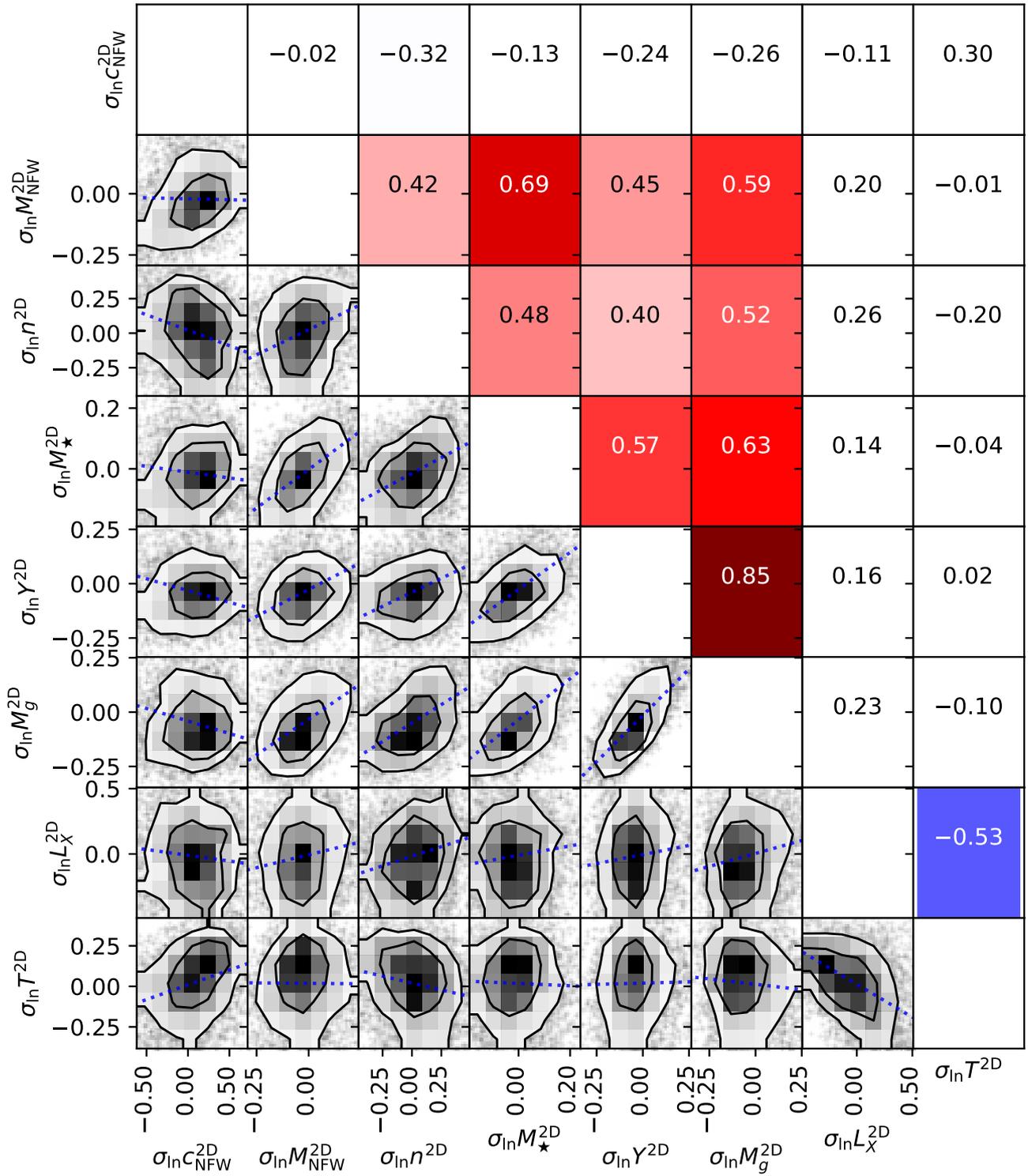
**Fig. A.2.** Density profiles of a mock halo that deviates from NFW and the corresponding NFW profile fit. The mock halo mass, concentration parameter and gNFW log-slopes are chosen to match the ones of the simulated halo presented in Fig. A.1. The upper panel reports the total matter density profile of the mock halo (solid blue line) and the profile from the corresponding NFW profile fit (dashed black line). The bottom panel shows the reduced shear and the profile from the corresponding NFW profile fit (dotted black line). The error bars indicate the uncertainty for each radial bin, as defined in Eq. (8).

ray luminosity in Fig. B.4 (top panel), where it is visually clear that the projected X-ray luminosity is (as expected) always larger than the 3D one. One can also notice that the increase in X-ray luminosity depends on the fact that a halo is over-luminous or not: the increase of luminosity growing from the 3D to 2D is larger for under-luminous halos than for over-luminous halos. We prove this point in the bottom panel of Fig. B.4 where we show the ratio between the 2D and 3D luminosity as a function of their residual of the 3D scaling relation (the higher the value of the  $x$  axis, the more over-luminous is the object for its mass bin), where we can see a strong anti-correlation: overly luminous objects (for a given mass bin) are not going to be affected much by the fact that their luminosity is computed in 3D or 2D. The possible cause is that an interloper in the LoS will not affect much an overly luminous object.

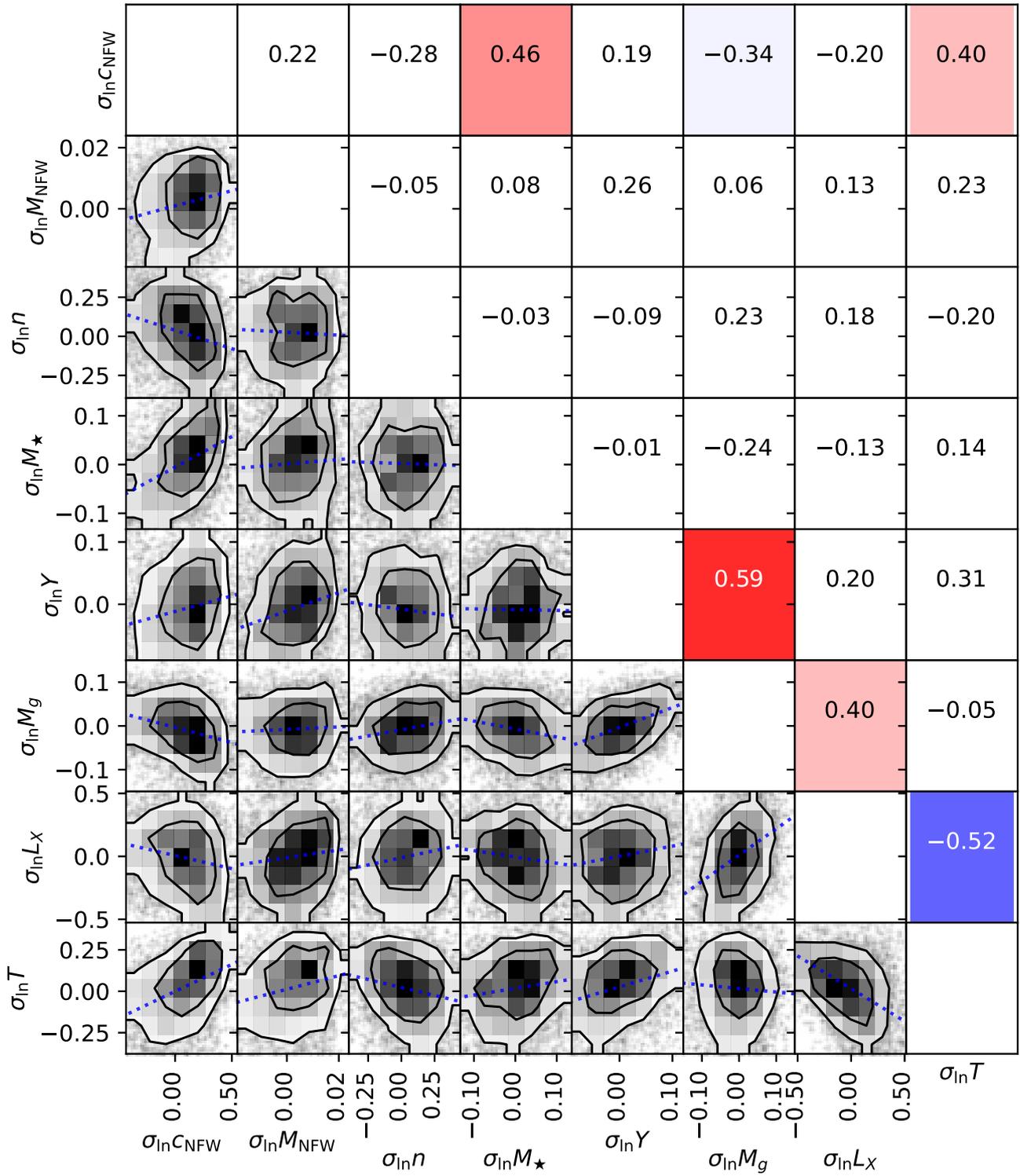
For completeness, in Fig. B.5 we show the correlation coefficients between the gas mass and stellar mass computed within both  $r_{500c}$  and  $r_{200c}$  and the concentration. Here we can see a change of sign between  $M_{\star,500c}-M_{g,500c}$  correlations and  $M_{\star,500c}-M_g$  correlations and a change in the sign between  $c_{\text{NFW}}-M_g$  correlations and  $c_{\text{NFW}}-M_{g,500c}$  correlations.

Finally, in Fig. B.8 we report the scatter of observable properties at fixed mass for both *Euclid*-like quantities (lensing mass, richness, and projected stellar mass) and possible multi-wavelength properties (integrated Compton- $y$  parameter, X-ray luminosity, and temperature), where we computed the X-ray luminosity and temperature within  $r_{500c}$ , as they are typically derived within this overdensity. The upper panel of Fig. B.8 shows the residuals of the log-log linear regression where we see

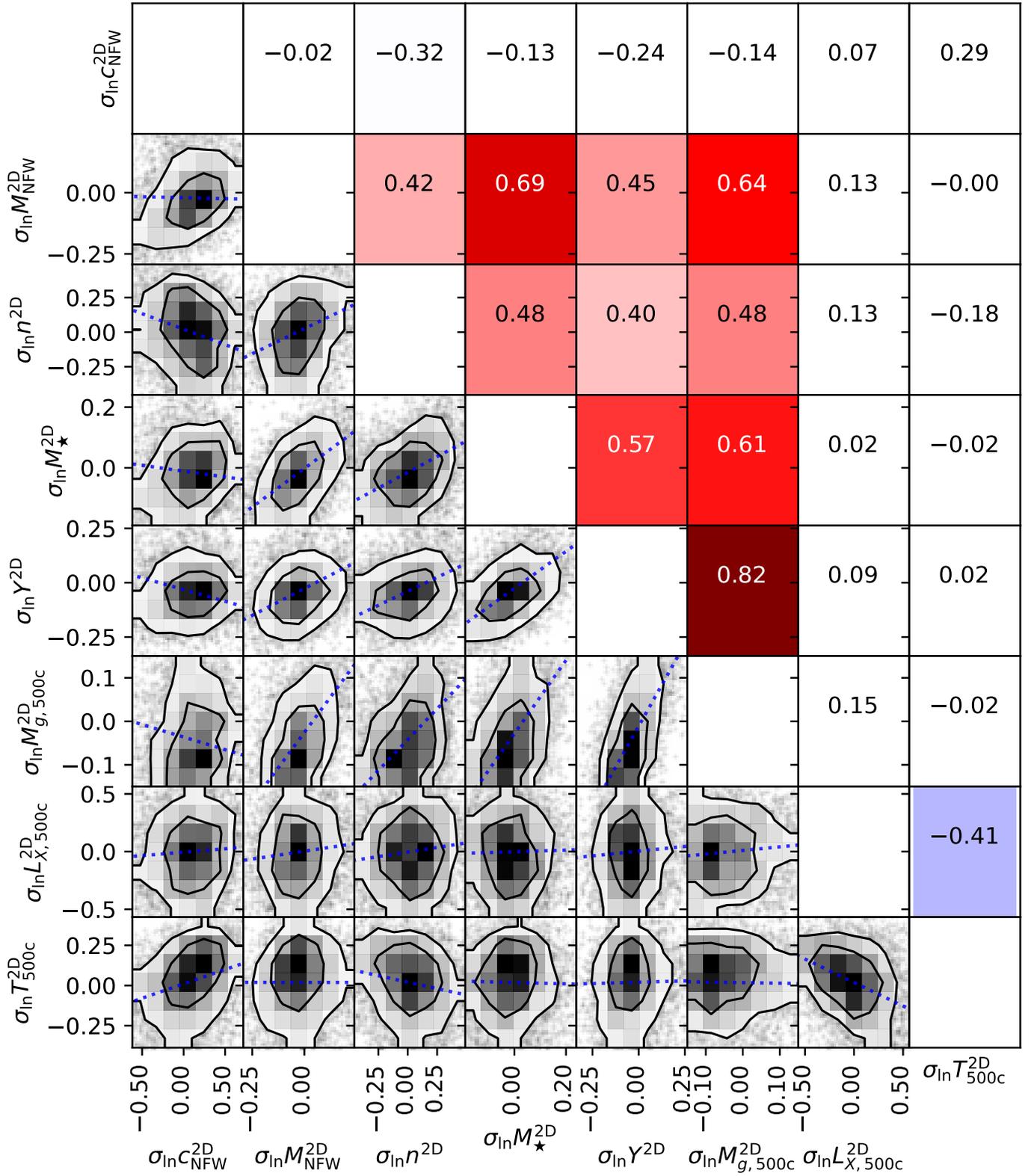
that in terms of 2D scatter, the properties with the lowest scatter are the stellar mass and the temperature. The bottom panel shows the data points used to perform the fit (in black). We used a visually-inspected cut on the halo mass values to ensure that mass values are complete for a given observable value.



**Fig. B.1.** Correlation coefficients matrix (*upper-right triangle*) and scatter plot (*bottom-left triangle*) of power-law log-residuals of *Euclid*-data (lensing concentration, lensing mass, richness, and stellar mass, respectively) and possible outcomes from multi-wavelength observations (integrated Compton- $y$  parameter, gas mass, X-ray luminosity, and temperature, respectively). Cell colouring goes from blue (negative correlation coefficients) to red (positive correlation coefficients) and is white in the interval  $[-0.35, 0.35]$  in order to enhance the visibility of the most significant coefficients.



**Fig. B.2.** Same as Fig. B.1 but here we show the quantities computed in the 3D space.



**Fig. B.3.** Same as Fig. B.1 but we show the projected X-ray luminosity, the projected gas mass, and the projected temperature computed within the overdensity of  $\Delta_c = 500$  instead of the respective quantities within  $\Delta_c = 200$ .

**Table B.1.** Scatter and correlation coefficient matrix between  $z = 0.24$  log-residuals of scaling relations.

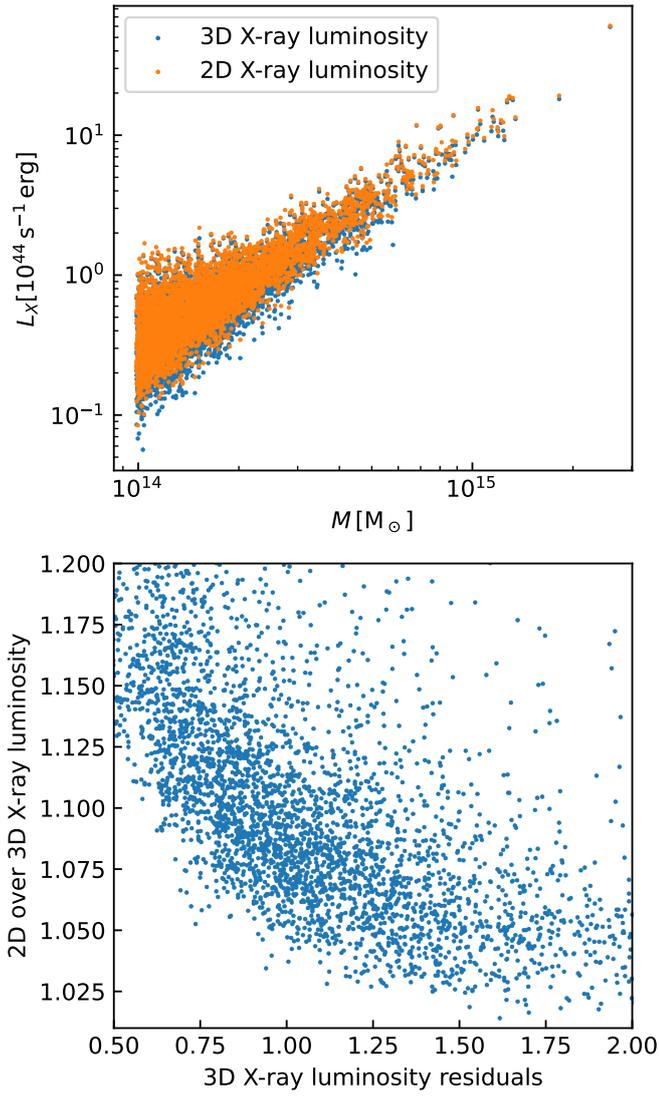
	$c_{\text{NFW}}$	$c_{\text{NFW}}^{2\text{D}}$	$M_{\text{NFW}}^{2\text{D}}$	$n$	$n^{2\text{D}}$	$M_{\star}$	$M_{\star}^{2\text{D}}$	$Y$	$Y^{2\text{D}}$	$M_g$	$M_g^{2\text{D}}$	$M_{g,500c}$	$M_{g,500c}^{2\text{D}}$	$L_X$	$L_X^{2\text{D}}$	$L_{X,500c}$	$L_{X,500c}^{2\text{D}}$	$L_{X,ce500c}^{2\text{D}}$	$T$	$T^{2\text{D}}$	$T_{500c}$	$T_{500c}^{2\text{D}}$	
$c_{\text{NFW}}$	0.33																						
$c_{\text{NFW}}^{2\text{D}}$	0.60	0.45																					
$M_{\text{NFW}}^{2\text{D}}$	--	--	0.18																				
$n$	-0.28	-0.22	--	0.28																			
$n^{2\text{D}}$	--	-0.32	0.42	0.71	0.31																		
$M_{\star}$	0.46	0.23	--	--	--	0.09																	
$M_{\star}^{2\text{D}}$	0.23	--	0.69	--	0.48	0.59	0.13																
$Y$	--	--	--	--	--	--	--	0.09															
$Y^{2\text{D}}$	--	-0.24	0.45	--	0.40	--	0.57	0.44	0.20														
$M_g$	-0.34	-0.21	--	0.23	0.23	-0.24	--	0.59	0.26	0.07													
$M_g^{2\text{D}}$	--	-0.26	0.59	--	0.52	--	0.63	0.21	0.85	0.21	0.20												
$M_{g,500c}$	--	0.35	--	--	--	--	--	0.54	--	0.48	--	0.14											
$M_{g,500c}^{2\text{D}}$	--	--	0.64	--	0.48	--	0.61	0.28	0.82	0.22	0.97	--	0.18										
$L_X$	--	--	--	--	--	--	--	0.20	--	0.40	--	0.36	--	0.35									
$L_X^{2\text{D}}$	--	--	0.20	--	0.26	--	--	0.20	--	0.37	0.23	0.31	0.26	0.91	0.35								
$L_{X,500c}$	--	--	--	--	--	--	--	0.29	--	0.33	--	0.55	--	0.91	0.82	0.41							
$L_{X,500c}^{2\text{D}}$	--	--	--	--	--	--	--	0.28	--	0.35	--	0.47	--	0.93	0.91	0.94	0.38						
$L_{X,ce500c}^{2\text{D}}$	-0.28	--	--	--	--	-0.24	--	0.28	--	0.49	--	0.56	--	0.59	0.62	0.52	0.66	0.33					
$T$	0.40	0.30	--	-0.20	--	--	--	0.31	--	--	--	0.28	--	-0.52	-0.48	-0.32	-0.40	--	0.26				
$T^{2\text{D}}$	0.39	0.30	--	--	--	--	--	0.31	--	--	--	0.30	--	-0.44	-0.53	-0.26	-0.37	--	0.94	0.27			
$T_{500c}$	0.38	0.27	--	--	--	--	--	0.26	--	--	--	0.21	--	-0.53	-0.49	-0.44	-0.46	--	0.94	0.88	0.28		
$T_{500c}^{2\text{D}}$	0.38	0.29	--	--	--	--	--	0.30	--	--	--	0.28	--	-0.47	-0.52	-0.29	-0.41	-0.21	0.95	0.98	0.91	0.27	

**Notes.** Diagonal terms report the scatter of the log-residuals of each quantity, namely  $\sigma_{\text{ln}}$  of Eq. (9), while the off-diagonal terms report the correlation coefficient between the log-residuals. We do not report values of the correlation coefficient below 0.20 because they are not significant. We do not report the values for the 3D NFW mass  $M_{200c}$  because it has a very low scatter of log-residuals ( $\approx 0.01$ ) and its correlation coefficients are not meaningful. Note that in this table we also added the core-excised X-ray luminosity.

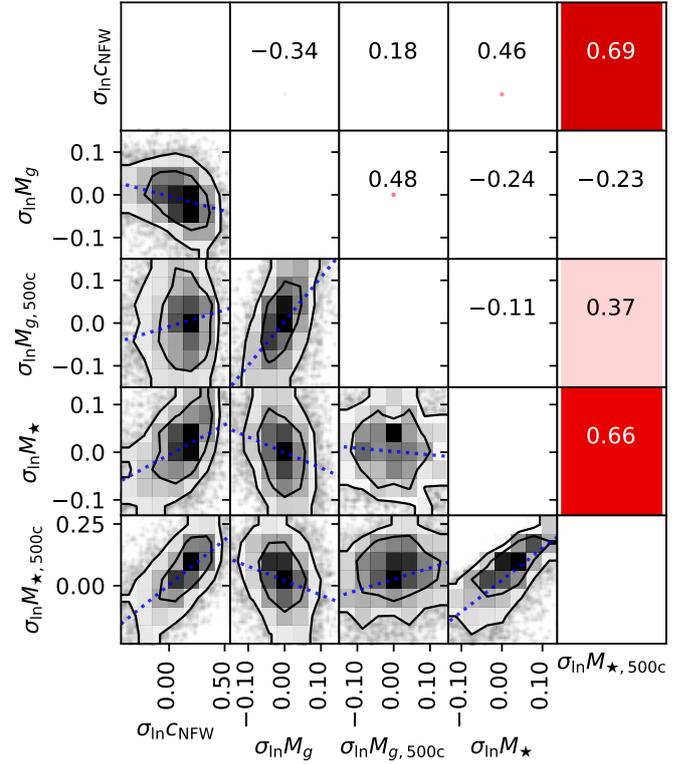
**Table B.2.** Scatter and correlation coefficient matrix between  $z = 0.9$  log-residuals of scaling relations.

	$c_{\text{NFW}}$	$c_{\text{NFW}}^{2\text{D}}$	$M_{\text{NFW}}^{2\text{D}}$	$n$	$n^{2\text{D}}$	$M_{\star}$	$M_{\star}^{2\text{D}}$	$Y$	$Y^{2\text{D}}$	$M_g$	$M_g^{2\text{D}}$	$M_{g,500c}$	$M_{g,500c}^{2\text{D}}$	$L_X$	$L_X^{2\text{D}}$	$L_{X,500c}$	$L_{X,500c}^{2\text{D}}$	$L_{X,ce500c}^{2\text{D}}$	$T$	$T^{2\text{D}}$	$T_{500c}$	$T_{500c}^{2\text{D}}$	
$c_{\text{NFW}}$	0.32																						
$c_{\text{NFW}}^{2\text{D}}$	0.51	0.44																					
$M_{\text{NFW}}^{2\text{D}}$	--	--	0.21																				
$n$	-0.28	--	--	0.26																			
$n^{2\text{D}}$	-0.22	-0.34	0.51	0.70	0.31																		
$M_{\star}$	0.37	--	--	--	--	0.08																	
$M_{\star}^{2\text{D}}$	--	-0.31	0.78	--	0.57	0.47	0.15																
$Y$	0.34	0.27	--	-0.23	--	--	--	0.08															
$Y^{2\text{D}}$	--	-0.30	0.63	--	0.32	--	0.64	0.41	0.17														
$M_g$	-0.29	--	--	0.23	0.21	-0.30	--	0.40	0.20	0.05													
$M_g^{2\text{D}}$	--	-0.38	0.78	--	0.53	--	0.71	--	0.79	--	0.20												
$M_{g,500c}$	--	0.41	--	--	--	-0.28	-0.25	0.52	--	0.44	--	0.15											
$M_{g,500c}^{2\text{D}}$	--	-0.24	0.80	--	0.49	--	0.67	--	0.77	--	0.96	--	0.18										
$L_X$	-0.20	--	--	0.26	--	--	--	--	0.51	--	0.51	--	0.25										
$L_X^{2\text{D}}$	--	--	0.42	0.26	0.48	--	0.32	--	0.22	0.44	0.39	0.35	0.44	0.79	0.28								
$L_{X,500c}$	--	0.26	--	--	--	--	--	0.32	--	0.45	--	0.73	--	0.89	0.67	0.30							
$L_{X,500c}^{2\text{D}}$	--	--	0.23	0.23	0.29	-0.23	--	0.23	--	0.50	--	0.59	0.22	0.87	0.86	0.87	0.28						
$L_{X,ce500c}^{2\text{D}}$	-0.31	--	0.25	0.22	0.31	-0.30	--	--	0.49	--	0.58	0.24	0.69	0.75	0.65	0.85	0.31						
$T$	0.52	0.40	--	-0.22	--	--	--	0.52	--	--	--	0.33	--	--	--	--	--	--	0.22				
$T^{2\text{D}}$	0.47	0.43	--	-0.22	-0.28	--	--	0.50	--	--	-0.20	0.37	--	--	-0.28	--	--	--	0.90	0.24			
$T_{500c}$	0.52	0.35	--	-0.21	--	--	--	0.45	--	--	--	0.21	--	--	--	--	--	--	0.95	0.84	0.22		
$T_{500c}^{2\text{D}}$	0.48	0.41	--	-0.21	-0.27	--	--	0.49	--	--	--	0.34	--	--	-0.27	--	--	--	0.90	0.98	0.86	0.23	

**Notes.** Rows and columns are as in Table B.1.



**Fig. B.4.** Comparison between 3D and projected X-ray luminosities. Top panel shows a scatter plot of the two mass-observable relations, while the bottom panel shows their ratio as a function of the 3D X-ray scaling relation residuals.



**Fig. B.5.** We report the correlation coefficient between the concentration, gas mass, and stellar mass computed at both  $r_{500c}$  and  $r_{200c}$ .

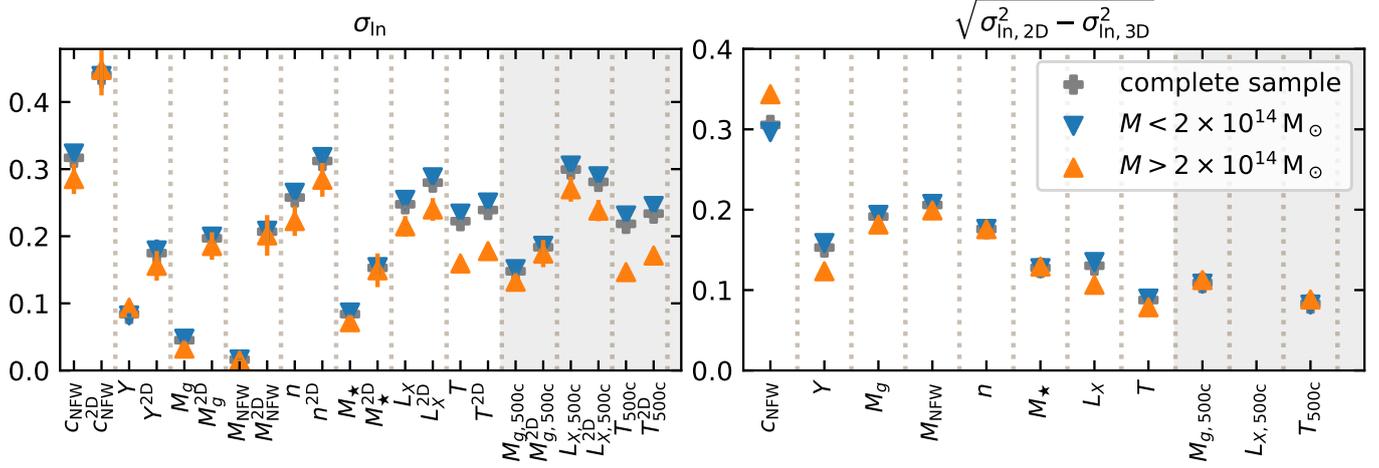


Fig. B.6. Same as Fig. 3 but for the data at  $z = 0.9$ .

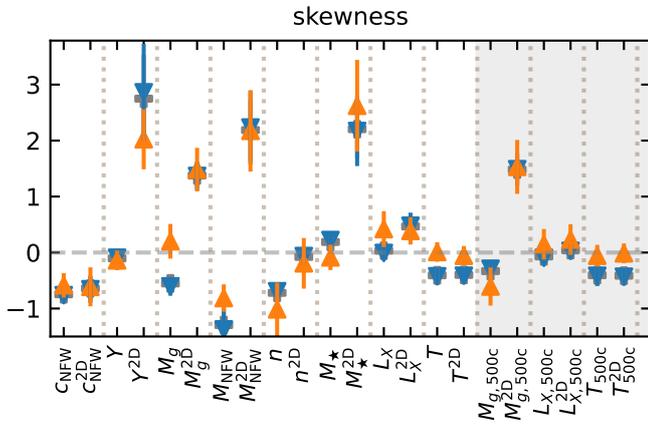
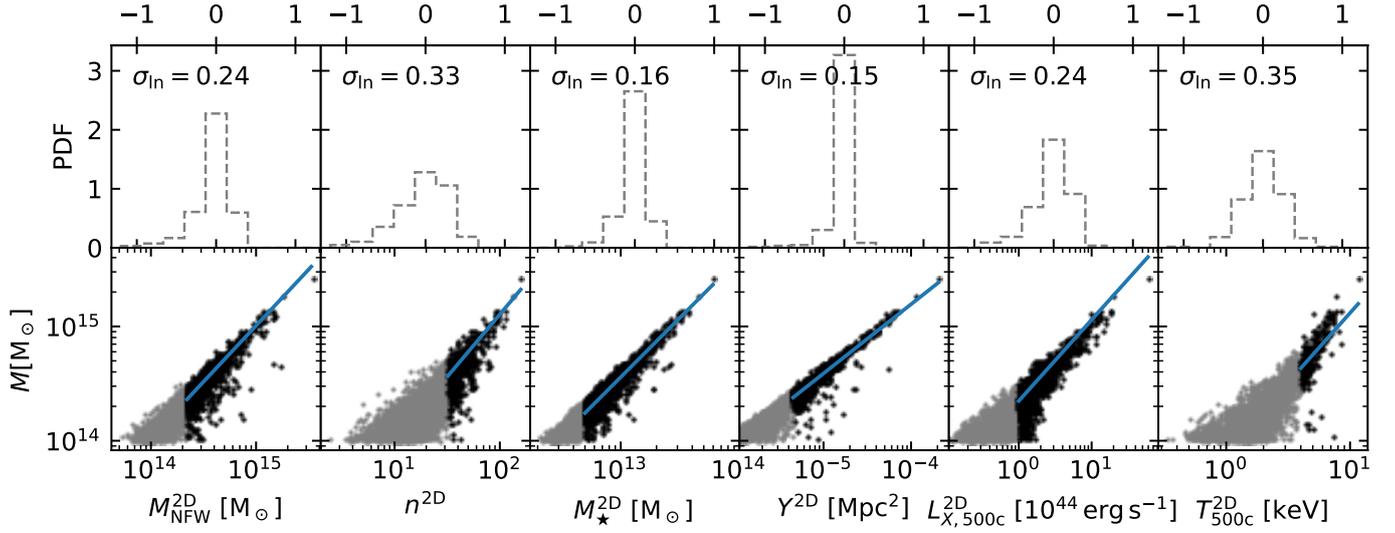


Fig. B.7. Same as Fig. 4 but for the data at  $z = 0.9$ . We do not report the value for the concentration because in our fit radial range the lensing one does not correlate with the 3D one.



**Fig. B.8.** Halo masses at fixed observable properties. We report the lensing mass, lensing richness, projected stellar mass, projected integrated Compton- $y$ , projected X-ray luminosity, and projected temperature in each column, respectively. The top panel shows residuals of the observable-mass relations and respective scatter of log-residuals  $\sigma_{\ln}$ , and its axes are on the upper part of the plot. The bottom panel shows the scaling relation fit (blue solid line); the data used to perform the fit (black data points) over-plotted on top of the total sample (grey data points) of the mass  $M$  as a function of the observable properties.